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1.
 - a. Both programs have a runtime complexity of $O(n)$ because they loop n times.
 - b.

```
int g(int n)
{
    return n;
}
```
2. $g(n)$ has $O(\log(n))$ complexity, because there is division by 2 in the number of times it loops.
- 3.

```
#include <iostream>
bool checkArr(bool nums[10])
{
    for(int i = 0; i < 10; i++)
    {
        if(!nums[i])
            return false;
    }
    return true;
}

int findK(int n)
{
    int k = 1;
    bool nums[10] = {0, 0, 0, 0, 0, 0, 0, 0, 0, 0};
    while(!checkArr(nums))
    {
        int nMultiplied = k*n;
        int nCopy = nMultiplied;
        unsigned int nLength = 0;

        do
        {
            ++nLength;
            nCopy /= 10;
        }while(nCopy);

        nums[nMultiplied % 10] = true;

        for(int i = 1; i < nLength; i++)
        {
            int divisor = pow(10,i);
            nums[nMultiplied / divisor % 10] = true;
        }
        k++;
    }
    return k-1;
}
```

It would be very difficult to directly formalize a worst case for this algorithm, because there is no relationship between the size of the number, and the complexity of the algorithm. I estimate that the worst case is somewhere around $O(n^2)$.

4.

- a. $O(1)$. requires only the use of modulo. `if(!n%2){return true;}`
- b. $O(\log n)$ if the list is sorted, otherwise $O(n)$. If the list is sorted binary search can be used which halves the search every time, resulting in logarithmic complexity, otherwise the whole list must be iterated over, resulting in $O(n)$.
- c. $O(1)$ if the list is sorted, $O(n)$ if unsorted. If sorted, simply return the first or last element, otherwise the whole list must be iterated over, resulting in $O(n)$.
- d. $O(n^2)$. For each element of one list, the entire second list must be iterated over.
- e. $O(n)$. Simply compare the values at each index.
- f. $O(\log(n))$. The equation to get the height of a BST is $\text{ceiling}[\log(n+1)]$, and If we are finding worst case complexity, the full height of the tree must be traversed.

5.

```
#include <iostream>

bool contains(char c, std::string s)
{
    for(char const &element : s)
    {
        if(element == c)
            return true;
    }
    return false;
}

bool isAnnogram(std::string s1, std::string s2)
{
    for(char const &element : s2)
    {
        if(!contains(element, s1))
            return false;
    }
    return true;
}
```