

# Datathon 2023

NTT data

November 2023

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## 1 Supositions

- Price of product in year  $n$  is last year's price multiplied by a ratio  $\gamma$  (inflation)
- Central storage center that supplies all hospitals (stores their "almacenable" products)
- Environmental cost  $\propto$  #orders
- Unlimited transit (limited indirectly by maximum capacity of storage center)
- Products are distributed to hospitals in a uniform way (Not exactly: elaborate later)
- Mensual orders

## 2 Extras

- For products of "transito" we group them by day manually

### 3 Parameters

**Note.** Vamos a agrupar las compras de todos los hospitales en una única compra centralizada

Initial definition:

- $I = \{\text{index of product}\}$

Constantes:

- $\gamma$ : factor multiplicativo del precio de año a año (inflación + ...)
- $c_i$ : storage cost for a product  $i$  (unitary) for a day
- $C_{max}^i$ : maximum quantity of product  $i$  that we can store

Precalculados

- $v^i(t)$ : consumption velocity of product  $i$  at time  $t$
- $\xi^i(t)$ : all hospitals unified demand of product  $i$  at time  $t$



Constants to change by client:

- $\beta$ : extra quantity factor in order (resilience)
- $P_{max}$ : # orders  $\propto$   $CO_2$  emissions

## 4 Variables

- $p^i(t)$  : quantity of product  $i$  demanded at time  $t \in \{1, \dots, 12\}$
- $\delta(t)$ : boolean (binary) variable to determine if there is an order at time  $t \in \{1, \dots, 12\}$

## 5 Restrictions

 **Remark** . Fijamos  $i$ . Ajustamos un modelo para cada producto

**Definition 1.** We define  $S^i(t)$  as the inventory of product  $i$  at time  $t$ :

$$S^i(t+1) = - \sum_{t'=1}^t v^i(t') + \sum_{t'=1}^t \delta(t') \cdot p^i(t').$$

Capacity restriction:

$$S^i(t) \leq C_{max}^i.$$

Restriction to verify we have enough inventory

$$S^i(t) + \sum_{t'=1}^{t-1} v^i(t') \geq \beta \cdot \sum_{t'=1}^{t-1} \xi^i(t').$$

Restriction to only do  $P_{max}$  orders:

$$\sum_{t=1}^{12} \delta(t) = P_{max}.$$

Basic restrictions:

$$\begin{aligned} S^i(t) &\geq 0 \\ p^i(t) &\geq 0. \end{aligned}$$

Restrictions over variables:

$$\delta(t) \in \{0, 1\}.$$

 **Remark** . ESTO SE DEBE VERIFICAR  $\forall t = 1, \dots, 12$

## 6 Objetivos

- Minimizar precio

Formula a minimizar:

$$\min \sum_t S^i(t) \cdot c_i.$$