

## 4.1

根据所给数据，对偶问题是

$$\begin{aligned}
 L(\alpha) &= \min_{\alpha} \frac{1}{2} \sum_{i=1}^N \sum_{j=1}^N \alpha_i \alpha_j y_i y_j (x_i \cdot x_j) - \sum_{i=1}^N \alpha_i \\
 &= \frac{1}{2} (5\alpha_1^2 + 13\alpha_2^2 + 18\alpha_3^2 + 5\alpha_4^2 + 13\alpha_5^2 \\
 &\quad + 16\alpha_1\alpha_2 + 18\alpha_1\alpha_3 - 8\alpha_1\alpha_4 - 14\alpha_1\alpha_5 + 30\alpha_2\alpha_3 - 14\alpha_2\alpha_4 - 24\alpha_2\alpha_5 - 18\alpha_3\alpha_4 - 30\alpha_3\alpha_5 + 16\alpha_4\alpha_5 \\
 &\quad - \alpha_1 - \alpha_2 - \alpha_3 - \alpha_4 - \alpha_5) \\
 s.t. \quad &\alpha_1 + \alpha_2 + \alpha_3 - \alpha_4 - \alpha_5 = 0
 \end{aligned}$$

由

$$\begin{aligned}
 \frac{\nabla L(\alpha)}{\nabla \alpha_1} &= 0 \\
 \frac{\nabla L(\alpha)}{\nabla \alpha_2} &= 0 \\
 \frac{\nabla L(\alpha)}{\nabla \alpha_3} &= 0 \\
 \frac{\nabla L(\alpha)}{\nabla \alpha_4} &= 0 \\
 \frac{\nabla L(\alpha)}{\nabla \alpha_5} &= 0
 \end{aligned}$$

且

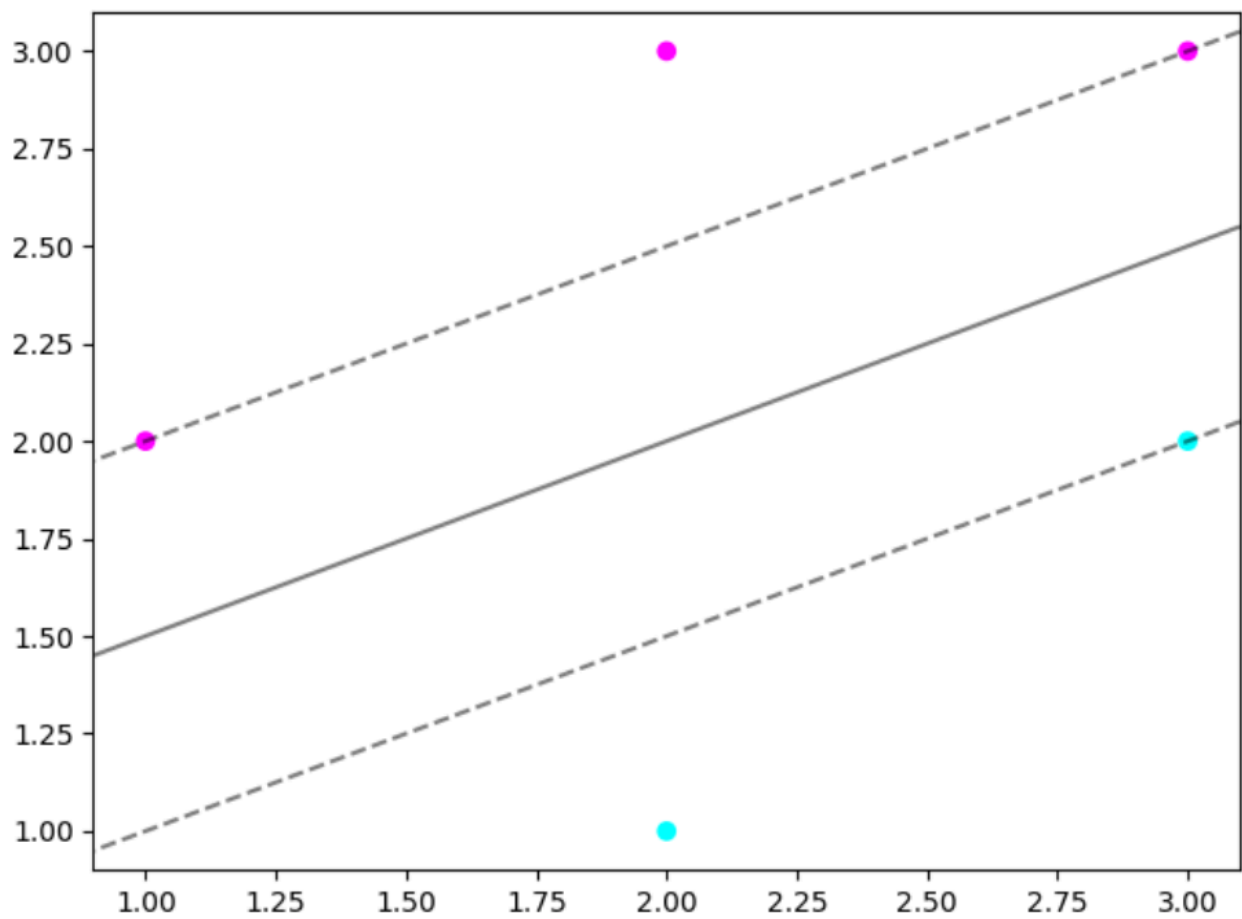
$$w^* = \sum_i \alpha_i^* y_i x_i, b^* = y_j - \sum_{i=1}^N \alpha_i^* y_i (x_i \cdot x_j)$$

求解得

$$w^* = [-1, 2], b^* = -2$$

所以超平面为  $-x_1 + 2x_2 - 2 = 0$ ，分类决策函数为  $f(x) = \text{sign}(-x_1 + 2x_2 - 2)$

图为



## 4.2

A,C

## 4.3

1.No

2.False

## 4.4

C,D

## 4.5

A,C,D

## **4.6**

B

## **4.7**

D

## **4.8**

B

## **4.9**

A,B