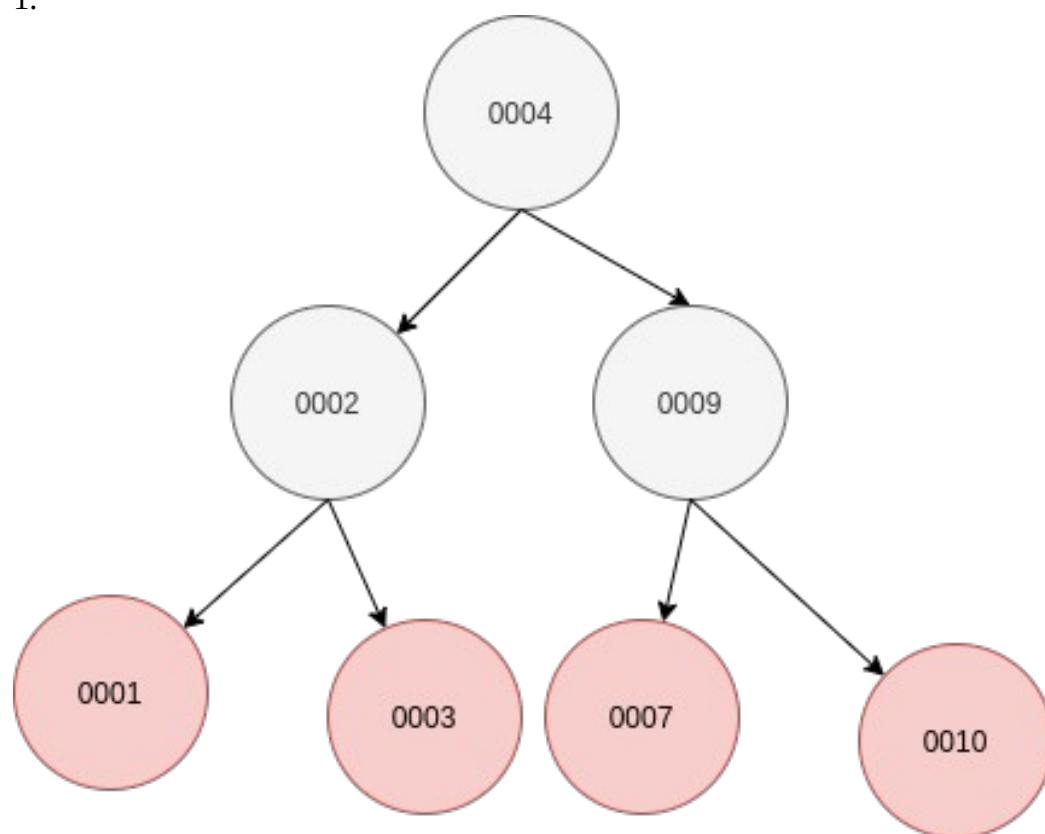
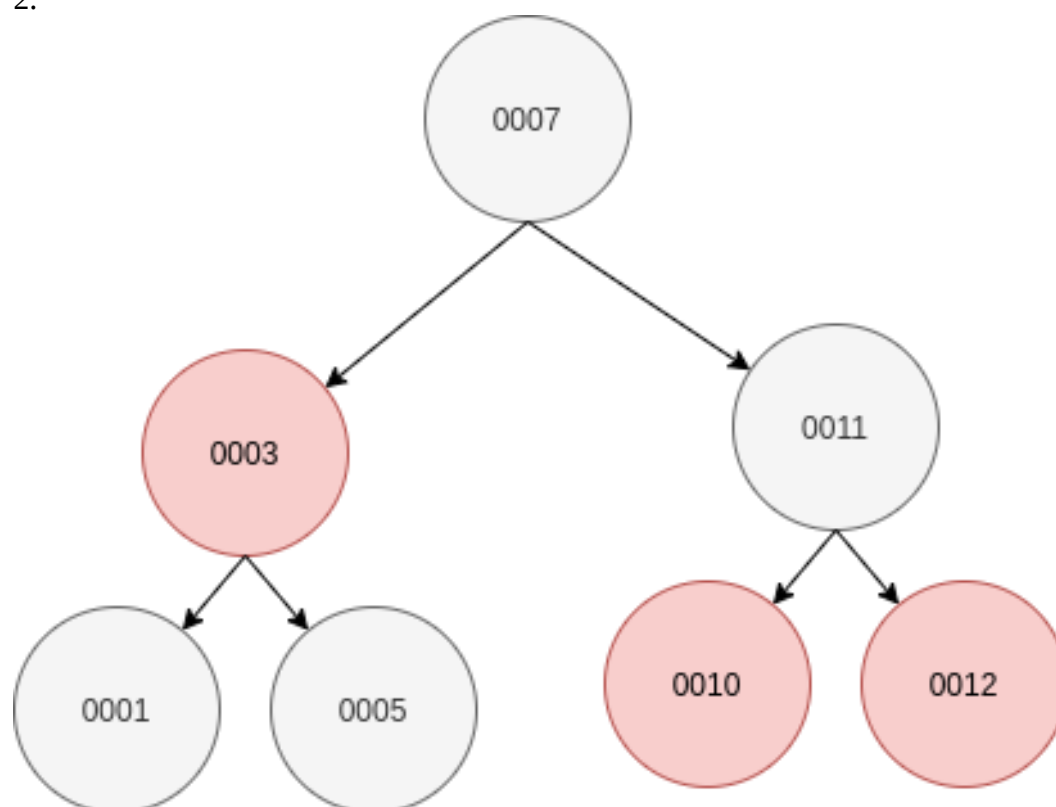


Joseph Steeb
3-27-2021
1.

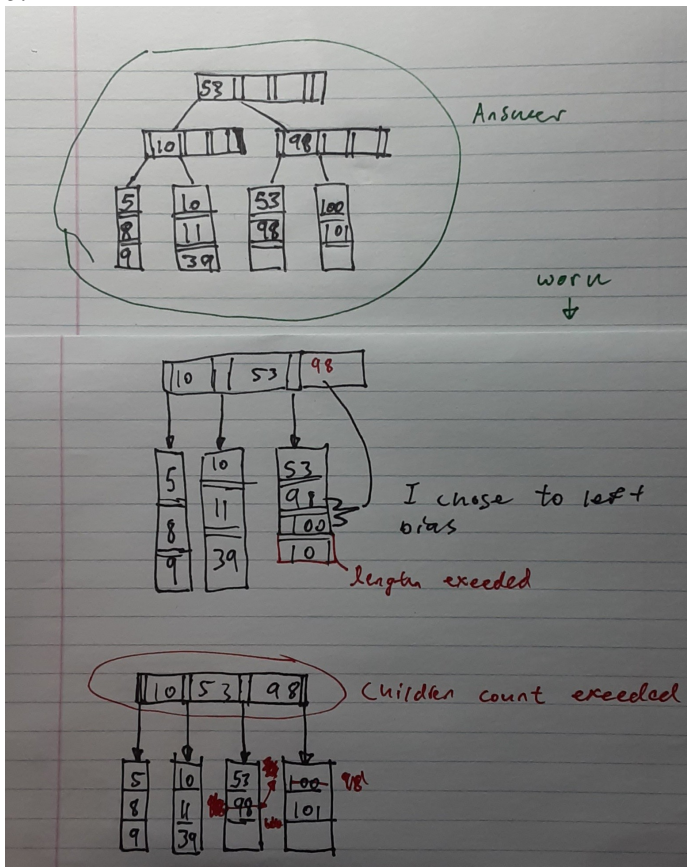


2.

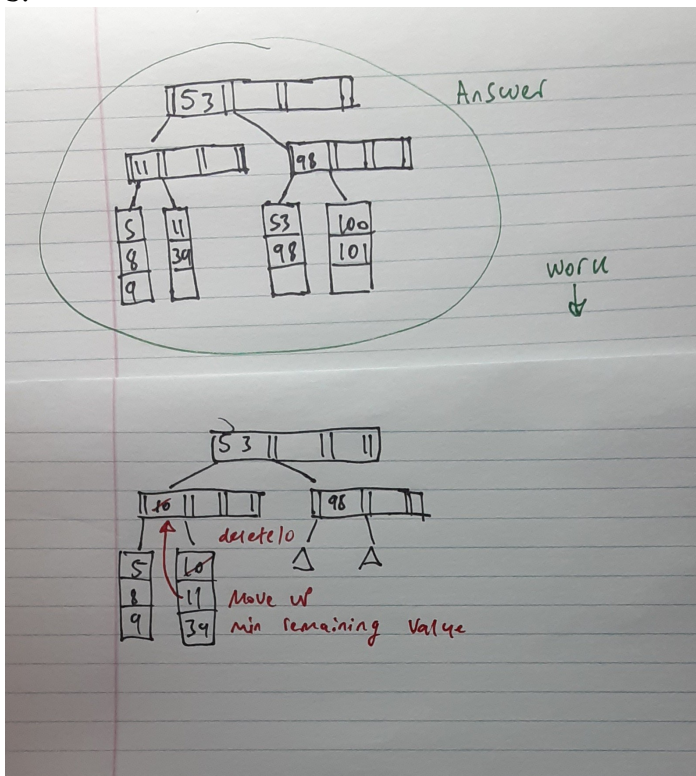


3.

a.



b.



4.

a. Assuming each internal node can at most fill one block of disk space in Ext4; a max size node would contain 8192 bytes. Each element of an internal node will contain a UUID and pointers on either side. The calculation to find max is as follows.

$$\text{UUID size} = 64/8 = 8 \text{ bytes}$$

$8192 - 8 = 8184$ subtracting eight bytes because there is always one more pointer than keys.

$$8184/(8+8) = 511.5 \text{ key pointer pairs} + 1 \text{ extra pointer}$$

$$\text{total number of pointers} = 512$$

b. Again assuming that a whole block should be used for leaf nodes, the same process as part a should be used. Leaf nodes however contain additional bytes to store name and sales.

$$\text{Sales size} = 32/8 = 4$$

$$\text{name size} = 32$$

$$\text{UUID} = 8$$

$$4 + 32 + 8 = 44 \text{ bytes}$$

$8192 - 8 = 8184$ subtracting eight bytes because each leaf node has a pointer to the next leaf

$$8184/(44) = 186$$

$$\text{total number of records} = 186$$

$$\text{c. Height} = \log_m(N) = \log_{512}(N)$$

$$\text{d. Height} = \log_{512}(30000) = 2$$

$$\text{e. Height} = \log_{512}(2500000) = 3$$