Day 6: Panel Data Models

Panel Data

Panels are a hybrid data structure that lives between the traditional data structures of microeconomics and forecasting.

- Contains observations of multiple individuals
 - Similar to standard cross-sectional data
- Contains multiple observations of each individual
 - Makes the data a collection of [possibly multivariate] time series data

Panel Data

Forecasting algorithms like ARIMA models and GAMs cannot cope with this kind of data structure

- How do we difference out a time series when we have multiple observations (of different individuals) in any given period?
- How do we control for unobservable or unmeasurable differences between individuals?

Panel Data

Panel data allows us to generalize much of what we can learn through time series analysis

- We can generalize the effect of covariates to more than one individual
- We can make forecasts for different groups simultaneously from the same model

$$y_{it} = lpha_{it} + X_{it}eta + \epsilon_{it}$$

i: individual index, t: time index

We might start with the model above, but we wouldn't get far.

 We have insufficient information to calculate the model!

$$\circ K + NT > NT$$

$$y_{it} = lpha + X_{it}eta + \epsilon_{it}$$

If we remove the individual-level intercepts, we can remedy our information problem.

ullet Now, so long as we choose a reasonable number of covariates, K < N

$$y_{it} = lpha + X_{it}eta + \epsilon_{it}$$

Unfortunately, panel data means that we have correlated error terms within individuals.

There is no good reason to believe

$$corr(y_{it},y_{it+1})=0$$

 This is the same problem we saw with ARIMA models, but holds for each individual in our panel

$$y_{it} = lpha + X_{it}eta + \epsilon_{it}$$

We need to decompose our error terms so that

$$\epsilon_{it} = \mu_i +
u_{it}$$

where μ_i is an individual **fixed effect**, and ν_{it} is the noise term.

$$y_{it} = lpha + X_{it}eta + \mu_i +
u_{it}$$

Our model now has K+N parameters, and NT degrees of freedom.

ullet So long as K+N < NT, we can now solve our model!

$$y_{it} = lpha + X_{it}eta + \mu_i +
u_{it}$$

The model can actually be solved using a modified form of OLS.

$$egin{aligned} y_{it} &= lpha + X_{it}eta + \mu_i +
u_{it} \ &\downarrow \ y_{it} - ar{y}_i &= (X_{it} - ar{X}_i)eta +
u_{it} - ar{
u}_i \ &\downarrow \ &\downarrow \ &\ddot{y}_{it} &= \ddot{X}_{it}eta + \ddot{
u}_{it} \end{aligned}$$

$$\ddot{y}_{it} = \ddot{X}_{it}eta + \ddot{
u}_{it}$$

In effect, we difference each observation by subtracting the average values for a given individual over time, causing the intercept terms and individual fixed effects to be differenced out of the model.

$$ar{X}_i = rac{1}{T} \sum_{t=1}^T X_{it}$$

Robust Standard Errors

When we use panel data, we must consider that the variance in predictive power will vary by individual (some are more noisy than others)

- We can't just use standard OLS error functions
- Need to correct for the differences in variance between individuals

Robust Standard Errors

$$Var(eta) = \sigma^2(X'X)^{-1}(X'\Omega X)(X'X)^{-1}$$

but we can't know Ω . Instead, we need to estimate it.

- 1. Use OLS to estimate the model.
- 2. From OLS estimates, use the squared residuals to generate $\hat{\Sigma}$, an estimate of $\sigma^2\Omega$
- 3. Estimate Var(eta) as

$$(X'X)^{-1}(X'\hat{\Sigma}X)(X'X)^{-1}$$

First, we import the formula module from statsmodels, so that we can use formulas in our model without patsy (and save a few lines of code)

We can now explore our results, the effects of included variables, and what our forecasts might look like.

```
# Store predictions and truth
pred = fit.predict(data[data.YEAR==1954])
truth = data.loc[data.YEAR==1954, "I_"]
# Store errors
errors = pred - truth
# Calculate Absolute Percentage Error
pce = np.abs(errors/truth)*100
```

We need to perform the calculations that will provide us with information on how well we do at predicting out of sample with our current panel.

```
Mean Squared Error: 13288.423957448418

Mean Absolute Error: 77.27884184438867

Mean Absolute Percentage Error: 58.253213431705774
```

Yikes! It looks like we need more information...

For Lab Today:

We will look at how well we can forecast <u>student's</u> grades based on information about their study habits, social patterns, and family situation.

In your teams, develop a model for the data contained in continuous Train.csv that will allow you to forecast a student's final grade (G3).

Then, use the model that you have built to forecast the grades for the student data contained in continuousTest.csv.