Pulse-Shape Effects on the Autler-Townes Doublet in Strong-Field Ionization of Atomic Hydrogen

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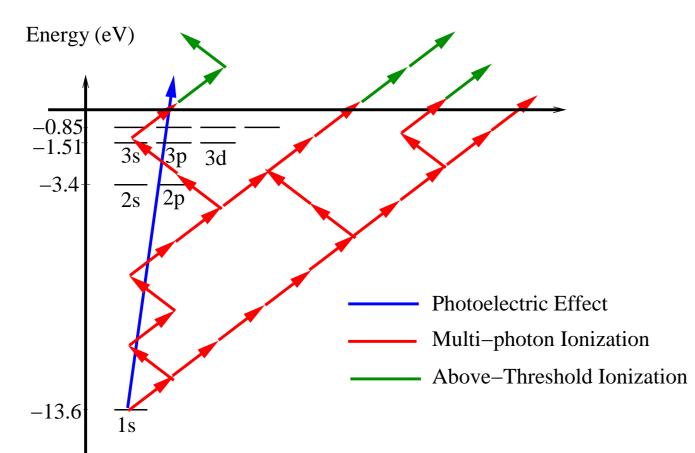
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Abstract

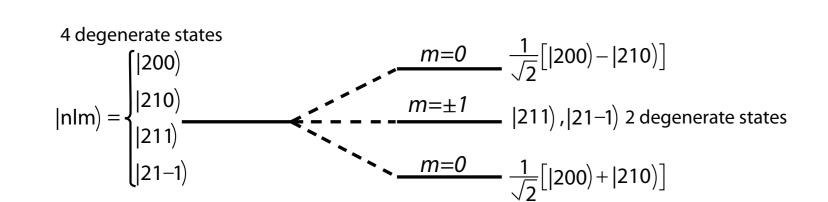
We have applied a newly developed parallelized computer code to treat the ionization of atomic hydrogen by a strong laser pulse. In particular, we studied the effect of the pulse shape, as well as the peak intensity and the central wavelength, on the theoretical results for the so-called Autler-Townes doublet. While the splitting is well known for the quasi-static case, the *dynamic* (time-dependent) Stark effect studied here is much less understood. The strong dependence on the laser pulse found in this work is not only surprising, but may also be a limiting factor for calibrating absolute laser intensities.

Introduction and Motivation

- Very short and intense laser pulses can be used to study the details of (valence) electron interactions in atoms and molecules.
- Typical laser intensities in this field range from 10^{12} to 10^{15} W/cm².
- 10¹⁴ W/cm² is a million billion times stronger than the radiation that the Earth receives from the Sun directly above us on a clear day.
- Such intensities can rip electrons away from atoms in several ways:
- -Multi-photon ionization
- Above-threshold ionizationField (tunnel) ionization



The Stark Effect



- The **Stark effect** splits up the energetically degenerate (for fixed n) energy levels in atomic hydrogen by the interaction with a strong external electric field.
- The energy splitting is proportional to the electric field strength.
- For linearly polarized light, we can "see" only the two m=0 levels.
- These levels form the **Autler-Townes doublet** in the energy spectrum of the ejected electron.
- We investigate this doublet in two-photon ionization, where the central frequency of the laser is tuned in such a way that it either hits (0.375 a.u. = 10.2 eV) or just misses (0.350 a.u. = 9.5 eV) the $1s \rightarrow 2s$, 2p resonance transition as as stepping stone.
- Also, we vary the splitting by ramping on/off the pulse.
- Notation: S (T) = \sin^2 (trapezoidal) envelope at ramp-on/off. $n_1 n_2 n_3$: number of cycles for ramp-on-plateau-ramp-off

Numerical Method

• We start with the **Time-Dependent Schrödinger Equation**

$$\dot{\boldsymbol{I}}\Psi = i\frac{\partial}{\partial t}\Psi$$

• In the **Length Form** of the electric dipole operator,

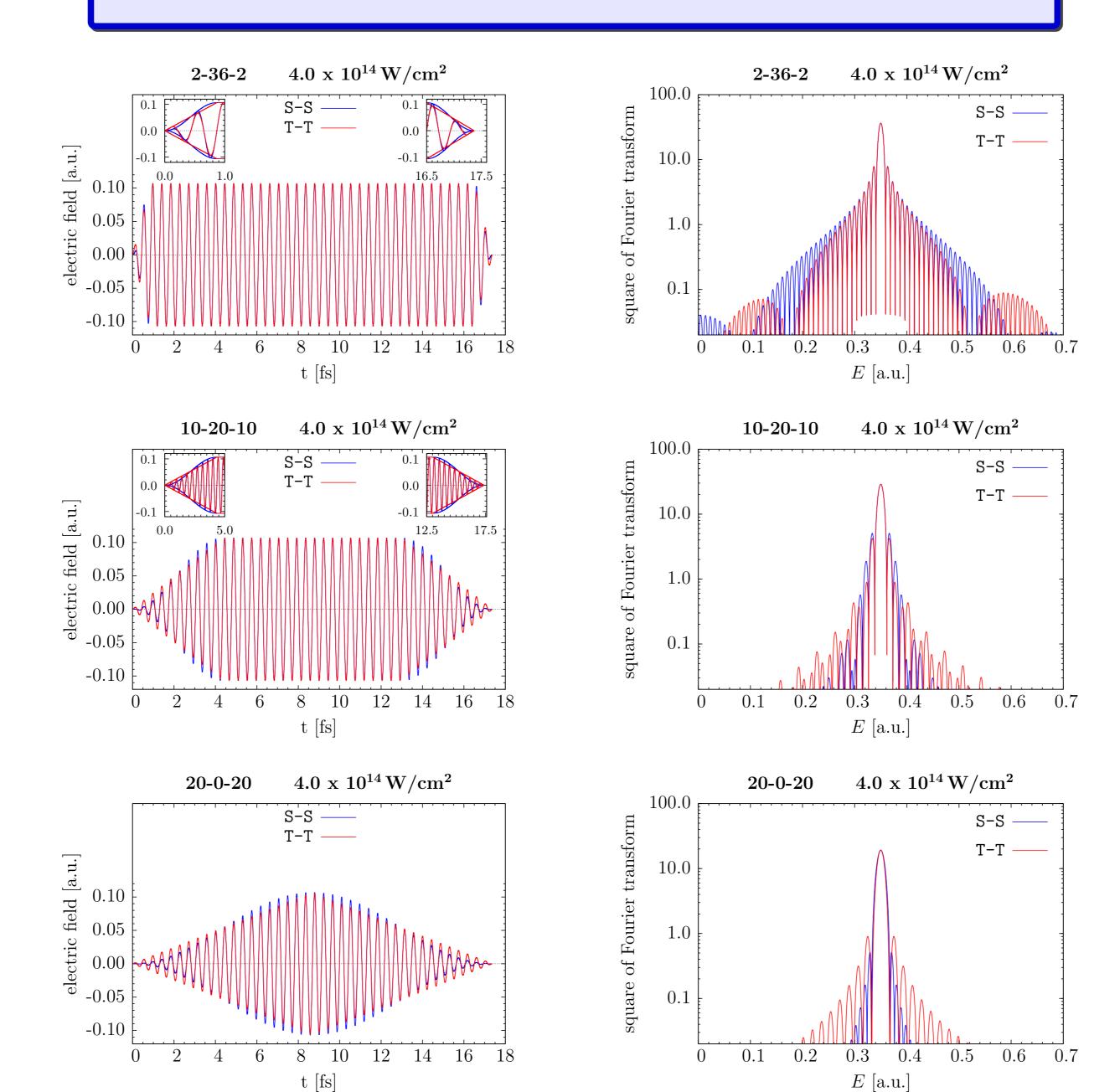
$$\hat{\mathbf{H}} = -\frac{1}{2}\nabla^2 - \frac{1}{r} + r\cos(\vartheta)E(t) \tag{2}$$

- We propagate the initial wavefunction $\Psi(\mathbf{r}, t=0)$ in time using **Finite Differences**.
- We use the Crank-Nicolson Approximation

$$\Psi(\mathbf{r}, t + \Delta t) \approx \frac{1 - i\hat{\mathbf{H}}\Delta t/2}{1 + i\hat{\mathbf{H}}\Delta t/2}\Psi(\mathbf{r}, t)$$
(3)

• This is an **implicit** method that allows for large timesteps.

The Field



• The pulse-shape effect only occurs at the highest intensity studied $(4.0 \times 10^{14} \text{ W/cm}^2)$.

Conclusions

• This suggests possible interference effects between electrons ejected at different times.

- It also only occurs if the pulse is ramped on/off very rapidly.
- The ramp-off is far more important than the ramp-on.
- Further work is needed to explain the details.

2-36-2 $0.25 \times 10^{14} \, \mathrm{W/cm^2}$ S-S 2-36-2 $1.0 \times 10^{14} \, \mathrm{W/cm^2}$ S-S 2-36-2 $4 \times 10^{14} \, \mathrm{W/cm^2}$ S-S 2-36-2 $4.0 \times 10^{14} \, \mathrm{W/cm^2}$ S-S Ionization — $\begin{array}{c} n \le 2 \\ n > 2 \end{array}$ 2-36-2 $4.0 \times 10^{14} \, \mathrm{W/cm^2}$ 10.2 eV 2-36-2 $0.25 \times 10^{14} \, \text{W/cm}^2$ 10.2 eV T-S ---10.00 S-T ---T-T ---- $0.10 \quad 0.15 \quad 0.20$ E [a.u.] E [a.u] 2-36-2 $4.0 \times 10^{14} \, \mathrm{W/cm^2}$ 9.5 eV 2-36-2 $0.25 \times 10^{14} \, \mathrm{W/cm^2}$ $9.5 \, \mathrm{eV}$ T-S ---T-S ---10.00 10.00 S-T ----S-T T-T ----0.20E [a.u.] E [a.u.] 3-34-3 $4.0 \times 10^{14} \, \mathrm{W/cm^2}$ 9.5 eV 4-32-4 $4.0 \times 10^{14} \, \mathrm{W/cm^2}$ 9.5 eV 100.00 100.00 S-S ---S-S ---T-S ---T-S -10.00 10.00 S-T ----S-T Т-Т ----T-T ----

0.01

 $0.10 \quad 0.15 \quad 0.20$

 $0.25 \quad 0.30 \quad 0.35 \quad 0.40$

E [a.u.]

 $0.10 \quad 0.15 \quad 0.20$

 $0.25 \quad 0.30$

E [a.u.]

Results