# celestine

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**CHAPTER** 

**ONE** 

## **CELESTINE**

## 1.1 celestine package

## 1.1.1 Subpackages

celestine.diagnostics package

**Submodules** 

celestine.diagnostics.brine\_drainage\_parameterisation module

celestine.diagnostics.brine\_drainage\_parameterisation.main(output\_dir: Path)

**Module contents** 

celestine.enthalpy\_method package

**Submodules** 

celestine.enthalpy\_method.common module

celestine.enthalpy\_method.common.calculate\_common\_enthalpy\_method\_vars(state: EQMState |

DISEQState, cfg:
Config, phase\_masks)

→ Tuple[ndarray[Any,
dtype[\_ScalarType\_co]],
ndarray[Any,
dtype[\_ScalarType\_co]],
ndarray[Any,
dtype[\_ScalarType\_co]],
ndarray[Any,
dtype[\_ScalarType\_co]]]

## celestine.enthalpy\_method.enthalpy\_method module

Module containing enthalpy method to calculate state variables from bulk enthalpy, bulk salinity and bulk gas.

 $\texttt{celestine.enthalpy\_method.enthalpy\_method.get\_enthalpy\_method}(\textit{cfg:} \ \texttt{Config}) \rightarrow \\$ 

Callable[[EQMState | DISEQState], EQMStateFull | DISEQStateFull]

### celestine.enthalpy\_method.gas module

 ${\tt celestine.enthalpy\_method.gas.} {\tt calculate\_DISEQ\_dissolved\_gas} ({\it state:} \ {\tt DISEQState}, {\it liquid\_fraction}, \\$ 

physical\_params:
EQMPhysicalParams |
DISEQPhysicalParams,
phase\_masks) → ndarray[Any,
dtype[\_ScalarType\_co]]

celestine.enthalpy\_method.gas.calculate\_EQM\_dissolved\_gas(state: EQMState, liquid\_fraction,

physical\_params: EQMPhysicalParams |
DISEQPhysicalParams) → ndarray[Any,
dtype[\_ScalarType\_co]]

 $celestine.enthalpy\_method.gas. \textbf{calculate\_EQM\_gas\_fraction} (\textit{state}: EQMS tate, \textit{liquid\_fraction}: and \textit{liquid\_fraction}) and \textit{liquid\_fraction} (\textit{state}: EQMS tate, \textit{liquid\_fraction}) and \textit{liquid\_fraction}) and \textit{liquid\_fraction} (\textit{liquid\_fraction}) and \textit{liquid\_fract$ 

 $ndarray[Any, dtype[\_ScalarType\_co]], physical\_params: EQMPhysicalParams | DISEQPhysicalParams) <math>\rightarrow$  ndarray[Any, dtype[\\_ScalarType\\_co]]

### celestine.enthalpy\_method.phase\_boundaries module

Module for calculating the phase boundaries needed for the enthalpy method. calculates the phase boundaries neglecting the gas fraction so that

$$\phi_s + \phi_l = 1$$

celestine.enthalpy\_method.phase\_boundaries.get\_phase\_masks(state: EQMState | DISEQState, physical\_params: EQMPhysicalParams | DISEQPhysicalParams)

**Module contents** 

celestine.equations package

**Subpackages** 

celestine.equations.RJW14 package

#### **Submodules**

## celestine.equations.RJW14.brine\_channel\_sink\_terms module

## celestine.equations.RJW14.brine\_drainage module

Module to calculate the Rees Jones and Worster 2014 parameterisation for brine convection velocity and the strength of the sink term.

Exports the functions:

calculate\_brine\_convection\_liquid\_velocity To be used in velocities module when using brine convection parameterisation.

calculate\_brine\_channel\_sink To be used to add sink terms to conservation equations when using brine convection parameterisation.

Calculate the local Rayleigh number for brine convection as

$$Ra(z) = Ra_S K(z)(z+h)\Theta_l$$

#### **Parameters**

- **cell\_centers** (*Numpy Array shape* (*I*,)) The vertical coordinates of cell centers.
- edge\_grid (Numpy Array (size I+1)) The vertical coordinate positions of the edge grid.
- liquid\_salinity (Numpy Array shape (I,)) liquid salinity on center grid
- liquid\_fraction (Numpy Array (size I)) liquid fraction on center grid
- **cfg** (*celestine.params.Config*) Configuration object for the simulation.

#### Returns

Array of shape (I,) of Rayleigh number at cell centers

celestine.equations.RJW14.brine\_drainage.calculate\_brine\_channel\_sink(liquid\_fraction,

liquid\_salinity,
center\_grid, edge\_grid,
cfg: Config)

Calculate the sink term due to brine channels.

sink = A

in the convecting region. Zero elsewhere.

NOTE: If no ice is present or if no convecting region exists returns zero

#### **Parameters**

- liquid\_fraction (Numpy Array of shape (I,)) liquid fraction on center grid
- liquid\_salinity (Numpy Array of shape (I,)) liquid salinity on center grid
- center\_grid (Numpy Array of shape (I,)) vertical coordinate of center grid
- edge\_grid (Numpy Array of shape (I+1,)) Vertical coordinates of cell edges
- **cfg** (*celestine.params.Config*) Configuration object for the simulation.

#### Returns

Strength of the sink term due to brine channels on the center grid.

ice\_depth, convecting\_region\_height,
cfg: Config)

Calculate the brine channel strength in the convecting region as

$$\mathcal{A} = \frac{\alpha \mathrm{Ra}_e}{(h + z_c)^2}$$

the effective Rayleigh number multiplied by a tuning parameter (Rees Jones and Worster 2014) over the convecting region thickness squared.

## **Parameters**

- Rayleigh\_number (Numpy Array of shape (I,)) local Rayleigh number on center grid
- ice\_depth (float) depth of ice (positive)
- **convecting\_region\_height** (*float*) position of the convecting region boundary (negative)
- **cfg** (*celestine.params.Config*) Configuration object for the simulation.

## Returns

Brine channel strength parameter

celestine.equations.RJW14.brine\_drainage.calculate\_brine\_convection\_liquid\_velocity(liquid\_fraction,

liquid\_salinity,
center\_grid,
edge\_grid,
cfg:
Config)

Calculate the vertical liquid Darcy velocity from Rees Jones and Worster 2014

$$W_l = \mathcal{A}(z_c - z)$$

in the convecting region. The velocity is stagnant above the convecting region. The velocity is constant in the liquid region and continuous at the interface.

NOTE: If no ice is present or if no convecting region exists returns zero velocity

## **Parameters**

- liquid\_fraction (Numpy Array of shape (I,)) liquid fraction on center grid
- liquid\_salinity (Numpy Array of shape (I,)) liquid salinity on center grid
- center\_grid (Numpy Array of shape (I,)) vertical coordinate of center grid
- edge\_grid (Numpy Array of shape (I+1,)) Vertical coordinates of cell edges
- **cfg** (*celestine.params.Config*) Configuration object for the simulation.

#### Returns

Liquid darcy velocity on the edge grid.

celestine.equations.RJW14.brine\_drainage.calculate\_integrated\_mean\_permeability(z, liq-

uid\_fraction,
ice\_depth,
cell\_centers,
cfg:

Config)

Calculate the harmonic mean permeability from the base of the ice up to the cell containing the specified z value using the expression of ReesJones2014.

$$K(z) = (\frac{1}{h+z} \int_{-h}^{z} \frac{1}{\Pi(\phi_{l}(z'))} dz')^{-1}$$

#### **Parameters**

- **z** (*float*) height to integrate permeability up to
- liquid\_fraction (Numpy Array shape (I,)) liquid fraction on the center grid
- ice\_depth (float) positive depth position of ice ocean interface
- cell\_centers (Numpy Array of shape (I,)) cell center positions
- **cfg** (*celestine.params.Config*) Configuration object for the simulation.

#### Returns

permeability averaged from base of the ice up to given z value

 ${\tt celestine.equations.RJW14.brine\_drainage.} \textbf{\textit{calculate\_permeability}} (\textit{liquid\_fraction}, \textit{cfg}: \texttt{Config})$ 

Calculate the absolute permeability as a function of liquid fraction

$$\Pi(\phi_l) = \phi_l^3$$

Alternatively if the porosity threshold flag is true

$$\Pi(\phi_l) = \phi_l^2(\phi_l - \phi_c)$$

#### **Parameters**

- liquid\_fraction (Numpy Array) liquid fraction
- **cfg** (*celestine.params.Config*) Configuration object for the simulation.

#### Returns

permeability on the same grid as liquid fraction

celestine.equations.RJW14.brine\_drainage.get\_convecting\_region\_height(Rayleigh\_number, edge\_grid, cfg: Config)

Calculate the height of the convecting region as the top edge of the highest cell in the domain for which the quantity

$$Ra(z) - Ra_c$$

is greater than or equal to zero.

NOTE: if no convecting region exists return np.NaN

#### **Parameters**

- Rayleigh\_number (Numpy Array of shape (I,)) local rayleigh number on center grid
- edge\_grid (Numpy Array (size I+1)) The vertical coordinate positions of the edge grid.
- **cfg** (*celestine.params.Config*) Configuration object for the simulation.

#### Returns

Edge grid value at convecting boundary.

celestine.equations.RJW14.brine\_drainage.get\_effective\_Rayleigh\_number(Rayleigh\_number, cfg: Config)

Calculate the effective Rayleigh Number as the maximum of

$$Ra(z) - Ra_c$$

in the convecting region.

NOTE: if no convecting region exists returns 0.

#### **Parameters**

- Rayleigh\_number (Numpy Array of shape (I,)) local rayleigh number on center grid
- **cfg** (*celestine.params.Config*) Configuration object for the simulation.

#### Returns

Effective Rayleigh number.

#### **Module contents**

Module to calculate the sink terms for conservation equations when using the Rees Jones and Worster 2014 brine drainage parameterisation.

These terms represent loss through the brine channels and need to be added in the convecting region when using this parameterisation

## celestine.equations.flux package

#### **Submodules**

### celestine.equations.flux.bulk\_dissolved\_gas\_flux module

calculate the flux terms for the dissolved gas equation in DISEQ model celestine.equations.flux.bulk\_dissolved\_gas\_flux.calculate\_bulk\_dissolved\_gas\_flux( $state\_BCs$ , Wl, V,  $D_\_g$ , cfg)

## celestine.equations.flux.bulk\_gas\_flux module

celestine.equations.flux.bulk\_gas\_flux.calculate\_advective\_dissolved\_gas\_flux(dissolved\_gas, Wl, cfg)

celestine.equations.flux.bulk\_gas\_flux.calculate\_bubble\_gas\_flux(gas\_fraction, Vg)

celestine.equations.flux.bulk\_gas\_flux.calculate\_diffusive\_gas\_flux(dissolved\_gas, liquid\_fraction, D\_g, cfg)

celestine.equations.flux.bulk\_gas\_flux.calculate\_frame\_advection\_gas\_flux(gas, V)

celestine.equations.flux.bulk\_gas\_flux.calculate\_gas\_flux(state\_BCs, Wl, V, Vg, D\_g, cfg)

## celestine.equations.flux.gas\_fraction\_flux module

Calculate gas phase fluxes for disequilibrium model celestine.equations.flux.gas\_fraction\_flux.calculate\_gas\_fraction\_flux(state\_BCs, V, Vg)

#### celestine.equations.flux.heat\_flux module

celestine.equations.flux.heat\_flux.calculate\_advective\_heat\_flux(temperature, Wl)

celestine.equations.flux.heat\_flux.calculate\_conductive\_heat\_flux(state\_BCs, D\_g, cfg)

Calculate conductive heat flux as

$$-\frac{\partial \theta}{\partial z}$$

or alteratively if the phase\_average\_conductivity configuration parameter is set to True then we use the conductivity ratio as follows

$$-[(\phi_l + \lambda \phi_s) \frac{\partial \theta}{\partial z}]$$

#### **Parameters**

- **temperature** (*Numpy Array of size I+2*) temperature including ghost cells
- **D\_g** (Numpy Array) difference matrix for ghost grid

• cfg (celestine.params.Config) - Simulation configuration

#### Returns

conductive heat flux

celestine.equations.flux.heat\_flux.calculate\_frame\_advection\_heat\_flux(enthalpy, V) celestine.equations.flux.heat\_flux.calculate\_heat\_flux(state\_BCs, Wl, V, D\_g, cfg)

#### celestine.equations.flux.salt flux module

celestine.equations.flux.salt\_flux.calculate\_advective\_salt\_flux(liquid\_salinity, Wl, cfg) celestine.equations.flux.salt\_flux.calculate\_diffusive\_salt\_flux(liquid\_salinity, liquid\_fraction,  $D_g$ , cfg)

Take liquid salinity and liquid fraction on ghost grid and interpolate liquid fraction geometrically celestine.equations.flux.salt\_flux.calculate\_frame\_advection\_salt\_flux(salt, V) celestine.equations.flux.salt\_flux.calculate\_salt\_flux(state\_BCs, Wl, V, D\_g, cfg)

#### Module contents

Module for calculating the fluxes using upwind scheme

```
celestine.equations.flux. \textbf{get\_dz\_fluxes}(cfg: Config, grids: Grids) \rightarrow Callable[[EQMStateBCs \mid DISEQStateBCs, ndarray[Any, dtype[\_ScalarType\_co]], ndarray[Any, dtype[\_ScalarType\_co]], ndarray[Any, dtype[\_ScalarType\_co]]], ndarray[Any, dtype[\_ScalarType\_co]]]
```

## celestine.equations.velocities package

#### **Submodules**

## celestine.equations.velocities.bubble\_parameters module

celestine.equations.velocities.bubble\_parameters.calculate\_bubble\_size\_fraction(bubble\_radius\_scaled, liq-uid\_fraction, cfg:

Config)

Takes bubble radius scaled and liquid fraction on edges and calculates the bubble size fraction as

$$\lambda = \Lambda/(\phi_l^q + \text{reg})$$

Returns the bubble size fraction on the edge grid.

## celestine.equations.velocities.mono\_distribution module

celestine.equations.velocities.mono\_distribution.calculate\_lag\_function(bubble\_size\_fraction)

Calculate lag function from bubble size fraction on edge grid as

$$G(\lambda) = 1 - \lambda/2$$

for 0<lambda<1. Edge cases are given by G(0)=1 and G(1)=0.5 for values outside this range.

celestine.equations.velocities.mono\_distribution.calculate\_mono\_lag\_factor(liquid\_fraction,

*cfg:* Config)

Take liquid fraction on the ghost grid and calculate the lag factor for a mono bubble size distribution as

$$I_2 = G(\lambda)$$

returns lag factor on the edge grid

 $celestine. equations. velocities. {\tt mono\_distribution.} \textbf{calculate\_mono\_wall\_drag\_factor} (\textit{liquid\_fraction}, \textbf{calculate\_mono\_wall\_drag\_factor}) \\$ 

*cfg:* Config)

Take liquid fraction on the ghost grid and calculate the wall drag factor for a mono bubble size distribution as

$$I_1 = \frac{\lambda^2}{K(\lambda)}$$

returns wall drag factor on the edge grid

celestine.equations.velocities.mono\_distribution.calculate\_wall\_drag\_function(bubble\_size\_fraction, cfg: Config)

Calculate wall drag function from bubble size fraction on edge grid as

$$\frac{1}{K(\lambda)} = (1 - \lambda)^r$$

in the power law case or in the Haberman case from the paper

$$\frac{1}{K(\lambda)} = \frac{1 - 1.5\lambda + 1.5\lambda^5 - \lambda^6}{1 + 1.5\lambda^5}$$

for 0 < lambda < 1. Edge cases are given by K(0)=1 and K(1)=0 for values outside this range.

#### celestine.equations.velocities.power law distribution module

celestine.equations.velocities.power\_law\_distribution.calculate\_lag\_integral(bubble\_size\_fraction\_min: float, bub-

oat, bub-

ble\_size\_fraction\_max:

float, cfg:

Config)

 $celestine. equations. velocities. power\_law\_distribution. \textbf{calculate\_lag\_integrand} (\textit{bubble\_size\_fraction:} \\$ 

float, cfg: Config)

Scalar function to calculate lag integrand for polydispersive case.

Bubble size fraction is given as a scalar input to calculate

$$\lambda^{3-p}G(\lambda)$$

```
celestine.equations.velocities.power_law_distribution.calculate_power_law_lag_factor(liquid_fraction,
                                                                                                     cfg:
                                                                                                     Con-
                                                                                                     fig)
     Take liquid fraction on the ghost grid and calculate the lag factor for power law bubble size distribution.
     Return on edge grid
celestine.equations.velocities.power_law_distribution.calculate_power_law_wall_drag_factor(liquid fraction,
                                                                                                            cfg:
                                                                                                           Con-
                                                                                                           fig)
     Take liquid fraction on the ghost grid and calculate the wall drag factor for power law bubble size distribution.
     Return on edge grid
celestine.equations.velocities.power_law_distribution.calculate_volume_integrand(bubble_size_fraction:
                                                                                               float, cfg:
                                                                                                Config)
     Scalar function to calculate the integrand for volume under a power law bubble size distribution given as
                                                     \lambda^{3-p}
     in terms of the bubble size fraction.
celestine.equations.velocities.power_law_distribution.calculate_wall_drag_integral(bubble_size_fraction_min:
                                                                                                  float,
                                                                                                  bub-
                                                                                                  ble_size_fraction_max:
                                                                                                  float,
                                                                                                  cfg:
                                                                                                  Config)
celestine.equations.velocities.power_law_distribution.calculate_wall_drag_integrand(bubble_size_fraction:
                                                                                                   float,
                                                                                                   cfg:
                                                                                                   Con-
                                                                                                   fig)
     Scalar function to calculate wall drag integrand for polydispersive case.
     Bubble size fraction is given as a scalar input to calculate
     where the wall drag enhancement funciton K can be given by a power law fit or taken from the Haberman paper.
celestine.equations.velocities.velocities module
celestine.equations.velocities.velocities.calculate_frame_velocity(cfg: Config)
celestine.equations.velocities.velocities.calculate_gas_interstitial_velocity(liquid_fraction,
```

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liq-

uid\_darcy\_velocity,
wall\_drag\_factor,
lag\_factor,
cfg: Config)

Calculate Vg from liquid fraction on the ghost frid and liquid interstitial velocity

$$V_g = \mathcal{B}(\phi_l^{2q} I_1) + U_0 I_2$$

Return Vg on edge grid

celestine.equations.velocities.velocities.calculate\_liquid\_darcy\_velocity(liquid\_fraction, liquid\_salinity, center\_grid, edge\_grid, cfg: Config)

Calculate liquid Darcy velocity either using brine convection parameterisation or as stagnant

#### **Parameters**

- liquid\_fraction (Numpy Array (size I+2)) liquid fraction on ghost grid
- liquid\_salinity (Numpy Array (size I+2)) liquid salinity on ghost grid
- center\_grid (Numpy Array of shape (I,)) vertical coordinates of cell centers
- edge\_grid (Numpy Array (size I+1)) Vertical coordinates of cell edges
- cfg (celestine.params.Config) simulation configuration object

#### Returns

liquid darcy velocity on edge grid

celestine.equations.velocities.velocities.calculate\_velocities(state\_BCs, cfg: Config)
Inputs on ghost grid, outputs on edge grid

needs the simulation config, liquid fraction, liquid salinity and grids

## **Module contents**

Module to calculate Darcy velocities.

The liquid Darcy velocity must be parameterised.

The gas Darcy velocity is calculated as gas\_fraction x interstitial bubble velocity

Interstitial bubble velocity is found by a steady state Stoke's flow calculation. We have implemented two cases mono: All bubbles nucleate and remain the same size power\_law: A power law bubble size distribution with fixed max and min.

#### **Submodules**

### celestine.equations.equations module

 $\label{eq:config} \textbf{celestine.equations.get\_equations}(\textit{cfg:} Config, \textit{grids}) \rightarrow \textbf{Callable}[[\textit{EQMStateBCs} \mid \textit{DISEQStateBCs}], \textit{ndarray}[Any, dtype[\_ScalarType\_co]]]$ 

### celestine.equations.nucleation module

```
celestine.equations.nucleation. \textbf{get\_nucleation}(\textit{cfg:} Config) \rightarrow Callable[[\textit{EQMStateBCs} \mid \textit{DISEQStateBCs}], ndarray[Any, dtype[\_ScalarType\_co]]]
```

## celestine.equations.radiative\_heating module

Calculate internal shortwave radiative heating due to oil droplets

```
celestine.equations.radiative_heating.get_radiative_heating(cfg: Config, grids: Grids) \rightarrow Callable[[EQMStateBCs | DISEQStateBCs], ndarray[Any, dtype[_ScalarType_co]]]
```

Calculate internal shortwave heating source for enthalpy equation.

if the RadForcing object is given as the forcing config then calculates internal heating based on the object given in the configuration for oil\_heating.

If another forcing is chosen then just returns a function to create an array of zeros as no internal heating is calculated.

#### Module contents

### celestine.forcing package

#### **Subpackages**

celestine.forcing.surface energy balance package

## **Submodules**

#### celestine.forcing.surface energy balance.surface energy balance module

Module to compute the surface heat flux from geophysical energy balance

```
following [1]
```

Refs: [1] P. D. Taylor and D. L. Feltham, 'A model of melt pond evolution on sea ice', J. Geophys. Res., vol. 109, no. C12, p. 2004JC002361, Dec. 2004, doi: 10.1029/2004JC002361.

```
celestine.forcing.surface_energy_balance.surface_energy_balance.calculate_emissivity(cfg:
```

```
Config,

top_cell_is_ice:

bool)

→

float
```

```
celestine.forcing.surface_energy_balance.surface_energy_balance.calculate_total_heat_flux(cfg:
                                                                                                         Con-
                                                                                                         fig,
                                                                                                         time:
                                                                                                         float,
                                                                                                         top_cell_is_ice:
                                                                                                         bool,
                                                                                                         sur-
                                                                                                         face_temp:
                                                                                                         float)
                                                                                                         \rightarrow
                                                                                                         float
     Takes non-dimensional surface temperature and returns non-dimensional heat flux
celestine.forcing.surface_energy_balance.surface_energy_balance.convert_surface_temperature_to_kelvin(c)
celestine.forcing.surface_energy_balance.surface_energy_balance.find_ghost_cell_temperature(state:
                                                                                                           EQM-
                                                                                                           State-
                                                                                                           Full
                                                                                                           DIS-
                                                                                                           E-
                                                                                                           QS-
                                                                                                           tate-
                                                                                                           Full,
                                                                                                           cfg:
                                                                                                           Con-
                                                                                                           fig)
                                                                                                           \rightarrow
                                                                                                           float
celestine.forcing.surface_energy_balance.surface_energy_balance.solve_for_surface_temp(cfg:
                                                                                                      Con-
                                                                                                      fig,
                                                                                                     time:
                                                                                                     float,
                                                                                                     top_cell_solid_fraction
                                                                                                     float,
                                                                                                     top_cell_center_temp
                                                                                                     float,
                                                                                                     sec-
                                                                                                     ond_cell_center_tem
                                                                                                     float)
                                                                                                      float
```

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Returns non dimensional surface temperature

```
celestine.forcing.surface\_energy\_balance.surface\_energy\_balance.surface\_temp\_gradient (\it cfg: all of the context of the cont
```

```
Config,
sur-
face_temp:
float,
top_cell_center_temp:
float,
sec-
ond_cell_center_temp.
float)
→
float
```

Approximate non dimensional temperature gradient using the unknown surface temperature value (top of edge grid) and the top two known temperature values on the center grid

celestine.forcing.surface\_energy\_balance.surface\_energy\_balance.top\_cell\_conductivity(cfg:

```
Config,
solid_fraction:
float)
float
```

## celestine.forcing.surface\_energy\_balance.turbulent\_heat\_flux module

Module to compute the turbulent atmospheric sensible and latent heat fluxes

All temperatures are in Kelvin in this module

Refs: [1] P. D. Taylor and D. L. Feltham, 'A model of melt pond evolution on sea ice', J. Geophys. Res., vol. 109, no. C12, p. 2004JC002361, Dec. 2004, doi: 10.1029/2004JC002361.

[2] E. E. Ebert and J. A. Curry, 'An intermediate one-dimensional thermodynamic sea ice model for investigating ice-atmosphere interactions', Journal of Geophysical Research: Oceans, vol. 98, no. C6, pp. 10085–10109, 1993, doi: 10.1029/93JC00656.

celestine.forcing.surface\_energy\_balance.turbulent\_heat\_flux.calculate\_bulk\_transfer\_coefficient(cfg:

```
fig,
top_cell
bool,
time:
float,
sur-
face ten
```

float)  $\rightarrow$ float

Con-

Calculation of bulk transfer coeff from [2]

```
celestine.forcing.surface_energy_balance.turbulent_heat_flux.calculate_latent_heat_flux(cfg:
                                                                                                                                                                                                                                                                                                                                                                                                      Con-
                                                                                                                                                                                                                                                                                                                                                                                                      fig,
                                                                                                                                                                                                                                                                                                                                                                                                     time:
                                                                                                                                                                                                                                                                                                                                                                                                    float,
                                                                                                                                                                                                                                                                                                                                                                                                    top_cell_is_ice:
                                                                                                                                                                                                                                                                                                                                                                                                     bool,
                                                                                                                                                                                                                                                                                                                                                                                                     sur-
                                                                                                                                                                                                                                                                                                                                                                                                    face_temp:
                                                                                                                                                                                                                                                                                                                                                                                                    float)
                                                                                                                                                                                                                                                                                                                                                                                                     float
                    Calculate latent heat flux from [2]
celestine.forcing.surface_energy_balance.turbulent_heat_flux.calculate_ref_air_temp(cfg:
                                                                                                                                                                                                                                                                                                                                                                                    Con-
                                                                                                                                                                                                                                                                                                                                                                                    fig,
                                                                                                                                                                                                                                                                                                                                                                                   time:
                                                                                                                                                                                                                                                                                                                                                                                   float)
                                                                                                                                                                                                                                                                                                                                                                                    \rightarrow
                                                                                                                                                                                                                                                                                                                                                                                   float
                    return air temperature at reference level above the ice in Kelvin
                    in the configuration the air temperature is given in deg C
celestine.forcing.surface\_energy\_balance.turbulent\_heat\_flux. \textbf{calculate\_ref\_atmospheric\_pressure} (\textit{cfg}: \texttt{calculate\_ref\_atmospheric\_pressure}) (\textit{cfg}: \texttt{calculate\_pressure}) (\textit{cfg}: \texttt{calculate\_pre
                                                                                                                                                                                                                                                                                                                                                                                                                                        Con-
                                                                                                                                                                                                                                                                                                                                                                                                                                         fig,
                                                                                                                                                                                                                                                                                                                                                                                                                                         time:
                                                                                                                                                                                                                                                                                                                                                                                                                                        float)
                                                                                                                                                                                                                                                                                                                                                                                                                                         float
                    return atmospheric pressure at reference level above the ice
celestine.forcing.surface_energy_balance.turbulent_heat_flux.calculate_ref_specific_humidity(cfg:
                                                                                                                                                                                                                                                                                                                                                                                                                           Con-
                                                                                                                                                                                                                                                                                                                                                                                                                           fig,
                                                                                                                                                                                                                                                                                                                                                                                                                           time:
                                                                                                                                                                                                                                                                                                                                                                                                                           float)
                                                                                                                                                                                                                                                                                                                                                                                                                             \rightarrow
                                                                                                                                                                                                                                                                                                                                                                                                                           float
                    return specific humidity at reference level above the ice
celestine.forcing.surface_energy_balance.turbulent_heat_flux.calculate_ref_windspeed(cfg:
                                                                                                                                                                                                                                                                                                                                                                                        Con-
                                                                                                                                                                                                                                                                                                                                                                                        fig,
                                                                                                                                                                                                                                                                                                                                                                                        time:
                                                                                                                                                                                                                                                                                                                                                                                        float)
                                                                                                                                                                                                                                                                                                                                                                                         \rightarrow
                                                                                                                                                                                                                                                                                                                                                                                        float
```

return windspeed at reference level above the ice

```
celestine.forcing.surface\_energy\_balance.turbulent\_heat\_flux. \textbf{\textit{calculate\_sensible\_heat\_flux} (\textit{\textit{cfg}}: \texttt{\textit{cfg}}: \texttt{\textit{cfg}}:
```

```
Config,
time:
float,
top_cell_is_ice:
bool,
sur-
face_temp:
float)
\rightarrow
float
```

Calculate sensible heat flux from [2]

 $celestine.forcing.surface\_energy\_balance.turbulent\_heat\_flux. \textbf{calculate\_surface\_specific\_humidity} (\textit{cfg:} it is a constant of the consta$ 

fig,
time:
float,
surface\_ten
float)
→
float

Following expression given in [1]

#### **Module contents**

## **Submodules**

16

## celestine.forcing.boundary\_conditions module

Module to provide functions to add boundary conditions to each quantity on the centered grid that needs to be on the ghost grid for the upwind scheme.

```
celestine.forcing.boundary_conditions.get_boundary_conditions(cfg: Config) \rightarrow Callable[[EQMStateFull | DISEQStateFull], EQMStateBCs | DISEQStateBCs]
```

## celestine.forcing.radiative forcing module

Module for providing surface radiative forcing to simulation.

Currently only total surface shortwave irradiance (integrated over entire shortwave part of the spectrum) is provided and this is used to calculate internal radiative heating.

Unlike temperature forcing this provides dimensional forcing

```
celestine.forcing.radiative_forcing.get_LW_forcing(time: float, cfg: Config) \rightarrow float celestine.forcing.radiative_forcing.get_SW_forcing(time, cfg: Config)
```

### celestine.forcing.temperature forcing module

Module for providing surface temperature forcing to simulation.

Note that the barrow temperature data is read in from a file if needed by the simulation configuration.

celestine.forcing.temperature\_forcing.get\_bottom\_temperature\_forcing(time, cfg: Config)

 $celestine.forcing.temperature\_forcing.get\_temperature\_forcing(\textit{state}: EQMS tateFull \mid alternature\_forcing(\textit{state}: EQMS tateFull \mid alternature\_forcing(\textit{st$ 

DISEQStateFull, cfg: Config)

escape\_ice\_surface:
bool = True)

#### **Module contents**

celestine.params package

**Subpackages** 

celestine.params.dimensional package

#### **Submodules**

## celestine.params.dimensional.bubble module

```
\begin{tabular}{ll} \textbf{class} & \texttt{celestine.params.dimensional.bubble.DimensionalBaseBubbleParams}(pore\_radius: float = 0.001, & pore\_throat\_scaling: & float = 0.5, & porosity\_threshold: bool & = False, porosity\_threshold: bool & = False, porosity\_threshold\_value: & float = 0.024, & \\ \end{tabular}
```

Bases: object

escape\_ice\_surface: bool = True

pore\_radius: float = 0.001

pore\_throat\_scaling: float = 0.5

porosity\_threshold: bool = False

porosity\_threshold\_value: float = 0.024

class celestine.params.dimensional.bubble.DimensionalMonoBubbleParams(pore\_radius: float =

0.001,

pore\_throat\_scaling:

float = 0.5,

porosity\_threshold: bool

= False, poros-

 $ity\_threshold\_value:$ 

float = 0.024,

 $escape\_ice\_surface:$ 

bool = True,

bubble\_radius: float =

0.001)

Bases: DimensionalBaseBubbleParams

bubble\_radius: float = 0.001

property bubble\_radius\_scaled

calculate the bubble radius divided by the pore scale

$$\Lambda = R_B/R_0$$

 $\textbf{class} \ \ \textbf{celestine.params.dimensional.bubble.} \textbf{\textit{DimensionalPowerLawBubbleParams}} (\textit{pore\_radius: float})$ 

= 0.001,

pore\_throat\_scaling:

float = 0.5,

porosity threshold:

bool = False, poros

ity\_threshold\_value:

float = 0.024, es-

cape\_ice\_surface:

bool = True, bub

ble\_distribution\_power:

float = 1.5, mini-

mum\_bubble\_radius:

float = 1e-06, maxi-

mum\_bubble\_radius:

float = 0.001)

Bases: DimensionalBaseBubbleParams

bubble\_distribution\_power: float = 1.5

maximum\_bubble\_radius: float = 0.001

property maximum\_bubble\_radius\_scaled

calculate the bubble radius divided by the pore scale

$$\Lambda = R_B/R_0$$

minimum\_bubble\_radius: float = 1e-06

property minimum\_bubble\_radius\_scaled

calculate the bubble radius divided by the pore scale

$$\Lambda = R_B/R_0$$

## celestine.params.dimensional.convection module

class celestine.params.dimensional.convection.DimensionalRJW14Params(couple\_bubble\_to\_horizontal\_flow:

bool = False, couple\_bubble\_to\_vertical\_flow: bool = False, Rayleigh\_critical: float = 2.9, convection\_strength: float = 0.13, haline\_contraction\_coefficient: float = 0.00075, reference\_permeability: float = 1e-08)

Bases: object

Rayleigh\_critical: float = 2.9

convection\_strength: float = 0.13

couple\_bubble\_to\_horizontal\_flow: bool = False

couple\_bubble\_to\_vertical\_flow: bool = False

haline\_contraction\_coefficient: float = 0.00075

reference\_permeability: float = 1e-08

class celestine.params.dimensional.convection.NoBrineConvection

Bases: object

No brine convection

## celestine.params.dimensional.dimensional module

Dimensional parameters required to run a simulation and convert output to dimensional variables.

The Dimensional Params class contains all the dimensional parameters needed to produce a simulation configuration.

The Scales class contains all the dimensional parameters required to convert simulation output between physical and non-dimensional variables.

class celestine.params.dimensional.dimensional.DimensionalParams(name: str, total\_time\_in\_days:

float, savefreq\_in\_days: float, lengthscale: float, gas params: DimensionalEQMGasParams | DimensionalDISEQGasParams, bubble params: Dimensional-MonoBubbleParams | DimensionalPowerLawBubbleParams. brine\_convection\_params: DimensionalRJW14Params | NoBrineConvection, forcing\_config: Dimensional Rad Forcing | DimensionalBRW09Forcing | DimensionalConstantForcing | Dimensional Yearly Forcing, initial conditions config: DimensionalOilInitialConditions | UniformInitialConditions | BRW09InitialConditions, water params: DimensionalWaterParams = DimensionalWater-Params(liquid\_density=1028, ocean salinity=34, eutectic\_salinity=270, eutectic\_temperature=-21.1, ocean\_temperature=-0.81,  $latent\_heat=334000.0,$ specific\_heat\_capacity=4184, phase\_average\_conductivity=False, liquid\_thermal\_conductivity=0.54, solid thermal conductivity=2.22, salt\_diffusivity=0, liquid viscosity=0.00278), numerical\_params: NumericalParams = NumericalParams(I=50,regularisation=1e-06), frame\_velocity\_dimensional: float = 0, gravity: float = 9.81)

Bases: object

Contains all dimensional parameters needed to calculate non dimensional numbers.

To see the units each input should have look at the comment next to the default value.

#### property B

calculate the non dimensional scale for buoyant rise of gas bubbles as

$$\mathcal{B} = \frac{\rho_l g R_0^2 h}{3\mu\kappa}$$

### property Rayleigh\_salt

Calculate the haline Rayleigh number as

$$\mathbf{Ra}_{S} = \frac{\rho_{l}g\beta\Delta SHK_{0}}{\kappa\mu}$$

brine\_convection\_params: DimensionalRJW14Params | NoBrineConvection

bubble\_params: DimensionalMonoBubbleParams | DimensionalPowerLawBubbleParams

## property damkohler\_number

Return damkohler number as ratio of thermal timescale to nucleation timescale

#### property expansion\_coefficient

calculate

$$\chi = \rho_l \xi_{\rm sat} / \rho_a$$

forcing\_config: DimensionalRadForcing | DimensionalBRW09Forcing |
DimensionalConstantForcing | DimensionalYearlyForcing

## property frame\_velocity

calculate the frame velocity in non dimensional units

frame\_velocity\_dimensional: float = 0

gas\_params: DimensionalEQMGasParams | DimensionalDISEQGasParams

gravity: float = 9.81

initial\_conditions\_config: DimensionalOilInitialConditions |

UniformInitialConditions | BRW09InitialConditions

lengthscale: float

## property lewis\_gas

Calculate the lewis number for dissolved gas, return np.inf if there is no dissolved gas diffusion.

$$Le_{\varepsilon} = \kappa/D_{\varepsilon}$$

## classmethod load(path)

load this object from a yaml configuration file.

name: str

numerical\_params: NumericalParams = NumericalParams(I=50, regularisation=1e-06)

save(directory: Path)

save this object to a yaml file in the specified directory.

The name will be the name given with \_dimensional appended to distinguish it from a saved non-dimensional configuration.

## property savefreq

calculate the save frequency in non dimensional time

```
savefreq_in_days: float
     property scales
         return a Scales object used for converting between dimensional and non dimensional variables.
     property total_time
         calculate the total time in non dimensional units for the simulation
     total_time_in_days: float
     water_params: DimensionalWaterParams = DimensionalWaterParams(liquid_density=1028,
     ocean_salinity=34, eutectic_salinity=270, eutectic_temperature=-21.1,
     ocean_temperature=-0.81, latent_heat=334000.0, specific_heat_capacity=4184,
     phase_average_conductivity=False, liquid_thermal_conductivity=0.54,
     solid_thermal_conductivity=2.22, salt_diffusivity=0, liquid_viscosity=0.00278)
celestine.params.dimensional.forcing module
class celestine.params.dimensional.forcing.DimensionalBRW09Forcing(Barrow_top_temperature_data_choice:
                                                                        str = 'air'
     Bases: object
     Barrow_top_temperature_data_choice: str = 'air'
class celestine.params.dimensional.forcing.DimensionalBackgroundOilHeating(oil_mass_ratio:
                                                                                float = 0, ice_type:
                                                                                str = 'FYI'
     Bases: object
     ice_type: str = 'FYI'
     oil_mass_ratio: float = 0
class celestine.params.dimensional.forcing.DimensionalConstantForcing(constant_top_temperature:
                                                                           float = -30.32)
     Bases: object
     constant_top_temperature: float = -30.32
class celestine.params.dimensional.forcing.DimensionalConstantLWForcing(LW_irradiance: float
                                                                             = 260, ice_emissitivty:
                                                                             float = 0.99,
                                                                             water_emissivity: float
                                                                             = 0.97)
     Bases: object
     LW_irradiance: float = 260
     ice_emissitivty: float = 0.99
     water_emissivity: float = 0.97
class celestine.params.dimensional.forcing.DimensionalConstantSWForcing(SW_irradiance: float
                                                                             = 280, SW_albedo:
                                                                             float = 0.7,
                                                                             SW\_penetration\_fraction:
                                                                             float = 0.4)
```

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```
Bases: object
     SW_albedo: float = 0.7
     SW irradiance: float = 280
     SW_penetration_fraction: float = 0.4
class celestine.params.dimensional.forcing.DimensionalConstantTurbulentFlux(ref height: float
                                                                                 = 10, windspeed:
                                                                                 float = 5,
                                                                                 air_temp: float =
                                                                                 0, spe-
                                                                                 cific_humidity:
                                                                                 float = 0.0036,
                                                                                 atm_pressure:
                                                                                 float = 101.325,
                                                                                 air_density: float
                                                                                 = 1.275,
                                                                                 air_heat_capacity:
                                                                                 float = 1005,
                                                                                 air_latent_heat_of_vaporisation:
                                                                                 float =
                                                                                 2501000.0)
     Bases: object
     air_density: float = 1.275
     air_heat_capacity: float = 1005
     air_latent_heat_of_vaporisation: float = 2501000.0
     air_temp: float = 0
     atm_pressure: float = 101.325
     ref_height: float = 10
     specific_humidity: float = 0.0036
     windspeed: float = 5
celestine.params.dimensional.forcing.DimensionalLWForcing
     alias of DimensionalConstantLWForcing
class celestine.params.dimensional.forcing.DimensionalMobileOilHeating(ice_type: str = 'FYI')
     Bases: object
     ice_type: str = 'FYI'
class celestine.params.dimensional.forcing.DimensionalNoHeating
     Bases: object
```

```
class celestine.params.dimensional.forcing.DimensionalRadForcing(SW_forcing: celes-
                                                                        tine.params.dimensional.forcing.DimensionalCons
                                                                        DimensionalConstantSWForc-
                                                                        ing(SW irradiance=280,
                                                                        SW albedo=0.7,
                                                                        SW_penetration_fraction=0.4),
                                                                        LW_forcing: celes-
                                                                        tine.params.dimensional.forcing.DimensionalCons
                                                                        = DimensionalConstantLW-
                                                                        Forcing(LW_irradiance=260,
                                                                        ice_emissitivty=0.99,
                                                                        water_emissivity=0.97),
                                                                        turbulent_flux: celes-
                                                                        tine.params.dimensional.forcing.DimensionalCons
                                                                        = DimensionalConstantTurbu-
                                                                        lentFlux(ref_height=10,
                                                                        windspeed=5, air\ temp=0,
                                                                        specific_humidity=0.0036,
                                                                        atm\_pressure=101.325,
                                                                        air_density=1.275,
                                                                        air_heat_capacity=1005,
                                                                        air_latent_heat_of_vaporisation=2501000.0),
                                                                        oil heating: celes-
                                                                        tine.params.dimensional.forcing.DimensionalBack
                                                                        tine.params.dimensional.forcing.DimensionalMob
                                                                        celes-
                                                                        tine.params.dimensional.forcing.DimensionalNoH
                                                                        = DimensionalBackgroundOil-
                                                                        Heating(oil_mass_ratio=0,
                                                                        ice_type='FYI'))
     Bases: object
     LW_forcing: DimensionalConstantLWForcing =
     DimensionalConstantLWForcing(LW_irradiance=260, ice_emissitivty=0.99,
     water_emissivity=0.97)
     SW_forcing: DimensionalConstantSWForcing =
     DimensionalConstantSWForcing(SW_irradiance=280, SW_albedo=0.7,
     SW_penetration_fraction=0.4)
     oil_heating: DimensionalBackgroundOilHeating | DimensionalMobileOilHeating |
     DimensionalNoHeating = DimensionalBackgroundOilHeating(oil_mass_ratio=0,
     ice_type='FYI')
     turbulent_flux: DimensionalConstantTurbulentFlux =
     DimensionalConstantTurbulentFlux(ref_height=10, windspeed=5, air_temp=0,
     specific_humidity=0.0036, atm_pressure=101.325, air_density=1.275,
     air_heat_capacity=1005, air_latent_heat_of_vaporisation=2501000.0)
celestine.params.dimensional.forcing.DimensionalSWForcing
     alias of DimensionalConstantSWForcing
```

```
celestine.params.dimensional.forcing.DimensionalTurbulentFlux
     alias \ of \ {\it Dimensional Constant Turbulent Flux}
class celestine.params.dimensional.forcing.DimensionalYearlyForcing(offset: float = -1.0,
                                                                             amplitude: float = 0.75,
                                                                             period: float = 4.0)
     Bases: object
     amplitude: float = 0.75
     offset: float = -1.0
     period: float = 4.0
celestine.params.dimensional.gas module
class celestine.params.dimensional.gas.DimensionalDISEQGasParams(gas\_density: float = 1,
                                                                         saturation_concentration: float
                                                                          = 1e-05,
                                                                          ocean_saturation_state: float =
                                                                          1.0, gas\_diffusivity: float = 0,
                                                                          tolera-
                                                                         ble_super_saturation_fraction:
                                                                         float = 1, nucleation\_timescale:
                                                                         float = 6869075)
     Bases: DimensionalEQMGasParams
     nucleation_timescale: float = 6869075
class celestine.params.dimensional.gas.DimensionalEQMGasParams(gas density: float = 1,
                                                                       saturation\_concentration: float =
                                                                       1e-05, ocean saturation state:
                                                                       float = 1.0, gas\_diffusivity: float =
                                                                       0, tolera-
                                                                       ble_super_saturation_fraction:
                                                                       float = 1)
     Bases: object
     gas_density: float = 1
     gas_diffusivity: float = 0
     ocean_saturation_state: float = 1.0
     saturation_concentration: float = 1e-05
     tolerable_super_saturation_fraction: float = 1
```

### celestine.params.dimensional.initial conditions module

values for bottom (ocean) boundary

```
class celestine.params.dimensional.initial_conditions.BRW09InitialConditions(Barrow_initial_bulk_gas_in_ice:
                                                                                float = 0.2)
    Bases: object
    values for bottom (ocean) boundary
    Barrow_initial_bulk_gas_in_ice: float = 0.2
class celestine.params.dimensional.initial_conditions.DimensionalOilInitialConditions(initial_ice_depth:
    Bases: object
    initial_ice_bulk_salinity: float = 5.92
    initial_ice_depth: float = 1
    initial_ice_temperature: float = -4
    initial_ocean_temperature: float = -2
    initial_oil_volume_fraction: float = 1e-07
class celestine.params.dimensional.initial_conditions.UniformInitialConditions
    Bases: object
```

float = 1,ini-

float

-2, ini-

float

-4, ini-

float

1e-07, ini-

float

5.92)

tial\_ocean\_temperatur

tial\_ice\_temperature:

tial\_oil\_volume\_fraction

tial\_ice\_bulk\_salinity:

### celestine.params.dimensional.numerical module

Bases: object

parameters needed for discretisation and choice of numerical method

I: int = 50

regularisation: float = 1e-06

property step

## celestine.params.dimensional.water module

class celestine.params.dimensional.water.DimensionalWaterParams(liquid\_density: float = 1028,

ocean\_salinity: float = 34, eutectic\_salinity: float = 270, eutectic\_temperature: float = -21.1, ocean\_temperature: float = -0.81, latent\_heat: float = 334000.0,

specific\_heat\_capacity: float =
4184,

 $phase\_average\_conductivity:$ 

bool = False,

liquid\_thermal\_conductivity:

float = 0.54,

solid\_thermal\_conductivity: float = 2.22, salt\_diffusivity: float = 0, liquid\_viscosity: float =

0.00278)

Bases: object

## property concentration\_ratio

Calculate concentration ratio as

$$C = S_i/\Delta S$$

## property conductivity\_ratio

Calculate the ratio of solid to liquid thermal conductivity

$$\lambda = \frac{k_s}{k_l}$$

eutectic\_salinity: float = 270

eutectic\_temperature: float = -21.1

latent\_heat: float = 334000.0

#### property lewis\_salt

Calculate the lewis number for salt, return np.inf if there is no salt diffusion.

$$Le_S = \kappa/D_s$$

liquid\_density: float = 1028

liquid\_thermal\_conductivity: float = 0.54

liquid\_viscosity: float = 0.00278

## property ocean\_freezing\_temperature

calculate salinity dependent freezing temperature using liquidus for typical ocean salinity

$$T_i = T_L(S_i) = T_E S_i / S_E$$

ocean\_salinity: float = 34

ocean\_temperature: float = -0.81

phase\_average\_conductivity: bool = False

## property salinity\_difference

calculate difference between eutectic salinity and typical ocean salinity

$$\Delta S = S_E - S_i$$

salt\_diffusivity: float = 0

solid\_thermal\_conductivity: float = 2.22

specific\_heat\_capacity: float = 4184

#### property stefan\_number

calculate Stefan number

$$St = L/c_p \Delta T$$

## property temperature\_difference

calculate

$$\Delta T = T_i - T_E$$

## property thermal\_diffusivity

Return thermal diffusivity in m2/s

$$\kappa = \frac{k}{\rho_l c_p}$$

#### **Module contents**

#### **Submodules**

### celestine.params.bubble module

```
class celestine.params.bubble.BaseBubbleParams(B: float = 100, pore_throat_scaling: float = 0.46,
                                                      porosity threshold: bool = False,
                                                      porosity\_threshold\_value: float = 0.024,
                                                      escape_ice_surface: bool = True)
     Bases: object
     Not to be used directly but provides parameters for bubble model in sea ice common to other bubble parameter
     objects.
     B: float = 100
     escape_ice_surface: bool = True
     pore_throat_scaling: float = 0.46
     porosity_threshold: bool = False
     porosity_threshold_value: float = 0.024
class celestine.params.bubble.MonoBubbleParams(B: float = 100, pore throat scaling: float = 0.46,
                                                      porosity_threshold: bool = False,
                                                      porosity\_threshold\_value: float = 0.024,
                                                      escape ice surface: bool = True,
                                                      bubble radius scaled: float = 1.0)
     Bases: BaseBubbleParams
     Parameters for population of identical spherical bubbles.
     bubble_radius_scaled: float = 1.0
class celestine.params.bubble.PowerLawBubbleParams(B: float = 100, pore_throat_scaling: float = 0.46,
                                                           porosity\_threshold: bool = False,
                                                           porosity\_threshold\_value: float = 0.024,
                                                           escape\_ice\_surface: bool = True,
                                                           bubble\_distribution\_power: float = 1.5,
                                                           minimum\_bubble\_radius\_scaled: float = 0.001,
                                                           maximum\_bubble\_radius\_scaled: float = 1)
     Bases: BaseBubbleParams
     Parameters for population of bubbles following a power law size distribution between a minimum and maximum
     bubble_distribution_power: float = 1.5
     maximum_bubble_radius_scaled: float = 1
     minimum_bubble_radius_scaled: float = 0.001
celestine.params.bubble.get_dimensionless_bubble_params(dimensional_params: DimensionalParams)
```

→ MonoBubbleParams | PowerLawBubbleParams

### celestine.params.convection module

class celestine.params.convection.RJW14Params( $Rayleigh\_salt$ : float = 44105,  $Rayleigh\_critical$ : float = 2.9,  $convection\_strength$ : float = 0.13,  $couple\_bubble\_to\_horizontal\_flow$ : bool = False,  $couple\_bubble\_to\_vertical\_flow$ : bool = False)

Bases: object

Parameters for the RJW14 parameterisation of brine convection

Rayleigh\_critical: float = 2.9

Rayleigh\_salt: float = 44105

convection\_strength: float = 0.13

couple\_bubble\_to\_horizontal\_flow: bool = False

couple\_bubble\_to\_vertical\_flow: bool = False

celestine.params.convection.get\_dimensionless\_brine\_convection\_params(dimensional\_params:

DimensionalParams) → *RJW14Params* | *NoBrineConvection* 

#### celestine.params.convert module

temperature\_difference: float, gas\_density: float,

saturation\_concentration: float)

Bases: object

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convert\_dimensional\_bulk\_air\_to\_argon\_content(dimensional\_bulk\_gas)

Convert kg/m3 of air to micromole of Argon per Liter of ice

convert\_from\_dimensional\_bulk\_gas(dimensional\_bulk\_gas)

Non dimensionalise bulk gas content in kg/m3

convert\_from\_dimensional\_bulk\_salinity(dimensional\_bulk\_salinity)

Non dimensionalise bulk salinity in g/kg

convert\_from\_dimensional\_dissolved\_gas(dimensional\_dissolved\_gas)

convert from dissolved gas in kg(gas)/kg(liquid) to dimensionless

convert\_from\_dimensional\_grid(dimensional\_grid)

Non dimensionalise domain depths in meters

convert\_from\_dimensional\_heat\_flux(dimensional\_heat\_flux)

convert from heat flux in W/m2 to dimensionless units

convert\_from\_dimensional\_heating(dimensional\_heating)

convert from heating rate in W/m3 to dimensionless units

```
convert_from_dimensional_temperature(dimensional_temperature)
          Non dimensionalise temperature in deg C
     convert_from_dimensional_time(dimensional time)
          Non dimensionalise time in days
     convert_to_dimensional_bulk_gas(bulk gas)
          Convert dimensionless bulk gas content to kg/m3
     convert_to_dimensional_bulk_salinity(bulk salinity)
          Convert non dimensional bulk salinity to g/kg
     convert_to_dimensional_dissolved_gas(dissolved_gas)
          convert from non dimensional dissolved gas to dimensional dissolved gas in kg(gas)/kg(liquid)
     convert_to_dimensional_grid(grid)
          Get domain depths in meters from non dimensional values
     convert_to_dimensional_temperature(temperature)
          get temperature in deg C from non dimensional temperature
     convert_to_dimensional_time(time)
          Convert non dimensional time into time in days since start of simulation
     gas_density: float
     lengthscale: float
     liquid_thermal_conductivity: float
     ocean_freezing_temperature: float
     ocean_salinity: float
     salinity_difference: float
     saturation_concentration: float
     temperature_difference: float
     thermal_diffusivity: float
     property time_scale
          in days
     property velocity_scale
          in m /day
celestine.params.forcing module
class celestine.params.forcing.BRW09Forcing(ocean_bulk_salinity: float = 0, ocean_gas_sat: float = 1.0,
                                                 Barrow_top_temperature_data_choice: str = 'air')
```

Surface and ocean temperature data loaded from thermistor temperature record during the Barrow 2009 field

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Bases: object

study.

```
Barrow_top_temperature_data_choice: str = 'air'
     ocean_bulk_salinity: float = 0
     ocean_gas_sat: float = 1.0
class celestine.params.forcing.BaseOceanForcing(ocean_temp: float = 0.1, ocean_bulk_salinity: float =
                                                        0, ocean\_gas\_sat: float = 1.0)
     Bases: object
     Not to be used directly but provides parameters for fixed ocean properties: gas saturation, temperature and bulk
     salinity to other forcing configuration classes
     ocean_bulk_salinity: float = 0
     ocean_gas_sat: float = 1.0
     ocean_temp: float = 0.1
class celestine.params.forcing.ConstantForcing(ocean_temp: float = 0.1, ocean_bulk_salinity: float =
                                                       0, ocean\_gas\_sat: float = 1.0,
                                                       constant\_top\_temperature: float = -1.5)
     Bases: BaseOceanForcing
     Constant temperature forcing
     constant_top_temperature: float = -1.5
class celestine.params.forcing.RadForcing(ocean\_temp: float = 0.1, ocean\_bulk\_salinity: float = 0,
                                                 ocean\_gas\_sat: float = 1.0, SW\_forcing:
                                                 DimensionalConstantSWForcing =
                                                 DimensionalConstantSWForcing(SW_irradiance=280,
                                                 SW_albedo=0.7, SW_penetration_fraction=0.4), LW_forcing:
                                                 DimensionalConstantLWForcing =
                                                 DimensionalConstantLWForcing(LW irradiance=260,
                                                 ice_emissitivty=0.99, water_emissivity=0.97), turbulent_flux:
                                                 DimensionalConstantTurbulentFlux =
                                                 DimensionalConstantTurbulentFlux(ref_height=10,
                                                 windspeed=5, air temp=0, specific humidity=0.0036,
                                                 atm pressure=101.325, air density=1.275,
                                                 air_heat_capacity=1005,
                                                 air_latent_heat_of_vaporisation=2501000.0), oil_heating:
                                                 DimensionalBackgroundOilHeating |
                                                 DimensionalMobileOilHeating | DimensionalNoHeating =
                                                 DimensionalBackgroundOilHeating(oil_mass_ratio=0,
                                                 ice_type='FYI')
     Bases: BaseOceanForcing
     Forcing parameters for radiative transfer simulation with oil drops
```

we have not implemented the non-dimensionalisation for these parameters yet and so we just pass the dimensional values directly to the simulation

```
LW_forcing: DimensionalConstantLWForcing =
DimensionalConstantLWForcing(LW_irradiance=260, ice_emissitivty=0.99,
water_emissivity=0.97)
```

```
SW_forcing: DimensionalConstantSWForcing =
     DimensionalConstantSWForcing(SW_irradiance=280, SW_albedo=0.7,
     SW_penetration_fraction=0.4)
     oil_heating: DimensionalBackgroundOilHeating | DimensionalMobileOilHeating |
     DimensionalNoHeating = DimensionalBackgroundOilHeating(oil_mass_ratio=0,
     ice_type='FYI')
     turbulent_flux: DimensionalConstantTurbulentFlux =
     DimensionalConstantTurbulentFlux(ref_height=10, windspeed=5, air_temp=0,
     specific_humidity=0.0036, atm_pressure=101.325, air_density=1.275,
     air_heat_capacity=1005, air_latent_heat_of_vaporisation=2501000.0)
class celestine.params.forcing.YearlyForcing(ocean_temp: float = 0.1, ocean_bulk_salinity: float = 0,
                                                 ocean\_gas\_sat: float = 1.0, offset: float = -1.0, amplitude:
                                                 float = 0.75, period: float = 4.0)
     Bases: BaseOceanForcing
     Yearly sinusoidal temperature forcing
     amplitude: float = 0.75
     offset: float = -1.0
     period: float = 4.0
celestine.params.forcing.get_dimensionless_forcing_config(dimensional params:
                                                               Dimensional Params) \rightarrow
                                                               ConstantForcing | YearlyForcing |
                                                               BRW09Forcing | RadForcing
celestine.params.initial_conditions module
class celestine.params.initial_conditions.0ilInitialConditions(initial_ice_depth: float = 0.5,
                                                                     initial_ocean_temperature: float
                                                                     = -0.05, initial ice temperature:
                                                                    float = -0.1,
                                                                     initial oil volume fraction: float
                                                                     = 1e-07, initial_ice_bulk_salinity:
                                                                    float = -0.1)
     Bases: object
     values for bottom (ocean) boundary
     initial_ice_bulk_salinity: float = -0.1
     initial_ice_depth: float = 0.5
     initial_ice_temperature: float = -0.1
     initial_ocean_temperature: float = -0.05
     initial_oil_volume_fraction: float = 1e-07
```

 $celestine.params.initial\_conditions. {\tt get\_dimensionless\_initial\_conditions\_config} ({\it dimensional\_params}: {\tt celestine.params}) and {\tt celestine.params} ({\tt celestine.p$ 

DimensionalParams)

→ UniformInitialConditions |
BRW09InitialConditions
| OilInitial-

**Conditions** 

### celestine.params.params module

Classes containing parameters required to run a simulation

The config class contains all the parameters needed to run a simulation as well as methods to save and load this configuration to a yaml file.

**class** celestine.params.params.**Config**(name: str, total\_time: float, savefreq: float, physical\_params:

EQMPhysicalParams | DISEQPhysicalParams, bubble\_params:

MonoBubbleParams | PowerLawBubbleParams,

brine\_convection\_params: RJW14Params | NoBrineConvection, forcing\_config: ConstantForcing | YearlyForcing | BRW09Forcing | RadForcing, initial\_conditions\_config: UniformInitialConditions | BRW09InitialConditions | OilInitialConditions, numerical\_params:

NumericalParams = NumericalParams(I=50,

regularisation=1e-06), scales: Scales | None = None)

Bases: object

total\_time: float

contains all information needed to run a simulation and save output

this config object can be saved and loaded to a yaml file.

```
brine_convection_params: RJW14Params | NoBrineConvection

bubble_params: MonoBubbleParams | PowerLawBubbleParams

forcing_config: ConstantForcing | YearlyForcing | BRW09Forcing | RadForcing

initial_conditions_config: UniformInitialConditions | BRW09InitialConditions |
OilInitialConditions

classmethod load(path)

name: str

numerical_params: NumericalParams = NumericalParams(I=50, regularisation=1e-06)

physical_params: EQMPhysicalParams | DISEQPhysicalParams

save(directory: Path)

savefreq: float

scales: Scales | None = None
```

```
celestine.params.get_config(dimensional\_params: DimensionalParams) \rightarrow Config Return a Config object for the simulation.
```

physical parameters and Darcy law parameters are calculated from the dimensional input. You can modify the numerical parameters and boundary conditions and forcing provided for the simulation.

#### celestine.params.physical module

```
class celestine.params.physical.BasePhysicalParams(expansion_coefficient: float = 0.029,
                                                             concentration\_ratio: float = 0.17, stefan\_number:
                                                             float = 4.2, lewis\_salt: float = inf, lewis\_gas:
                                                             float = inf, frame\_velocity: float = 0,
                                                             phase\_average\_conductivity: bool = False,
                                                             conductivity\_ratio: float = 4.11,
                                                             tolerable\_super\_saturation\_fraction: float = 1)
     Bases: object
     Not to be used directly but provides the common parameters for physical params objects
     concentration_ratio: float = 0.17
     conductivity_ratio: float = 4.11
     expansion_coefficient: float = 0.029
     frame_velocity: float = 0
     lewis_gas: float = inf
     lewis_salt: float = inf
     phase_average_conductivity: bool = False
     stefan_number: float = 4.2
     tolerable_super_saturation_fraction: float = 1
class celestine.params.physical.DISEQPhysicalParams(expansion_coefficient: float = 0.029,
                                                              concentration\_ratio: float = 0.17,
                                                              stefan_number: float = 4.2, lewis_salt: float =
                                                              inf, lewis_gas: float = inf, frame_velocity: float
                                                              = 0, phase\_average\_conductivity: bool = False,
                                                              conductivity\_ratio: float = 4.11,
                                                              tolerable\_super\_saturation\_fraction: float = 1,
                                                              damkohler number: float = 1)
     Bases: BasePhysicalParams
     non dimensional numbers for the mushy layer
     damkohler_number: float = 1
class celestine.params.physical.EQMPhysicalParams(expansion coefficient: float = 0.029,
                                                            concentration\_ratio: float = 0.17, stefan\_number:
                                                            float = 4.2, lewis\_salt: float = inf, lewis\_gas: float
                                                            = inf, frame\_velocity: float = 0,
                                                            phase average conductivity: bool = False,
                                                            conductivity ratio: float = 4.11,
                                                            tolerable\_super\_saturation\_fraction: float = 1)
```

```
Bases: BasePhysicalParams
```

non dimensional numbers for the mushy layer

celestine.params.physical.get\_dimensionless\_physical\_params(dimensional\_params:

Dimensional Params)  $\rightarrow$ EOMPhysicalParams | DISEQPhysicalParams

return a PhysicalParams object

#### **Module contents**

## celestine.state package

#### **Submodules**

#### celestine.state.disequilibrium state module

```
class celestine.state.disequilibrium_state.DISEQState(time: float, enthalpy: ndarray[Any,
                                                                dtype[_ScalarType_co]], salt: ndarray[Any,
                                                                dtype[_ScalarType_co]], bulk_dissolved_gas:
                                                                ndarray[Any, dtype[_ScalarType_co]],
                                                                gas_fraction: ndarray[Any,
                                                                dtype[_ScalarType_co]])
```

Bases: object

Contains the principal variables for solution with non-equilibrium gas phase. The total bulk gas is partitioned between dissolved gas and free phase gas with a finite nucleation rate (non dimensional damkohler number).

principal solution components: bulk enthalpy bulk salinity bulk dissolved gas gas fraction

all on the center grid.

```
Note: Define bulk dissolved gas for the system as
expansion_coefficient * liquid_fraction * dissolved_gas
so that this is different from the dissolved gas concentration and
bulk_gas = bulk_dissolved_gas + gas_fraction
in non-dimensional units.
bulk_dissolved_gas: ndarray[Any, dtype[_ScalarType_co]]
```

enthalpy: ndarray[Any, dtype[\_ScalarType\_co]]

property gas: ndarray[Any, dtype[\_ScalarType\_co]]

Calculate bulk gas content and use same attribute name as EQMState

gas\_fraction: ndarray[Any, dtype[\_ScalarType\_co]]

salt: ndarray[Any, dtype[\_ScalarType\_co]]

time: float

```
class celestine.state.disequilibrium_state.DISEQStateBCs(time: float, enthalpy: ndarray[Any,
                                                                dtype[_ScalarType_co]], salt:
                                                                ndarray[Any, dtype[ ScalarType co]],
                                                                temperature: ndarray[Any,
                                                                dtype[_ScalarType_co]], liquid_salinity:
                                                                ndarray[Any, dtype[_ScalarType_co]],
                                                                dissolved gas: ndarray[Any,
                                                                dtype[_ScalarType_co]], liquid_fraction:
                                                                ndarray[Any, dtype[_ScalarType_co]],
                                                                bulk_dissolved_gas: ndarray[Any,
                                                                dtype[_ScalarType_co]], gas_fraction:
                                                                ndarray[Any, dtype[_ScalarType_co]])
     Bases: object
     Stores information needed for solution at one timestep with BCs on ghost cells as well
     Initialiase the prime variables for the solver: enthalpy, bulk salinity and bulk air
     bulk_dissolved_gas: ndarray[Any, dtype[_ScalarType_co]]
     dissolved_gas: ndarray[Any, dtype[_ScalarType_co]]
     enthalpy: ndarray[Any, dtype[_ScalarType_co]]
     gas_fraction: ndarray[Any, dtype[_ScalarType_co]]
     liquid_fraction: ndarray[Any, dtype[_ScalarType_co]]
     liquid_salinity: ndarray[Any, dtype[_ScalarType_co]]
     salt: ndarray[Any, dtype[_ScalarType_co]]
     temperature: ndarray[Any, dtype[_ScalarType_co]]
     time:
             float
```

 $\textbf{class} \ \ \textbf{celestine.state.disequilibrium\_state.} \textbf{DISEQStateFull} (\textit{time: float, enthalpy: ndarray} [\textit{Any, enthalpy: ndarray}] (\textit{time: float, enthalpy: ndarray}) (\textit{time: float, enthalpy: float, enth$ 

dtype[\_ScalarType\_co]], salt:
ndarray[Any, dtype[\_ScalarType\_co]],
bulk\_dissolved\_gas: ndarray[Any,
dtype[\_ScalarType\_co]], gas\_fraction:
ndarray[Any, dtype[\_ScalarType\_co]],
temperature: ndarray[Any,
dtype[\_ScalarType\_co]],
liquid\_fraction: ndarray[Any,
dtype[\_ScalarType\_co]], solid\_fraction:
ndarray[Any, dtype[\_ScalarType\_co]],
liquid\_salinity: ndarray[Any,
dtype[\_ScalarType\_co]], dissolved\_gas:
ndarray[Any, dtype[\_ScalarType\_co]])

Bases: object

Contains all variables variables for solution with non-equilibrium gas phase after running the enthalpy method on DISEQSate. The total bulk gas is partitioned between dissolved gas and free phase gas with a finite nucleation rate (non dimensional damkohler number).

principal solution components: bulk enthalpy bulk salinity bulk dissolved gas gas fraction enthalpy method variables: temperature liquid\_fraction solid\_fraction liquid\_salinity dissolved\_gas

```
all on the center grid.
     Note: Define bulk dissolved gas for the system as
     expansion_coefficient * liquid_fraction * dissolved_gas
     so that this is different from the dissolved gas concentration and
     bulk gas = bulk dissolved gas + gas fraction
     in non-dimensional units.
     bulk_dissolved_gas: ndarray[Any, dtype[_ScalarType_co]]
     dissolved_gas: ndarray[Any, dtype[_ScalarType_co]]
     enthalpy: ndarray[Any, dtype[_ScalarType_co]]
     property gas: ndarray[Any, dtype[_ScalarType_co]]
          Calculate bulk gas content and use same attribute name as EQMState
     gas_fraction: ndarray[Any, dtype[_ScalarType_co]]
     liquid_fraction: ndarray[Any, dtype[_ScalarType_co]]
     liquid_salinity: ndarray[Any, dtype[_ScalarType_co]]
     salt: ndarray[Any, dtype[_ScalarType_co]]
     solid_fraction: ndarray[Any, dtype[_ScalarType_co]]
     temperature: ndarray[Any, dtype[_ScalarType_co]]
     time: float
celestine.state.equilibrium_state module
class celestine.state.equilibrium_state.EQMState(time: float, enthalpy: ndarray[Any,
                                                      dtype[_ScalarType_co]], salt: ndarray[Any,
                                                      dtype[_ScalarType_co]], gas: ndarray[Any,
                                                      dtype[_ScalarType_co]])
     Bases: object
     Contains the principal variables for solution with equilibrium gas phase:
     bulk enthalpy bulk salinity bulk gas
     all on the center grid.
     enthalpy: ndarray[Any, dtype[_ScalarType_co]]
     gas: ndarray[Any, dtype[_ScalarType_co]]
     salt: ndarray[Any, dtype[_ScalarType_co]]
     time:
            float
```

```
class celestine.state.equilibrium_state.EQMStateBCs(time: float, enthalpy: ndarray[Any,
                                                             dtype[_ScalarType_co]], salt: ndarray[Any,
                                                             dtype[ ScalarType co]], gas: ndarray[Any,
                                                             dtype[_ScalarType_co]], temperature:
                                                             ndarray[Any, dtype[_ScalarType_co]],
                                                             liquid salinity: ndarray[Any,
                                                             dtype[ ScalarType co]], dissolved gas:
                                                             ndarray[Any, dtype[_ScalarType_co]],
                                                             gas fraction: ndarray[Any,
                                                             dtype[_ScalarType_co]], liquid_fraction:
                                                             ndarray[Any, dtype[_ScalarType_co]])
     Bases: object
     Stores information needed for solution at one timestep with BCs on ghost cells as well
     Initialiase the prime variables for the solver: enthalpy, bulk salinity and bulk air
     dissolved_gas: ndarray[Any, dtype[_ScalarType_co]]
     enthalpy: ndarray[Any, dtype[_ScalarType_co]]
     gas: ndarray[Any, dtype[_ScalarType_co]]
     gas_fraction: ndarray[Any, dtype[_ScalarType_co]]
     liquid_fraction: ndarray[Any, dtype[_ScalarType_co]]
     liquid_salinity: ndarray[Any, dtype[_ScalarType_co]]
     salt: ndarray[Any, dtype[_ScalarType_co]]
     temperature: ndarray[Any, dtype[_ScalarType_co]]
     time:
             float
class celestine.state.equilibrium_state.EQMStateFull(time: float, enthalpy: ndarray[Any,
                                                              dtype[_ScalarType_co]], salt: ndarray[Any,
                                                              dtype[_ScalarType_co]], gas: ndarray[Any,
                                                              dtype[_ScalarType_co]], temperature:
                                                              ndarray[Any, dtype[_ScalarType_co]],
                                                              liquid_fraction: ndarray[Any,
                                                              dtype[_ScalarType_co]], solid_fraction:
                                                              ndarray[Any, dtype[_ScalarType_co]],
                                                              liquid_salinity: ndarray[Any,
                                                              dtype[_ScalarType_co]], dissolved_gas:
                                                              ndarray[Any, dtype[_ScalarType_co]],
                                                              gas_fraction: ndarray[Any,
                                                              dtype[_ScalarType_co]])
     Bases: object
     Contains all variables variables for solution with equilibrium gas phase after running the enthalpy method on
     EQMSate.
     principal solution components: bulk enthalpy bulk salinity bulk gas
     enthalpy method variables: temperature liquid_fraction solid_fraction liquid_salinity dissolved_gas gas_fraction
     all on the center grid.
```

```
dissolved_gas: ndarray[Any, dtype[_ScalarType_co]]
enthalpy: ndarray[Any, dtype[_ScalarType_co]]
gas: ndarray[Any, dtype[_ScalarType_co]]
gas_fraction: ndarray[Any, dtype[_ScalarType_co]]
liquid_fraction: ndarray[Any, dtype[_ScalarType_co]]
liquid_salinity: ndarray[Any, dtype[_ScalarType_co]]
salt: ndarray[Any, dtype[_ScalarType_co]]
solid_fraction: ndarray[Any, dtype[_ScalarType_co]]
temperature: ndarray[Any, dtype[_ScalarType_co]]
time: float
```

#### **Module contents**

celestine.state.get\_unpacker(cfg: Config)  $\rightarrow$  Callable[[float, ndarray[Any, dtype[\_ScalarType\_co]]],  $EQMState \mid DISEQState$ ]

## 1.1.2 Submodules

## 1.1.3 celestine.example module

Script to run a simulation starting with dimensional parameters and plot output

 $\label{lem:create_and_save_config} (\textit{data\_directory: Path, simulation\_dimensional\_params: } \\ \text{DimensionalParams)}$ 

celestine.example.main(data\_directory: Path, frames\_directory: Path, simulation\_dimensional\_params: DimensionalParams)

Generate non dimensional simulation config and save along with dimensional config then run simulation and save data.

## 1.1.4 celestine.grids module

Module providing functions to initialise the different grids and interpolate quantities between them.

```
class celestine.grids.Grids(number_of_cells: int)
```

Bases: object

Class initialised from number of grid cells to contain:

grid cell width, center, edge and ghost grids and difference matrices

property D\_e: ndarray[Any, dtype[\_ScalarType\_co]]

Difference matrix to differentiate edge grid quantities to the center grid

property D\_g: ndarray[Any, dtype[\_ScalarType\_co]]

Difference matrix to differentiate ghost grid quantities to the edge grid

```
property centers: ndarray[Any, dtype[_ScalarType_co]]
    Center grid

property edges: ndarray[Any, dtype[_ScalarType_co]]
    Edge grid

property ghosts: ndarray[Any, dtype[_ScalarType_co]]
    Ghost grid

number_of_cells: int

property step: float
    Grid cell width
```

celestine.grids.add\_ghost\_cells(centers, bottom, top)

Add specified bottom and top value to center grid

#### **Parameters**

- **centers** (*Numpy array*) numpy array on centered grid (size I).
- **bottom** (*float*) bottom value placed at index 0.
- **top** (*float*) top value placed at index -1.

#### Returns

numpy array on ghost grid (size I+2).

### celestine.grids.calculate\_ice\_ocean\_boundary\_depth(liquid\_fraction, edge\_grid)

Calculate the depth of the ice ocean boundary as the edge position of the first cell from the bottom to be not completely liquid. I.e the first time the liquid fraction goes below 1.

If the ice has made it to the bottom of the domain raise an error.

If the domain is completely liquid set h=0.

NOTE: depth is a positive quantity and our grid coordinate increases from -1 at the bottom of the domain to 0 at the top.

#### **Parameters**

- liquid\_fraction (Numpy Array (size I)) liquid fraction on center grid
- edge\_grid (Numpy Array (size I+1)) The vertical coordinate positions of the edge grid.

#### Returns

positive depth value of ice ocean interface

```
celestine.grids.geometric(ghosts)
```

Returns geometric mean of the first dimension of an array

```
celestine.grids.get_difference_matrix(size, step)
```

celestine.grids.upwind(ghosts, velocity)

## 1.1.5 celestine.initial conditions module

Module to provide initial state of bulk enthalpy, bulk salinity and bulk gas for the simulation. celestine.initial\_conditions.get\_initial\_conditions(cfg: Config)

#### 1.1.6 celestine.load module

## 1.1.7 celestine.oil\_simulation module

```
celestine.oil_simulation.generate_oil_simulation_config(name: str, total_time_in_days: float, lengthscale: float, initial_oil_mass_ratio: float, oil_density: float, oil_droplet_radius: float, SW_irradiance: float, SW_albedo: float, SW_penetration_fraction: float, LW_irradiance: float, air_temp: float, windspeed: float, ref_height: float, oil_heating_params:

DimensionalBackgroundOilHeating |
```

DimensionalNoHeating, initial\_ice\_depth: float, initial\_ice\_temperature: float, initial\_ocean\_temperature: float, initial\_ice\_bulk\_salinity: float = 34,

brine\_convection\_params:
DimensionalRJW14Params |

Dimensional Mobile Oil Heating

NoBrineConvection = Dimensional-

RJW14Params(couple\_bubble\_to\_horizontal\_flow=False, couple\_bubble\_to\_vertical\_flow=False,

Rayleigh\_critical=2.9,

convection\_strength=0.13,

 $ha line\_contraction\_coefficient = 0.00075,$ 

 $reference\_permeability{=}1e\text{-}08), I{=}50,$ 

 $savefreq\_in\_days=1.0,$ 

 $config\_directory = PosixPath('.')) \rightarrow None$ 

Parameters to generate a simulation config for melting of an initially uniform layer of ice in an ocean under SW, LW radiative fluxes and sensible heat flux.

The latent heat flux is disabled by setting the latent heat of vaporisation to 0.

The initially uniform mass concentration of oil in the domain is set in ng/g.

## 1.1.8 celestine.printing module

celestine.printing.get\_printer(verbosity\_level: int) → Callable[[str], None]

## 1.1.9 celestine.run\_simulation module

Module to run the simulation on the given configuration with the appropriate solver.

Solve reduced model using scipy solve\_ivp using RK23 solver.

Impose a maximum timestep constraint using courant number for thermal diffusion as this is an explicit method.

This solver uses adaptive timestepping which makes it a good choice for running simulations with large buoyancy driven gas bubble velocities and we save the output at intervals given by the savefreq parameter in configuration.

celestine.run\_simulation.run\_batch( $list\_of\_cfg: List[Config], directory: Path, verbosity\_level=0) \rightarrow None Run a batch of simulations from a list of configurations.$ 

Each simulation name is logged, as well as if it successfully runs or crashes. Output from each simulation is saved in a .npz file.

#### **Parameters**

**list\_of\_cfg** (List[celestine.params.Config]) – list of configurations

celestine.run\_simulation.solve(cfg: Config, directory: Path,  $verbosity\_level=0$ )  $\rightarrow$  Literal[0]

#### 1.1.10 Module contents

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