IN THIS STEP WE FIND THE ASYMPTOTES FOR OUR GRAPH

A VERTICAL ASSMPTOTE FOR A FUNCTION IS A VERTICAL LINE X = K SHOWING WHERE THE FUNCTION BECOMES UNBOUNDED.

IF YOUR FUNCTION IS RATIONAL, THAT IS, IF F(X) HAS THE FORM OF A FRACTION, F(X) = P(X) / Q(X), IN WHICH BOTH P(X)AND Q(X) ARE POLYNOMIALS, THEN WE FOLLOW THESE TWO STEPS:

- 1. FACTOR BOTH THE NUMERATOR (TOP) AND DENOMINATOR (BOTTOM). THIS IS VERY IMPORTANT BECAUSE IF ANY FACTORS END UP CANCELING, THEN THEY WOULD NOT CONTRIBUTE ANY VERTICAL ASYMPTOTES.
- 2. ONCE YOUR RATIONAL FUNCTION IS COMPLETELY REDUCED, LOOK AT THE FACTORS IN THE DENOMINATOR. IF THERE IS A FACTOR INVOLVING (X R), THEN X = R IS A POSSIBLE ASYMPTOTE. IF THERE IS A FACTOR INVOLVING (X + R), THEN X = -R IS A POSSIBLE ASYMPTOTE. NOTE HOW THE SIGN SEEMS TO BE OPPOSITE BOTH TIMES (JUST LIKE SOLVING A FACTOREO POLYNOMIAL THAT HAS BEEN SET EQUAL TO ZERO).
- 3. TAKE EACH "POSSIBLE ASYMPTOTE" AND CHECK IF A LIMIT EXISTS AT THAT POINT IN THE $\lim_{\text{GRAPH, THIS MEANS A CANNOT OBEY}}\lim_{\infty^-\to a}\text{RND }_{\infty^+\to a}$
- 4. TO FIND THE HORIZONTAL ASSIMPTOTE SET $x \to \infty$ FOR SOUR FUNCTION

Asymptote

$$\frac{4x}{x^2+1} = y$$

No x statistions (ould be assumed from the national function.

Also domain is $x \in \mathbb{R}$ so no vertical asymptote.

horizontal assymptote

$$\lim_{x \to \infty} \frac{4x}{x^2+1} = y$$

$$\lim_{x \to \infty} \frac{4x}{x^2} = \frac{4}{x^2} = \frac{4}{x^2} = 0 = y$$

horizontal asymptote
$$y = 0$$