IN THIS STEP WE FIND THE ASYMPTOTES FOR OUR GRAPH

A VERTICAL ASSIMPTOTE FOR A FUNCTION IS A VERTICAL LINE X = K SHOWING WHERE THE FUNCTION BECOMES LINROLINDED.

IF YOUR FUNCTION IS RATIONAL, THAT IS, IF F(X) HAS THE FORM OF A FRACTION, F(X) = P(X) / Q(X), IN WHICH BOTH P(X)AND Q(X) ARE POLYNOMIALS, THEN WE FOLLOW THESE TWO STEPS:

- 1. FACTOR BOTH THE NUMERATOR (TOP) AND DENOMINATOR (BOTTOM). THIS IS VERY IMPORTANT BECAUSE IF ANY FACTORS END UP CANCELING, THEN THEY WOULD NOT CONTRIBUTE ANY VERTICAL ASYMPTOTES.
- 2. ONCE YOUR RATIONAL FUNCTION IS COMPLETELY REDUCED, LOOK AT THE FACTORS IN THE DENOMINATOR. IF THERE IS A FACTOR INVOLVING (X R), THEN X = R IS A POSSIBLE ASYMPTOTE. IF THERE IS A FACTOR INVOLVING (X + R), THEN X = R IS A POSSIBLE ASYMPTOTE. NOTE HOW THE SIGN SEEMS TO BE OPPOSITE BOTH TIMES (JUST LIKE SOLVING A FACTORED POLYNOMIAL THAT HAS BEEN SET EQUAL TO ZERO).
- 3. TAKE EACH "POSSIBLE ASYMPTOTE" AND CHECK IF A LIMIT EXISTS AT THAT POINT IN THE GRAPH, THIS MEANS $\lim_{} \qquad \lim_{} \qquad \lim_{}$

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4. TO FIND THE HORIZONTAL ASYMPTOTE SET $x \to \infty$ FOR YOUR FUNCTION

 $\chi^3 - 6\chi^2 + 9\chi + 1 = y$ Polynomial, therefore no restriction. Also because $\chi \in \mathbb{R}$ no vertical Asymptote Because $y \in \mathbb{R}$, no horizontal Asymptote