

IN THIS STEP WE FIND THE CONCAVITY OF THE GRAPH.

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HERE WE FIND THE INFLECTION POINTS AND WHERE THE GRAPH CONCAVES UP AND DOWN.

-TO FIND THE INFLECTION POINTS OF THE GRAPH WE NEED TO SOLVE FOR

$$f(x)'' = 0;$$

-NEXT WE FIND WHERE THE GRAPH IS CONCAVE UP AND DOWN ---->

-IF THE $f(x)'' > 0$ THEN THERE IS A CONCAVE UP

-IF THE $f(x)'' < 0$ THEN THERE IS A CONCAVE DOWN

Second Derivative:

$$f''(x) = 60x^3 - 30x = 30x(2x^2 - 1)$$

$$f''(x) = 0 \Rightarrow x = 0 \text{ or } x = \pm 1/\sqrt{2}$$

$$f(0) = 0, \quad f(-1/\sqrt{2}) = (-1/\sqrt{2})^3 [3(1/2) - 5] = 7\sqrt{2}/8 \cong 1.24$$

$$f(1/\sqrt{2}) = -7\sqrt{2}/8 \cong -1.24$$

x		$-1/\sqrt{2}$		0		$1/\sqrt{2}$	
$f(x)$	\cap	$7\sqrt{2}/8$	\cup	0	\cap	$-7\sqrt{2}/8$	\pm
$f''(x)$	$-$	0	$+$	0	$-$	0	\pm

$(-1/\sqrt{2}, 7\sqrt{2}/8)$ and $(1/\sqrt{2}, -7\sqrt{2}/8)$ are points of inflection.