

# ‘Cause I’m Strong Enough: Reasoning about Consistency Choices in Distributed Systems

Presented By:  
Aldrin Montana

# Example

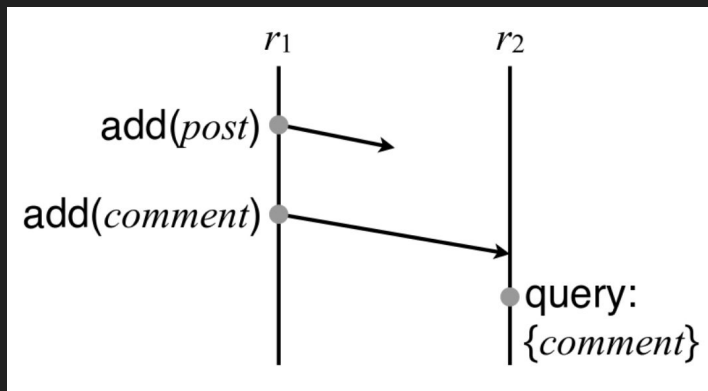


Figure 1A  
Illustration of **Add** and **Query**

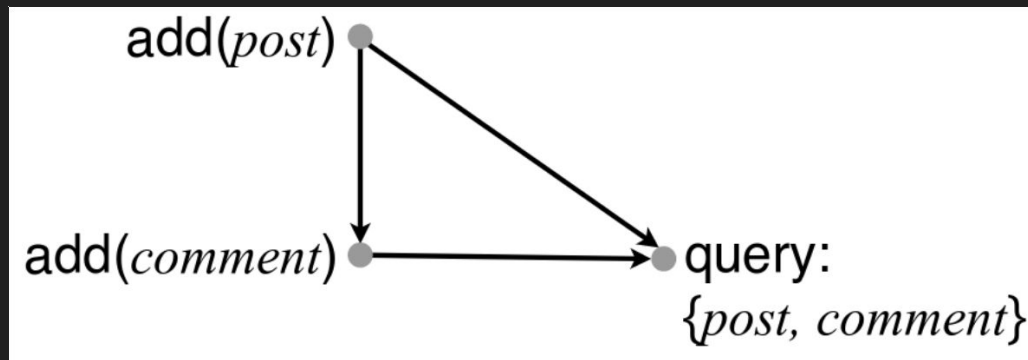


Figure 2A  
Example of Definition 1  
for **Add** and **Query**

# Example

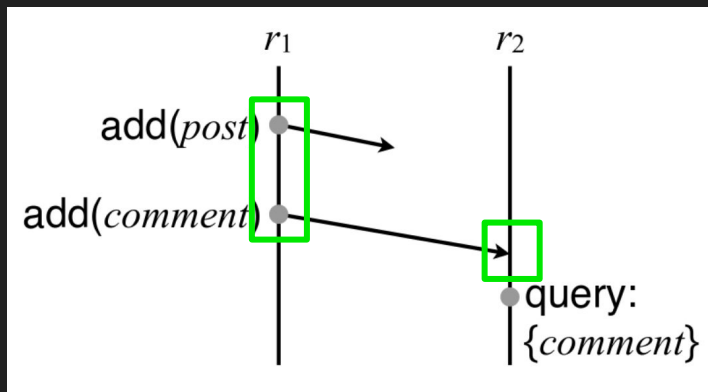


Figure 1A  
Illustration of **Add** and **Query**

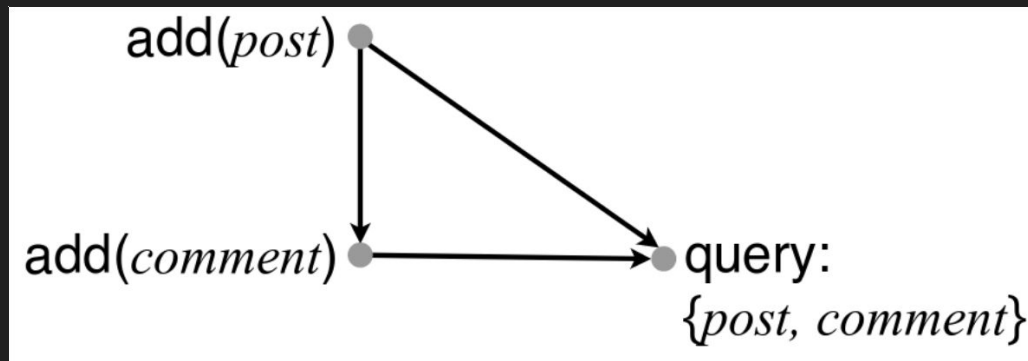


Figure 2A  
Example of Definition 1  
for **Add** and **Query**

# Example

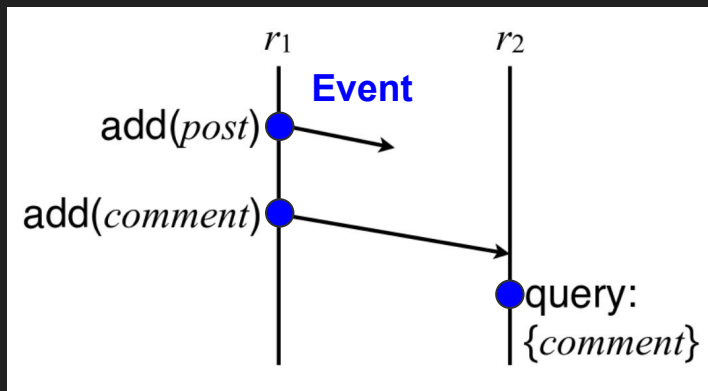


Figure 1A  
Illustration of **Add** and **Query**

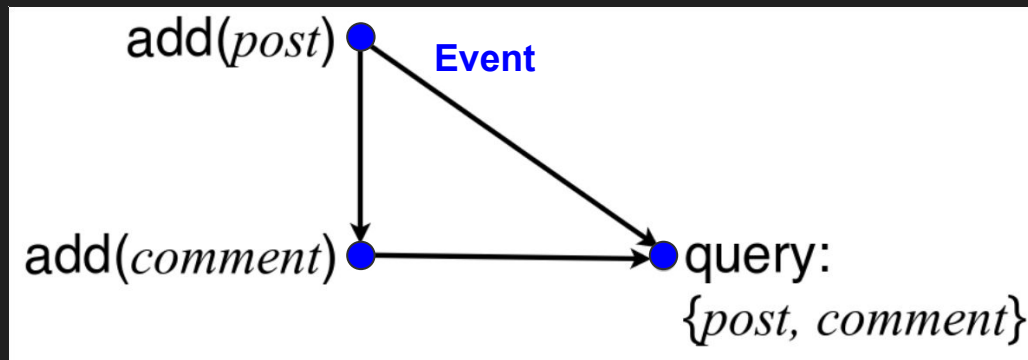


Figure 2A  
Example of Definition 1  
for **Add** and **Query**

# Example

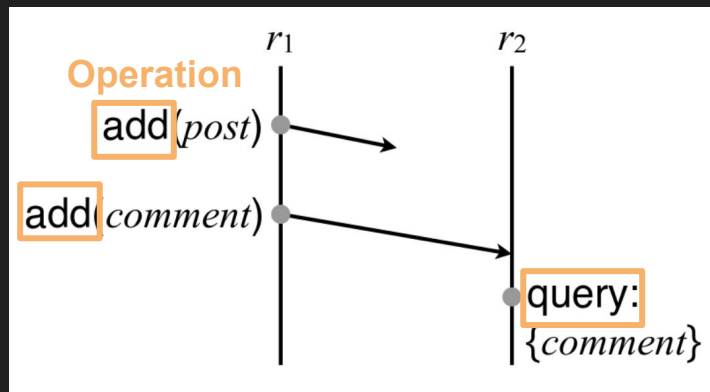


Figure 1A  
Illustration of **Add** and **Query**

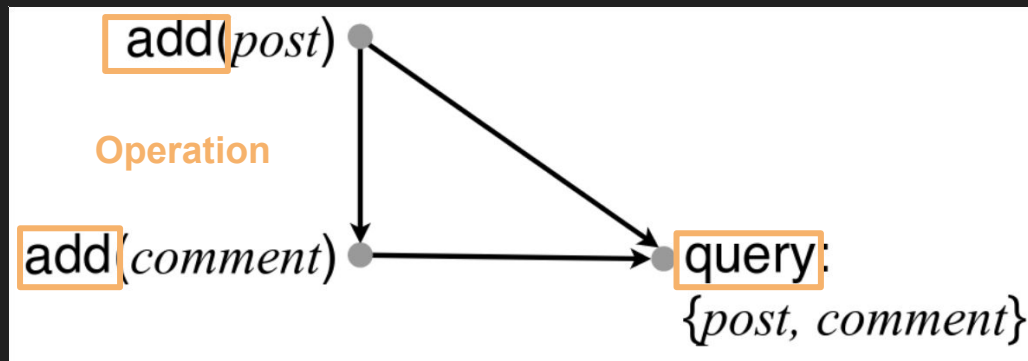


Figure 2A  
Example of Definition 1  
for **Add** and **Query**

# Example

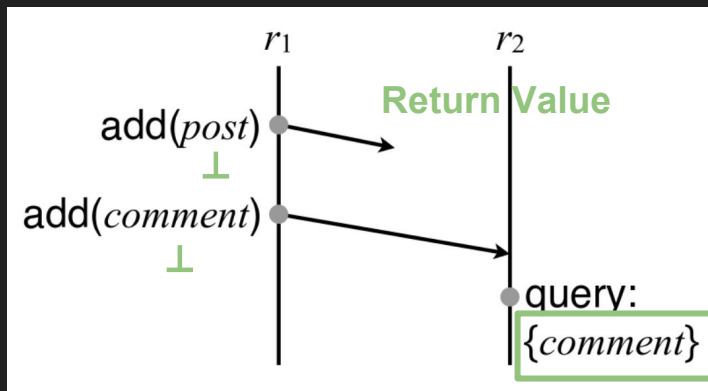


Figure 1A  
Illustration of **Add** and **Query**

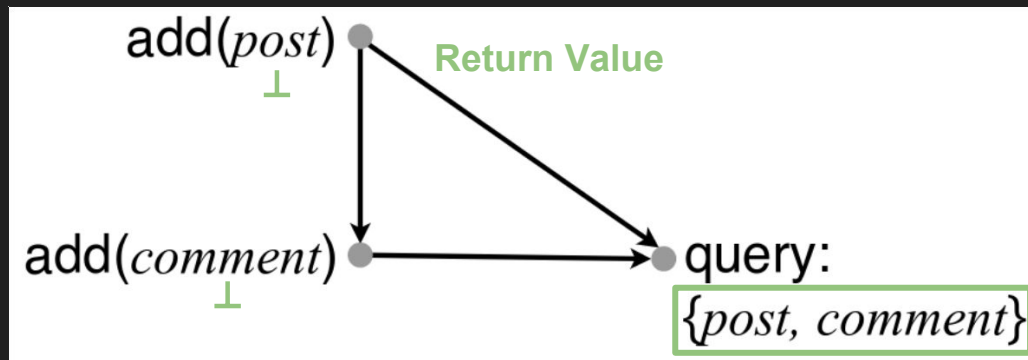


Figure 2A  
Example of Definition 1  
for **Add** and **Query**

# Example

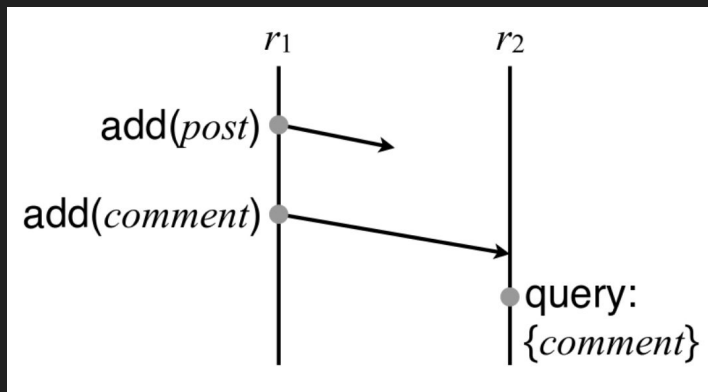


Figure 1A  
Illustration of **Add** and **Query**

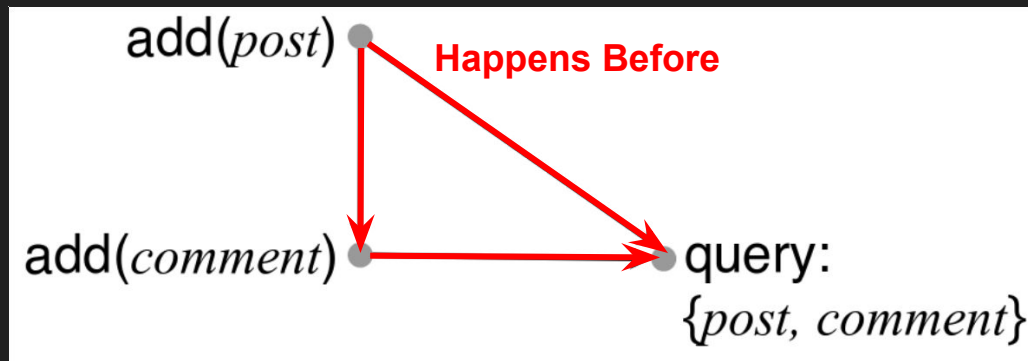


Figure 2A  
Example of Definition 1  
for **Add** and **Query**

# Example

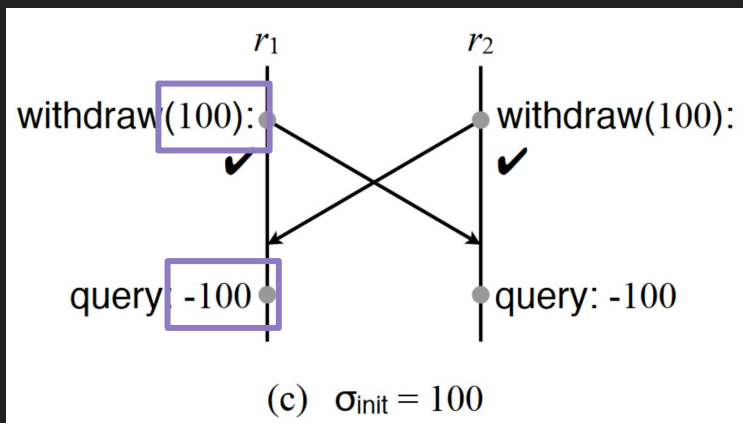


Figure 1C  
Illustration of **Withdraw** and **Query**

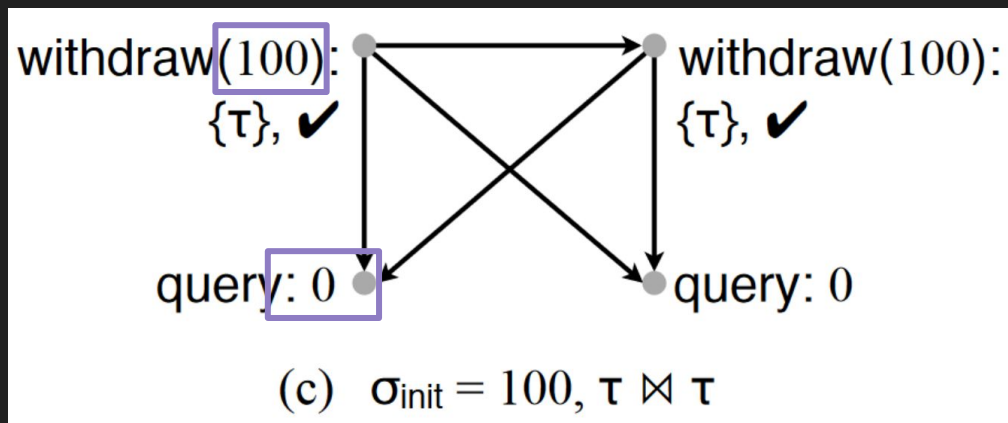


Figure 2C  
Example of Definition 1  
for **Withdraw** and **Query**



# Definitions and Notations

$$\begin{aligned} F \in \text{Op} &\rightarrow (\text{State} \rightarrow (\text{Val} \times (\text{State} \rightarrow \\ &\text{State}))) \\ F_o(\sigma) &= (\text{Val} , (\text{State} \rightarrow \text{State})) \\ F_o(\sigma) &= (F_o^{\text{val}}(\sigma) , (F_o^{\text{eff}}(\sigma) \quad )) \end{aligned}$$

# Example

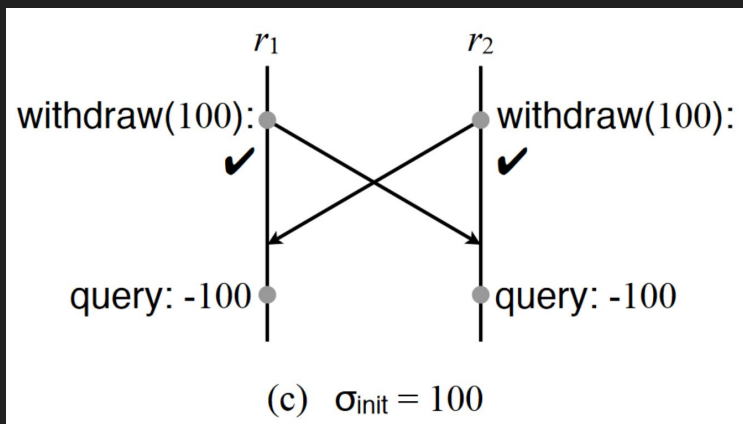


Figure 1C  
Illustration of **Withdraw** and **Query**

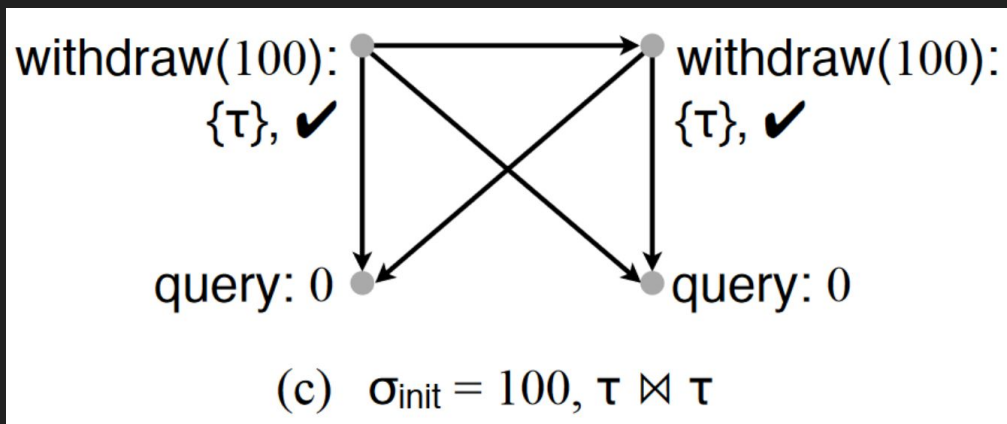


Figure 2C  
Example of Definition 1  
for **Withdraw** and **Query**

# Example

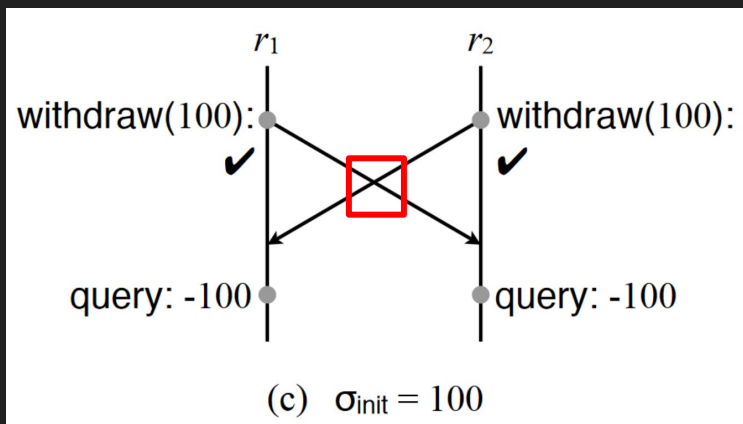


Figure 1C  
Illustration of **Withdraw** and **Query**

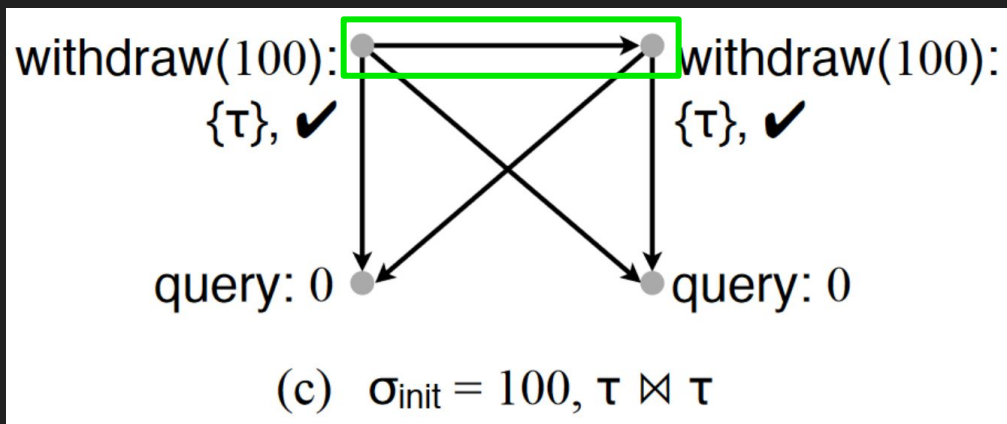


Figure 2C  
Example of Definition 1  
for **Withdraw** and **Query**

# Example

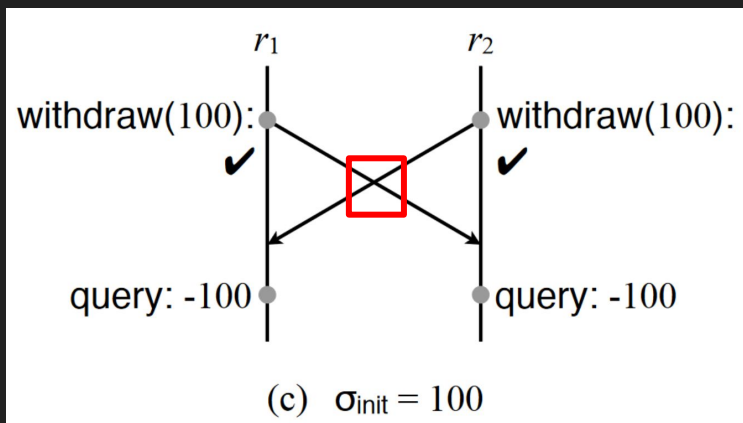


Figure 1C  
Illustration of **Withdraw** and **Query**

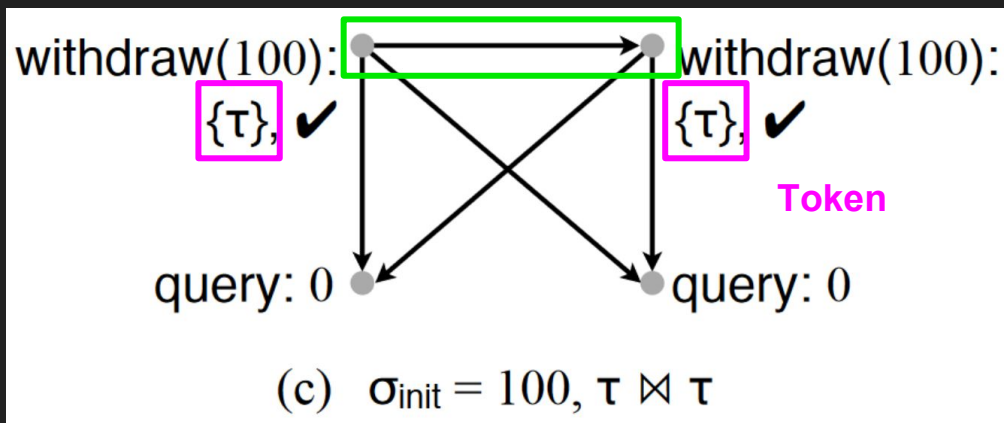


Figure 2C  
Example of Definition 1  
for **Withdraw** and **Query**

# Definitions and Notations - Extensions

$$I = \{\text{subset of State}\}$$

$$T = (\text{Token}, \bowtie)$$

$$F \in \text{Op} \rightarrow (\text{State} \rightarrow (\text{Val} \times (\text{State} \rightarrow \text{State})) \times \mathbb{P}(\text{Token}))$$

$$F_o(\sigma) = (\text{Val}, (\text{State} \rightarrow \text{State}), \mathbb{P}(\text{Token}))$$

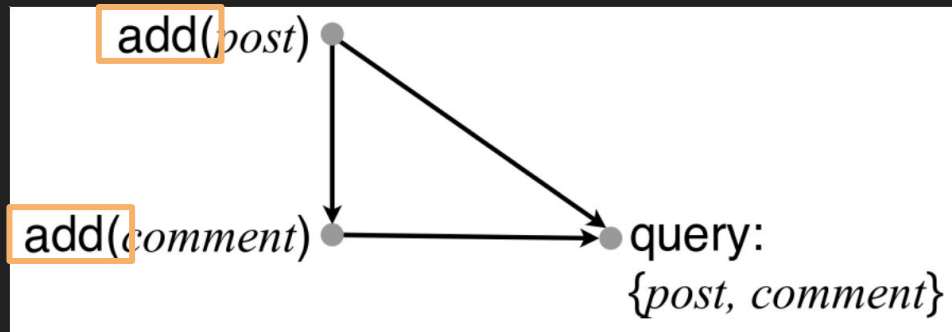
$$F_o(\sigma) = (F_o^{\text{val}}(\sigma), (F_o^{\text{eff}}(\sigma)), F_o^{\text{tok}}(\sigma))$$

# Definitions and Notations - Extensions

$$T = (\text{Token}, \bowtie)$$

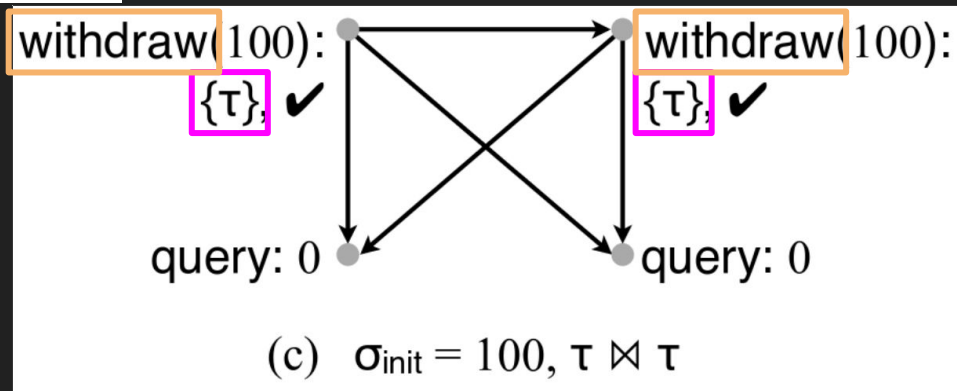
$$\begin{aligned} & \mathcal{F}_{\text{withdraw}(a)}(\sigma) \\ = & \left\{ \begin{array}{ll} (\checkmark, (\lambda\sigma'.\sigma' + .05 * \sigma), T), & \text{if } \sigma \geq a \\ (\times, \text{skip}, T), & \text{else} \end{array} \right. \end{aligned}$$

# Intuition



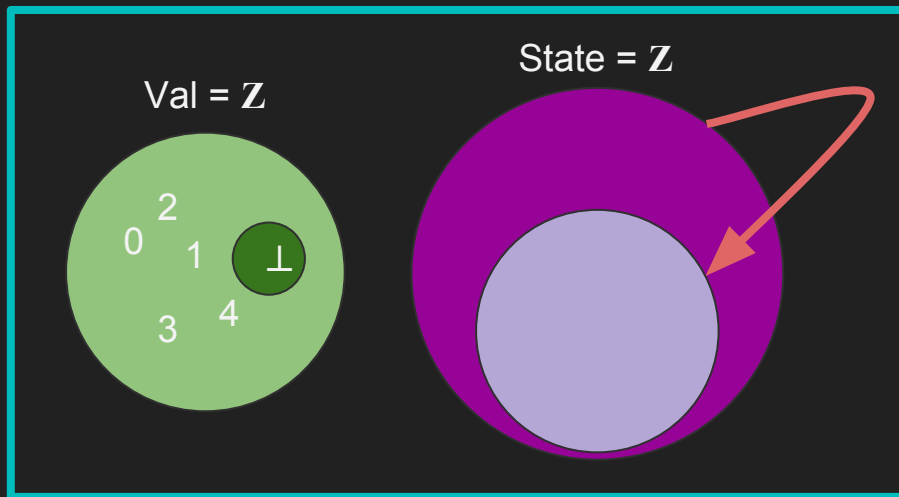
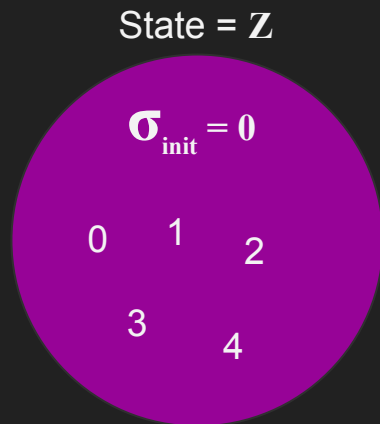
If **operations** are **convergent**,  
then **tokens** are **not necessary**

If **operations** are **not convergent**,  
then **tokens** are **necessary**



# Definitions and Notations

$$F \in \text{Op} \rightarrow (\text{State} \rightarrow (\text{Val} \times (\text{State} \rightarrow \text{State})))$$





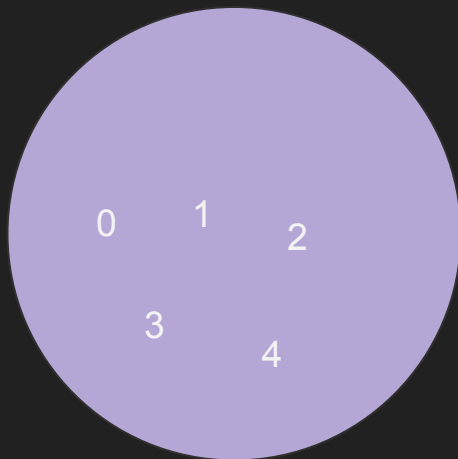
# Definitions and Notations

State



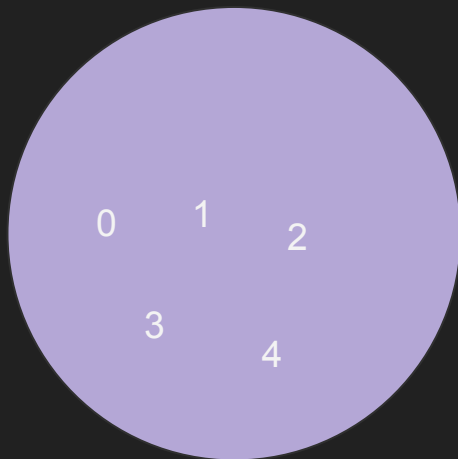
# Definitions and Notations

State =  $\mathbb{Z}$

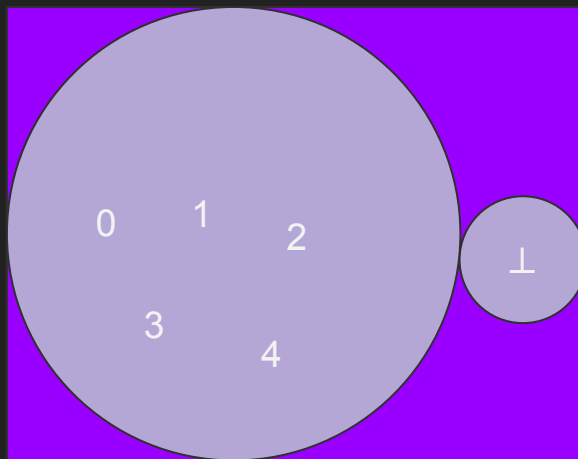


# Definitions and Notations

State =  $\mathbb{Z}$

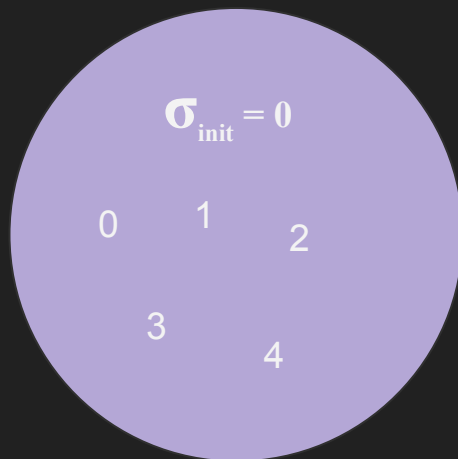


Val =  $\mathbb{Z}$



# Definitions and Notations

State =  $\mathbb{Z}$



Val =  $\mathbb{Z}$

