

Modelling Low Earth Orbit Constellations for Networking

Joseph McGuchan

May 6, 2019

I, Joseph Law McGuchan of King's College, being a candidate for Part II of the Computer Science Tripos, hereby declare that this dissertation and the work described in it are my own work, unaided except as may be specified below, and that the dissertation does not contain material that has already been used to any substantial extent for a comparable purpose.

Signed

Date

Modelling Low Earth Orbit Constellations for Networking

Contents

1	Introduction	5
1.1	What is Starlink?	5
1.2	Why Focus on Starlink?	6
1.3	Why Create a Visualisation?	7
1.4	Mark Handley's Work	7
1.5	What I Will Be Using	7
2	Preparation	7
2.1	Starting Point	7
2.2	The Properties of Orbits	8
2.3	The Structure of Starlink	8
2.4	Modelling Sattelites in Orbit	9
2.5	Variables	10
3	Implementation	12
3.1	Repository Overview	12
3.2	Difficulties of Modeling Orbits	12
3.3	Representing Links	13
3.4	Patterns used	14
3.5	Initial Observations of Network	14
3.6	Visualization	15
3.7	The Motion of the Player	15
3.8	Inputs	15
3.9	Describing Linking Methods	18
3.10	Finding the Nearest Satellite	18
3.11	Tests	20
3.12	Dijkstra's Algorithm	20
3.13	Calculating the Latency Across a Path	21
3.14	Coding for Visualisation and Efficent Algorithms	21
4	Evaluation	21
4.1	Analysis of Variables	21
4.2	Using the Program	21
4.3	Test 0: Observing the constellation	22
4.4	Test 1: Highlighting Northbound and Southbound Satellites	22
4.5	Test 2: Following a Satellite	22

4.6	Test 3: Total Connectivity As Satellites Are Removed	23
4.7	Test 4: Total Connectivity with Alternate Linking Method . . .	25
4.8	Test 5: Total Connectivity Localised	25
4.9	Test 6: Shortest Path London to New York	26
4.10	Test 7-: Shortest Path London to New York	26
4.11	Godot as a Simulation Environment	26
4.12	Direction and Focus	27
5	Conclusion	28
A	Appendix A	29

1 Introduction

SpaceX are planning to launch a constellation of 4,425 low Earth orbit communication satellites in the next few years. The objective of this constellation, called Starlink, is to provide low-latency internet connection across the world.

The satellites in this network will be in constant motion, not just relative to the ground, but relative to one another, creating a network with a constantly changing topology and associated latencies. The question of how to structure such a network, and what the resultant latencies of said network will be, has not been thoroughly explored, but it will become increasingly relevant as more and more companies build similar constellations. If these Constellations prove to provide significant gains in latency while providing competitive bandwidth, they might render previous submarine optical cables obsolete.

My goals are:

1. To create visualizations of the SpaceX constellation.
2. To experiment with different topologies of the SpaceX network and test their associated latencies.

1.1 What is Starlink?

The purpose of Starlink is to provide low latency internet connections, as of 21/11/18, there are two companies offering satellite internet services,

Excede[?], and Hughes, whose 9202 BGAN Land Portable Satellite Terminal offers connection speeds up to 464kbps[2]. These companies largely target domestic use in rural areas which don't have a faster coverage, and corporations, providing internet connections to airplanes and cargo ships. Currently, Satellite Internet connection is a last resort, something turned to when conventional means of connection are not available, Starlink intends to invert this, turning satellite internet into the premium option.

The difference between Starlink and currently existing brands is that current brands use geostationary satellites [9], while Starlink will use LEO satellites. The significantly shorter distance will create much shorter paths for signals. On top of this, SpaceX will be utilizing laser communication between satellites, as opposed to the competitors who have little to no intra-satellite communication. In the vacuum of space, lights travels 47% faster than in glass [8]. Therefore, in theory, a LEO network utilising lasers would achieve latencies far lower than that by even the best terrestrial fiber optic connections over long distances.

1.2 Why Focus on Starlink?

Starlink is only one of a number of different LEO internet networks that have been proposed, so why should I focus on it's topology? Ideally, I would like the conclusions of my study to be generalized to many other LEO constellations. However, constellations are approved by the FCC on a case-by-case basis, using a complicated and changing system of legislations, it's not easy to know what a normal network looks like. By analyzing the properties of a network of my own design, I run a much greater risk of coming to conclusions that cannot be generalized, as I am not working on an FCC-approved constellation.

What about the constellations of other companies?

By analyzing the properties of Starlink, we are analysing a network that is confirmed legally and scientifically plausible.

But there is another reason to investigate Starlink. As the largest of most high-profile attempts to build a LEO internet backbone, Starlink represents the most significant competitor to other emerging satellite communications networks and the one more likely to become dominant in future years. By theorising about it's properties now, we can prepare ourselves for the changes Starlink might pose to communications in the upcoming years.

1.3 Why Create a Visualisation?

When it comes to understanding a network such as starlink, a visual description is incredibly valuable. By visualising the network we can develop an intuition for how it operates, and use that intuition to develop ideas for new algorithms and structures for testing.

Creating a visualization also poses a minimal additional cost on my part, as to accurately model the latencies between base stations I will need to simulate satellite positions and links anyway.

1.4 Mark Handley's Work

My initial proposal for the project was inspired by the findings of an existing study done by Mark Handley, since proposing the project, Mark Handley has made his results publicly available[6], so my new goal will be to replicate and expand upon his findings.

1.5 What I Will Be Using

To create the visualisation I will be using the open-source game engine Godot. Using a game engine struck me as the simplest way to create a visualisation tool, and Godot, being powerful, open-source, and capable of running easily on many devices, seemed like the ideal choice.

For the parts of code related to visualization I will be using godots build in script GDScript, which is easy to use and specifically designed to intergrate well with the godot engine. For parts of the code related to simulation I will use C#, which godot is compatable with, and which offers significance performance improvements over gdscript.

2 Preparation

2.1 Starting Point

Most of the information I will be using for the structure of the SpaceX network comes from their application to the FCC on March 29th, 2018[4], and their technical attachment[5], which outlines the various orbital spheres, planes within each sphere, and various other details of the constellation. I will also be building on insights gleaned from Handley's original research.

Figure 1: The layout of Starlink

SPACEX SYSTEM CONSTELLATION					
Parameter	Initial Deployment (1,600 satellites)	Final Deployment (2,825 satellites)			
Orbital Planes	32	32	8	5	6
Sattelites per Plane	50	50	50	75	75
Altitude	1150km	1110km	1130km	1275km	1325km
Inclination	53°	53.8°	74°	80°	70°

SpaceX have already sent up two test sattelites, and according the Elon Musk, they are working very well, providing a latency of only 25ms[3].

2.2 The Properties of Orbits

2.3 The Structure of Starlink

There is a lot we do not know about Starlink, but this is what we can infer from SpaceX’s application to the FCC[4],

Starlink is a constellation of 4,425 LEO sattelites with a further proposed.

We will be examining only the 4,425 sattelites proposed for the first implemantation of Starlink, as these intend to provide a viable network by temselves, and additional sattelites might overwhelm my visualisation techniques.

In it’s application to the FCC SpaceX was required to state any notable debris that might not burn up if a sattelite were to descend from orbit. Among the components listed where 5 silicon carbide “communication components”, silicon carbide is used in mirrors for laser communication links, and we can therefore conclude that SpaceX’s sattelites will have, at most, 5 available links to form with nearby sattelites.

We also know information about how Starlink sattelites will communicate with ground stations, a base station may only connect with a sattelite at an inclination less than 40°from the vertical using Radio Frequency (not laser) connections. Connections will be stronger to sattelites directly overhead, however as Starlink does not provide much information in exactly how their intra-sattelite communications work, speculations on bandwidth will

not prove to be helpful.

2.4 Modelling Sattelites in Orbit

Typically, an orbit around the surface of the earth is described by:

Distance Above the Surface

Inclination This is the angle between the orbital plane, and the equatorial plane, (the plane on which the equator lies).

Longditudonal Offset If inclination is greater than 0° , then the orbital plane and equatorial plane will intersect at a line, the angle between this line and the plane described by the great circle at longditute 0° is the longditudonal offset. In other words, the Longditudonal offset is the Londitudute of the point where this line passes through the surface of the earth.

Eccentricity The eccentricity coefficient describes the “squashness” of the orbit. For the time being, we will be ignoring this...

Retrograde A retrograde orbit is one that goes against the rotation of the earth, typically these are described by orbits with a longditudonal offset greater than 180° . It is significantly more expensive to put a sattelite into a retrograde orbit, and is essentially never done.

Furthermore, an individual satellite’s position in an orbit can be described by:

True Anomaly The angle between the line drawn from the origin to the satellite, and the line drawn from the origin to the point on the satellite’s orbit of longditude 0.

Phase Offset This is the satellite’s true anomaly at time 0.

In our model, true anomaly is the only variable that changes. The way it changes is uniquely determined by the other 6 variables. The rate of change of true anomaly, the angular velocity, is given by

$$\sqrt{\frac{GM}{r^3}}$$

Where r is the distance from the origin, or altitude + radius of the Earth.

Note that while altitude is constant (eccentricity = 0) velocity is unchanging, and true anomaly can be described as a linear function of time.

The position of a satellite is calculated by taking it's true anomaly and adding it's angular velocity multiplied by the timestep (real timesince last frame update * some factor). The location is then calculated through a series of transformations performed on the true anomaly:

1. We take a vector $(r, 0, 0)$ where r is the distance above the surface + the radius of Earth.
2. We rotate this point around $(0, 1, 0)$ (the line through the poles) by the true anomaly.
3. We rotate this point around $(1, 0, 0)$ (the line from 0 longitude to 180 longitude through the equator) by the inclination.
4. We rotate this point around $(0, 1, 0)$ again by the longitudinal offset.

Because the only variable that is changed is the true anomaly, and the x , y , and z coordinates are determined by only this variable and a series of fixed variables, we do not run the same risks normal discrete physics models face when describing continuous behaviour, such as unpredictable behaviour when sped up, at extreme forces, or the steady moving of orbits.

For the rest of this document, a satellite will be denoted by $x_{i,j,k}$. Where i denotes the orbital sphere, s_i , and j denotes the orbital plane $o_{i,j}$. n_i will be used to denote the number of satellites per plane of orbital sphere s_i (50 or 75).

2.5 Variables

While we can learn a lot from SpaceX's applications, there are still a number of variables that are left undetermined.

Distribution on Orbit SpaceX only specifies which orbital planes it requires, and how many satellites will be on each plane, it does not specify where satellites will be positioned on those planes. This leads us to speculate as to how satellites will be distributed. I will describe the distribution of $o_{i,j}$ by the normalised n_i -dimensional vector d_i , where

$(2\pi d_i)_k$ gives the arc between $x_{i,j,k}$ and $x_{i,j,k+1}$. For simplicitys sake, I will use non-normalised vectors as shorthand for normalised vectors, and vectors that are too short as shorthand for repeatind patterns. For instance:

$$d_i = [1]$$

Is shorthand for:

$$d_i = \frac{1}{n_i}[1, 1, \dots, 1]$$

And:

$$d_i = [1, 3]$$

Is shorthand for:

$$d_i = \frac{1}{n_i}[0.5, 1.5, 0.5, 1.5, \dots]$$

Phase Offset As we do not know for certain how satellites will be positioned in orbits, we also do not know how they will be positioned relative to other orbits. The phase offset of an obit $o_{i,j}$, $po_{i,j}$, can be described as a number from 0 to 1, where, $\forall k$, 0 indicates that $x_{i,j,k}$ will cross the equator at the same time as $x_{i,j+1,k}$, and 1 indicates that satellite $x_{i,j,k}$ will cross the equator at the same time as $x_{i,j+1,k+1}$. This number will have to be some fraction of the total number of orbits, to garuntee that the first and last orbits are properly aligned.

Each of the orbital spheres can also be offset from each other. The phase offset of spheres will be described very differently: ps_i will be a 2D vector that decribes the longitude and latitude of $x_{i,0,0}$ when $x_{0,0,0}$ crosses the equator.

Link usage Each satellite will have a maximum of 5 links, however, we do not as of yet know which arrangements of links are the most optimal.

In his study Mark Handley uses two links to connect $x_{i,j,k}$ to $x_{i,j,k+1}$ and $x_{i,j,k-1}$. He then uses two more to connect $x_{i,j,k}$ to $x_{i,j+1,k+h_i}$ and

$x_{i,j-1,k-h_i}$, where h_i is a variable that describes how "diagonal" these sideways links should be. The final link connects to the nearest unconnected satellite. However there a number of different ways to connect up the satellites, for a given sphere s_i I will catagorise the different link usage methods as.

(h) Mark Handley's method where $h_i = h$.

OneFree(X) A generalisation of Handley, described by a 2*2 matrix X. Where $x_{i,j,k}$ connects to $x_{i,j+X_{0,0},k+X_{0,1}}$, $x_{i,j+X_{1,0},k+X_{1,1}}$ and visa-versa.

ThreeFreeBasic In which $x_{i,j,k}$ connects to $x_{i,j,k+1}$ and $x_{i,j,k-1}$, and the other three links connect to nearby satellites.

ThreeFree(v) A generalisation of ThreeFree, described by a 2d vector v, in which $x_{i,j,k}$ connects to $x_{i,j+v_0,k+v_1}$ and visa versa.

FiveFree In which all 5 links are free links, connecting dynamically to the closest nodes.

Response to Congestion Very little is known about how much load Starlink expects to receive or how it will respond to congestion. We know that Starlink will be quite a resilient network, with a great number of alternative parths available with similar latencies, so systems that predict hotspots on the network and route to avoid them might prove quite effective. However the exact benefit of these systems is yet to be examined.

3 Implementation

3.1 Repository Overview

3.2 Difficulties of Modeling Orbits

On Implementation, I found that my planned method of implimenting orbits was flawed, being able to simulate only 500 sattelites in motion before slowing down. Because of this, I changed to a precomputed method. In this method, orbits are precomputed as a number of points, and the position of sattelites is calculated by interpolating adgacent points, this sacrifices some accuracy, but vastly increases the computation speed.

3.3 Representing Links

There are 3 primary ways to represent a graph for algorithms:

Adjacency Matrix An NxN matrix of values representing all possible connections. Obviously inefficient for a sparse set of connections like this.

Adjacency List Associate each Satellite with a list of the vertices it is connected to. Space efficient, but creates difficulty in running dijkstra's algorithm.

Edge List Create a list of edges that refer to vertices. This is useful for algorithms that require iterating through all edges like dijkstra's algorithm. But to find the adjacent satellites to any given satellite requires searching through the whole list.

Furthermore, to draw a link, Godot demands that it be a "child" (not in the class inheritance sense) of one node in the scene. And I also want the ability to describe new linking methods, and have different spheres use different linking methods.

My solution was to use the method pattern. I would have an abstract class called "LinkingMethod" that implemented many different options for linking, and had three abstract methods. Initialise, which runs on a constellation of satellites and creates the links, UpdateOrbit, which is ran every step by every orbit (to exploit multithreading) and updates the associated links, and UpdateConstellation which is ran every step for the whole constellation.

Initially, I used adjacency lists, this led to a number of problems.

- Some algorithms require a list of all edges, which is very hard to obtain with adjacency lists.
- When drawing edges in the visualisation, each would be drawn twice, for each vertex they were associated with.
- When updating links, values such as the distance between two vertices had to be computed twice for each vertex.

Instead I created a new class of objects representing links, and gave each vertex a reference to the links associated with it.

In Godot, all drawn objects require a "child" (different to class inheritance) which is drawn with it. Children inherit the position and rotation of

their parents, and rotating a group of objects is significantly more efficient than rotating a single object alone. Because of this, backwards and forward links, which do not change distance or position relative to the satellite, should be made children of the satellite, and they will then never have to be updated. Because of this, all links have a primary and secondary satellite. Which the link always being the child of the primary satellite.

3.4 Patterns used

Due to the extensive customisability of the network, I elected to use the Template Method pattern in three separate locations.

- To describe different linking methods.
- To describe various different ways of colouring the network to highlight certain properties.
- To describe various tests to be applied to the network.

This gave me a lot of customizability as it came
I also utilised

3.5 Initial Observations of Network

The first and most interesting observation when modelling the network was the way satellites wrap around the network. At any given point on the ground, there will be some satellites above you moving North-East, and some moving South-East. No satellites will be moving west as that is retrograde motion, which is expensive and unnecessary. Satellites on the same orbit will remain in a fixed position relative to one another, while satellites moving in the same direction, but on different orbits, will move only slowly relative to one another. This means it is easy for a Northernly moving satellite to form stable links with other Northernly moving satellites. On the other hand, it is very difficult for a northernly moving satellite to form links with southernly moving satellites, as these satellites will be moving rather quickly relative to one another.

Because of this, an orbital sphere will contain two grids, one moving north and one moving south, with strong connectivity in the grid, but poor connectivity between the grids. It is worth noting however, that these grids are

never technically disconnected, as it is always possible to send a signal from one grid to another grid by routing it around the other side of the Earth.

This figure illustrates the concept. I have applied a gradient from black to red to all of the orbits, so that orbit 1 will be black, and orbit 17 will be red, with orbits 2 to 15 steadily growing more red, and 17 to 32 growing more black. Here we can clearly see how satellites from orbit 1 move southward underneath satellites from orbit 17.

However in the next figure we see how, when looking at the poles, the orbits have "sorted" themselves.

3.6 Visualization

For the earth texture I used a creative commons equirectangular map of the Earth. [13]

3.7 The Motion of the Player

One of the few pieces of code written in godot's native language GDScript is the code that controls user interaction with software. It made sense to write this in GDScript as GDScript is a much simpler language than C#, and because a very simple tutorial of first person motion was available in GDScript[12]. However this code required some adaptation to make it work in 3D, primarily the removal of a number of unnecessary features, and the addition of the ability to move up and down.

The code works using a "head" which is attached to a "neck". Left-right motions of the mouse are translated to left-right rotations of the neck, while up-down motions of the mouse are translated into up-down rotations of the head. By keeping the neck and head separate the player cannot turn themselves upside down or anything, which would be very disorientating. Motion is done relative to the head.

I also added the ability to free the mouse, to allow for repositioning the window and quitting the game.

3.8 Inputs

Constellations in my database are described in the a simple format that allows for much portability, this figure contains how to describe one theory or how the spaceX constellation might be arranged.

Figure 2: An orbital sphere where a gradient has been applied to the orbits

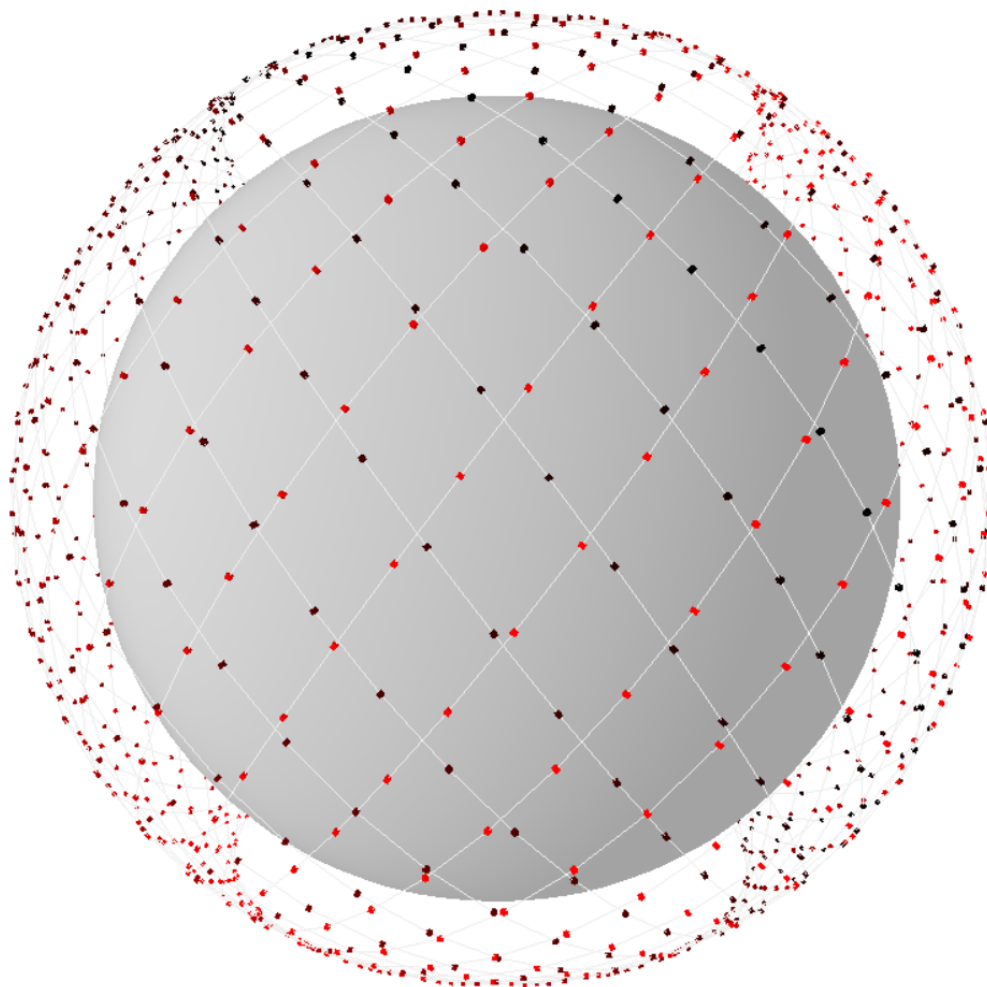


Figure 3: Looking up from inside the earth in the same model

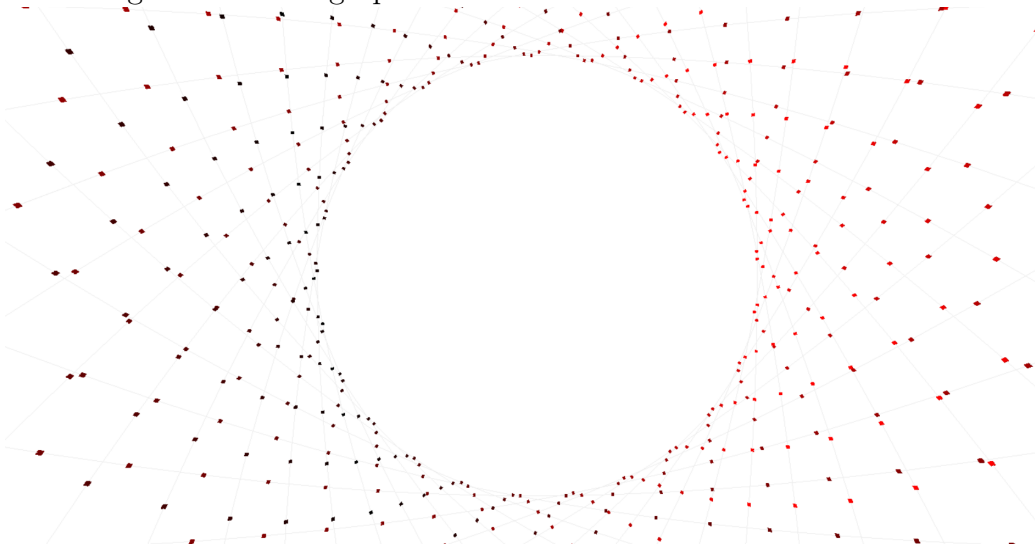


Figure 4: Keybindings.

Move Forward	W, Up Arrow
Move Backward	S, Down Arrow
Move Up	Q, Comma Key
Move Down	E, Full Stop Key
Move Left	A, Left Arrow
Move Right	D, Right Arrow
Restart Simualtion	R
Toggle Free Mouse	Esc
Activate Test	Space

Figure 5: An example for how a constellation might be described.

Number of Orbital Spheres	5				
Sphere Number	1	2	3	4	5
Altitude	1150km	1110km	1130km	1275km	1325km
Inclination	53°	53.8°	74°	80°	7°
Number of Orbits	32	32	8	5	6
Satellites per Orbit	50	50	50	75	75
Offset Between Orbits					
Offset of Sphere					
Linking Method	X	X	X	X	X

$$X = \textit{FourFixedOneFree} \begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix}$$

Notice the addition of offsets and linking methods, these are necessary to fully describe a constellation, but are not given in an FCC application.

3.9 Describing Linking Methods

A large proportion of time in the project was devoted to devising linking methods.

3.10 Finding the Nearest Satellite

One of the more surprisingly difficult tasks was locating a nearest satellite to a given satellite. As I know I was going to have to do this many times, I wanted a way to calculate the nearest satellite as quickly as possible.

Fortunately, the fact that within an orbital sphere all satellites are arranged in a grid proved extremely useful here. This figure gives the closeness to a point given the orbit and satellite numbers of the satellites in a sphere. As you can see this function increases smoothly to two peaks representing the closest point on the northward moving and southward moving grids.

Because of this a very simple algorithm can be developed to calculate the closest satellite to a point without having to search all satellites.

```

closest_satellite(Point p, OrbitalSphere X, int j, int k)
    looping = true
    while(looping)
        sat_middle = X.get(j,k)
        sat_above = X.get(j,k+1 mod X.max_k)
        if p.distance_to(sat_above) < p.distance_to(sat_middle)
            k = k+1 mod X.max_k
        else
            sat_below = X.get(j,k-1 mod X.max_k)
            if p.distance_to(sat_below) < p.distance_to(sat_middle)
                k = k-1 mod X.max_k
            else
                sat_right = X.get(j+1 mod X.max_j,k)
                if p.distance_to(sat_right) < p.distance_to(sat_middle)
                    j = j+1 mod X.max_j
                else
                    sat_left = X.get(j-1 mod X.max_j,k)
                    if p.distance_to(sat_left) < p.distance_to(sat_middle)
                        j = j-1 mod X.max_j
                    else
                        looping = false
    return X.get(j,k)

```

With a few optimisations this algorithm can run extremely fast.

However, this algorithm can only find one of the two peaks on the closeness function, so to get a true measure we have to run this algorithm twice on two points on opposite sides of the sphere and pick the closest result.

Now we can ask our linking method to use its free length to connect to a satellite in a different sphere to it, or on the same sphere travelling in the opposite direction.

However, this method hits a number of flaws. Firstly the links that are formed are not bidirectional, and also, close to the poles satellites form links across polar circle. This is because for any given area on the equator, the satellites moving south and the satellites moving north will end up at opposite sides of the circles at the poles.

Because of this, a more computationally expensive approach had to be taken.

3.11 Tests

The first test I did was a very simple test to calculate the connected components on the graph. This pseudocode gives the test.

```
connected_components(Constellation C)
    components = 0
    x = C.Sattelites
    for s in x
        if not s.marked
            components += 1
            bfs(s)
    unmark_all(x)
    return components

bfs(Sattelite s)
    q = new Queue
    q.add(s)
    while not q.empty()
        x = q.dequeue()
        if not x.marked
            x.marked = true
            for y in x.linked_sattelites
                q.add(y)
    return
```

This very straightforward test runs in $O(E)$ time, however when used on the network it becomes plainly apparent that it is not an extremely useful measure. The fact my model assumes that all satellites will be evenly spaced around the orbit (a very reasonable assumption) renders it so that satellites are either all in range of one another, or not. It is extremely unlikely that a constellation will ever be at risk of breaking into components. However this test did serve as a good way to test my ability to write tests on the network, and output to files.

3.12 Dijkstra's Algorithm

I used Dijkstra's algorithm in order to calculate shortest paths around the network, with the modification to allow for quickly retrieving the shortest

path when used.

Somewhat suprisingly, C sharp doesn't come with a priority queue, so I used one from <https://visualstudiomagazine.com/Articles/2012/11/01/Priority-Queues-with-C.aspx?Page=2>. And used comparisons from <https://github.com/BlueRaja/High-Speed-Priority-Queue-for-C-Sharp>.

3.13 Calculating the Latency Across a Path

There are 4 factors that effect the latency of a path

3.14 Coding for Visualisation and Efficient Algorithms

One of the most challenging parts of this project was writing code that would both be visualisable by the Godot engine while also running efficiently with shortest path algorithms. To do this requires the creation of numerous abstract classes and wrappers that would simplify more complex objects. There are two kinds of link

4 Evaluation

4.1 Analysis of Variables

For each of these variables, I modeled a variety of different possibilities, examining the latency of connections with each of these.

4.2 Using the Program

If you would like to see the program that was used to generate these images and results, simply download and run the exe hosted here

The exe will create files for test results in the same location as it is ran, as well as printing to the command line the results of tests as they are written.

It is recommended that you run in Windows 10, as it is not guaranteed to work in other operating systems.

You can navigate the simulation using the mouse, along with arrow keys or WASD. Press R to reset the whole simulation. Use X and Z to move between different tests. Press ESC to toggle the mouse between captured (for moving the camera) and free.

All the tests run at 20x realtime, which I found to be a very good time-factor for observing overarching trends in the network.

4.3 Test 0: Observing the constellation

This is not a test, but rather an opportunity to observe the constellation without any test running. Here we can make some observations about how the constellation works

4.4 Test 1: Highlighting Northbound and Southbound Satellites

In this test, I have applied a gradient to all of the satellites designed to highlight the

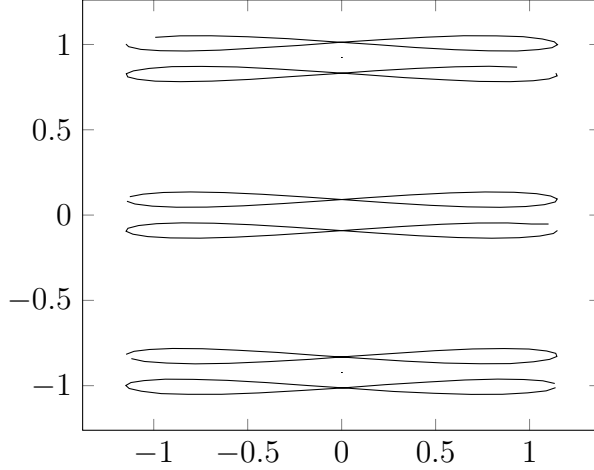
4.5 Test 2: Following a Satellite

This test locks your camera to the position of a single satellite as it moves through the constellation. Here we can see how the neighboring satellites move around you as you orbit the Earth. As you can see, the Satellites immediately before and after you remain in a constant place aside from some subtly movement, this is movement is caused by the fact that my orbits are not "perfect" but are simulated by interpolating between pre-computed translations. In an ideal orbit these satellites would remain stationary relevant to you.

Also highlighted are the 6 other closest satellites. Over the course of an orbit, the satellites to your left and right will pass back and forth across your orbital path, as your orbit crosses over their orbits. You should also see satellites moving in the opposite direction to you, Northward when you are Southward bound, and Southward when you are Northward bound, these satellites move past quite fast, and it is unlikely that you would connect to them because of the difficulty in tracking their positions. [6]

The test will output every second the coordinates of the 8 nearest satellites in the same orbital plane as you, relative to your own position and direction of motion. In the two figures you can see this motion graphed. The first figure shows the paths the 9 nearest satellites will trace relative to you, while the second shows their left/right bias over time (or rather, their distance in

Figure 6: An example of the paths that neighbors take relative to a satellite and it's direction of motion.



the z axis when the x axis is aligned with the direction of motion and the y axis is aligned towards the code of the Earth).

4.6 Test 3: Total Connectivity As Satellites Are Removed

In this test, I delete a certain number of satellites and their associated links, and then calculate the number of connected components. I do this 100 times each for 24 different levels of deletion, deleting 66 satellites (one orbit's worth) each time. The total number of connected components will not change over time, as the links between satellites are fixed and constant, so I only allow each simulation to run for one second before resetting. All of the results are logged and outputted to ConnectedComponents.csv.

The result of this test can be seen in the associated figure. I have also given a 95% confidence interval which is very small due to the high sample size. As you can see the number of disconnected components increases rapidly, before falling off rapidly towards the higher failure rates, where there are simply not enough satellites left in the constellation to form many components.

Figure 7: The distance over time from a satellite to it's neighbors perpendicular to it's direction of motion and the direction towards the core of the Earth, or how far to the left or right of the satellite it's neighbors are over time.

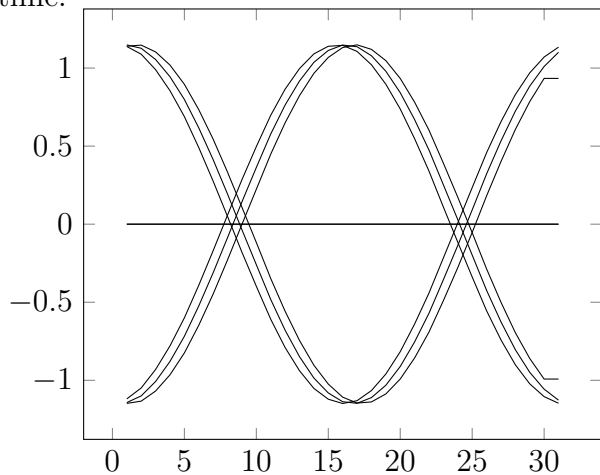


Figure 8: The number of connected components after various amounts of deletion of random satellites.

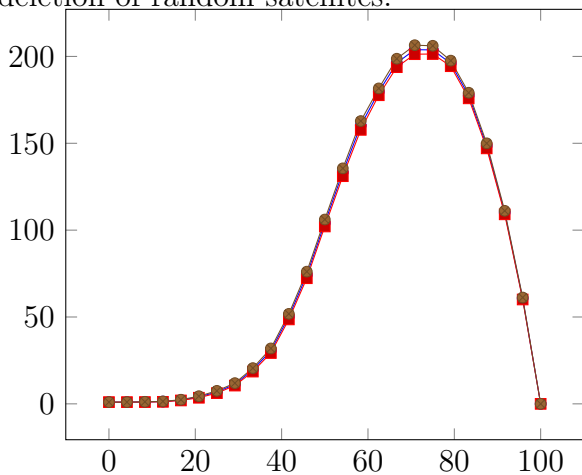
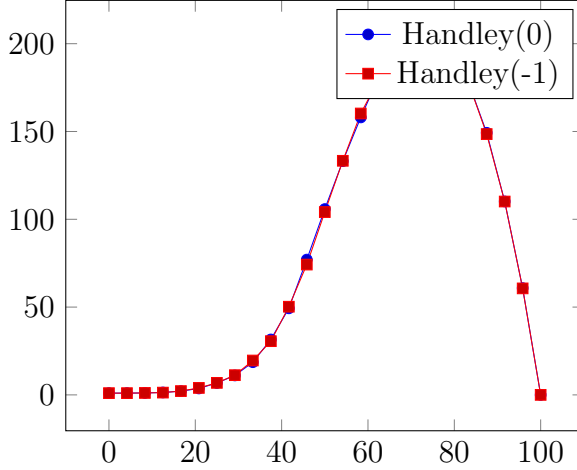


Figure 9: The number of connected components after various amounts of deletion of random satellites, using the Handley(0) linking method, compared with the Handley(-1) linking method.



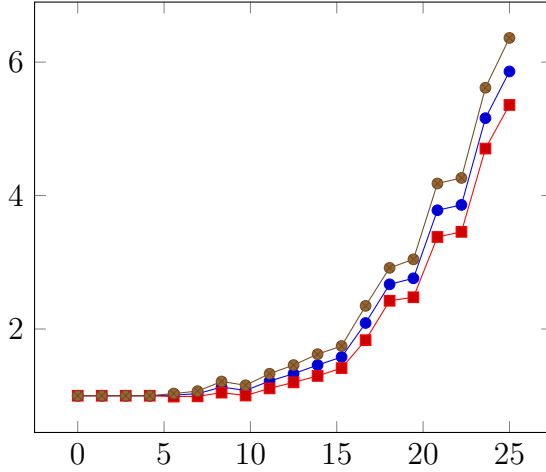
4.7 Test 4: Total Connectivity with Alternate Linking Method

Test 4 repeats the same test as before on the constellation using the Handley(0) linking method. As you can see these curves are almost completely identical, indicating that there is no significance difference in the reliability of these two different linking methods.

4.8 Test 5: Total Connectivity Localised

The initial overall results shows come interesting trends, and while it is useful to see an overall trend when increasing the failure rate all the way up to 100%, it is very unlikely that failure rates that high would ever be achieved, furthermore, as far as the engineers in SpaceX are concerned, any loss of connectivity in the constellation is bad. Because of this I ran a second test, this time examining only the failure rates up to 25%, removing 22 satellites (one third of an orbit) on each experiment, and running each test 100 times as before. Here instead of collating the data to show the average number of connected components, I instead gave the number of samples that contained more than one connected component.

Figure 10: The number of connected components after various amounts of deletion of random satellites, fucing on the range up to 25% faliure.



4.9 Test 6: Shortest Path London to New York

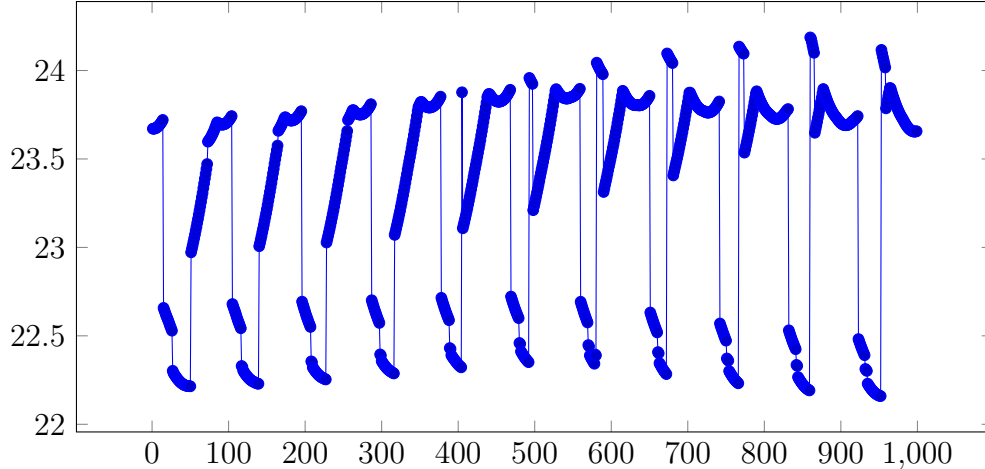
In this test I take a sample each second of the shortest path between London and New York, I then calculated the latency, which is shown below. As you can see each path remains for slightly less than a minute, these latencies change gradually as the positions of satellites move, before a shorter path becomes available, and an abrupt change is made. this is very good as it means that with a continual connections, packet reordering will be relatively uncommon. There appears to be a certain periodicity to the shortest path between two satellites, to examine this further, I ran a separate test (not in the model) at an increased speed.

4.10 Test 7-: Shortest Path London to New York

4.11 Godot as a Simulation Environment

One of the larger mistakes I think I made during this Dissertation was to choose Godot as the environment through which I would create my simulation. Godot being an open-source software hs little to no impact on the overall quality of my work, and the lack of proper support for the still relativey new engine, alongside some deficiencies in the debugging ability and a few bugs in the C# interaction made coding significantly harder. While

Figure 11: The Latency of the London-New York connection over time



in my pitch I argued I was using Godot because it was free and easy-to-use, in reality I was simply using it because it was familiar to me, If I had taken some extra time at the start of my project to familiarise myself with a more powerful engine, I could have saved time in the long run.

4.12 Direction and Focus

Maintaining a consistent goal has been challenging during such an open-ended project. If I were to do this project again I would more carefully choose my objectives

A number of projects in the early phases of the project had to be abandoned not just because of inefficiency but because new information came about that rendered them useless.

The announcement from SpaceX on that they were significantly changing the constellation had massive impacts to the project. Firstly, the new satellites would have only four links instead of five, this implied that the satellites would not have a "free" link but would instead be connected only to those ahead of and behind them. Because of this, I decided to drop the free links from my model, but doing so meant that a large chunk of code that had been written was discarded.

The knowledge that SpaceX were willing to change their designs so abruptly also had a significant impact on modelling their constellation. It is likely that

the second and third phases of Starlink will be similarly changed to be in similar altitudes to phase one, however without a full understanding on what these new spheres would be, or how they would connect to phase one, it was elected to instead focus solely on the first sphere's constellation.

5 Conclusion

References

- [1] <https://www.exede.com>
- [2] <https://www.hughes.com>
- [3] <https://twitter.com/elonmusk/status/1000453321121923072>
- [4] licensing.fcc.gov/cgi-bin/ws.exe/prod/ib/forms/reports/related_filing.htm?f_key=-289550&f_number=SATLOA2016111500118
- [5] https://licensing.fcc.gov/myibfs/download.do?attachment_key=1158350
- [6] <http://nrg.cs.ucl.ac.uk/mjh/starlink/>
- [7] <http://stuffin.space/>
- [8] <http://ece466.groups.et.byu.net/notes/smf28.pdf>
- [9] <https://www.hughes.com/who-we-are/resources/press-releases/hughes-high-throughput-satellite-successfully-launched-setting?locale=en>
- [10] https://space.skyrocket.de/doc_sdat/jupiter-2.htm
- [11] <file:///home/joe/Downloads/R12-ITURKA.BAND-C-0008!!PDF-E.pdf>
- [12] <https://github.com/turtletooth/GodotFirstPersonController>
- [13] https://commons.wikimedia.org/wiki/File:USGS_majplatecolor.png

A Appendix A