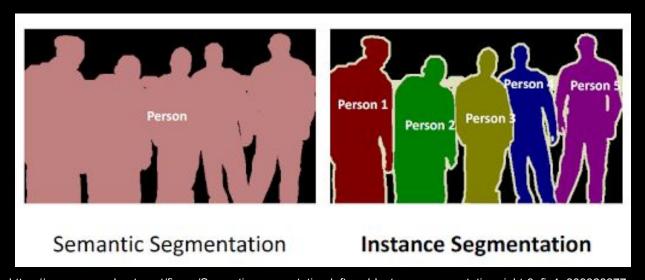
EQUIVARIANT DEEP LEARNING FOR HISTOPATHOLOGY IMAGE SEGMENTATION

Josef Liem 2025

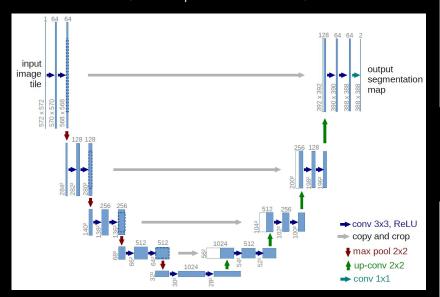
Segmentation



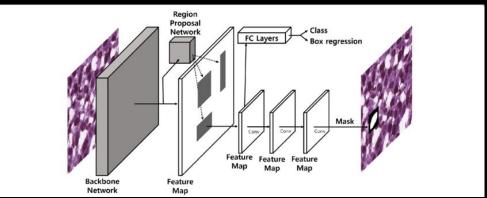
https://www.researchgate.net/figure/Semantic-segmentation-left-and-Instance-segmentation-right-8_fig1_339328277

- Pixel-wise classification ≈ Segmentation
- Achievable w/ autoencoder or autoencoder-like architectures

U-Net: An Autoencoder-like Architecture (w/ Skip Connections)



Mask-RCNN: Extension of Fast-RCNN Region Proposal Network



https://www.researchgate.net/figure/The-overall-network-architecture-of-Mask-R-CNN_fig 1 336615317

DeepLab V1,2,3+: Dilated Convolution for Large Scale Context and Spatial Resolution

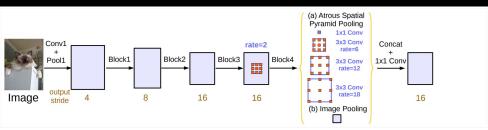


Figure 5. Parallel modules with atrous convolution (ASPP), augmented with image-level features.

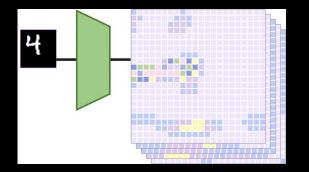
https://paperswithcode.com/method/deeplabv3

Equivariance

• We have learned in class (implicitly) that convolution is translationally equivariant:

"shift of position in input image = shift at output of convolution layer" (roughly speaking)

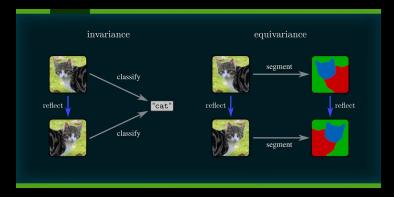
Not true for other transformations: rotations/reflections/etc...



Equivariance: f(T(x))=T(f(x)) for all x

Invariance: f(T(x))=f(x) for all x

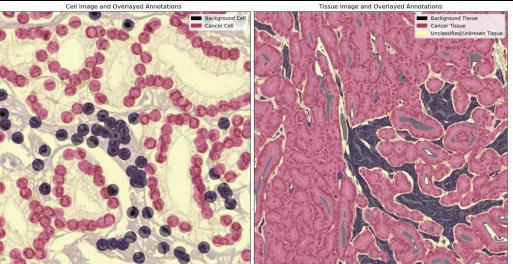
(Invariance is just equivariance under the identity)

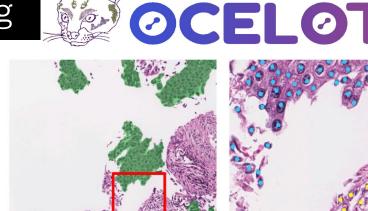


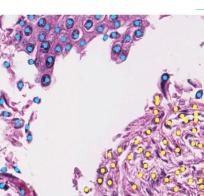
An easy read on equivariance:

https://maurice-weiler.gitlab.io/blog_post/cnn-book_1_equivariant_networks/

Motivation: Medical Imaging







 (x_s, y_s^c)

Overlapped Cell On Tissue Dataset for Histopathology MICCAI202

Dataset size per organ and data subset

The state of the s						
Organs	# Slides			# Patch Pairs		
	Train	Val	Test	Train	Val	Test
Bladder	35	14	14	82	29	26
Endometrium	38	13	13	86	29	25
Head-and-neck	13	5	6	27	9	10
Kidney	47	15	18	122	41	41
Prostate	25	12	10	47	17	16
Stomach	15	6	5	36	12	12
Total	173	65	66	400	137	130

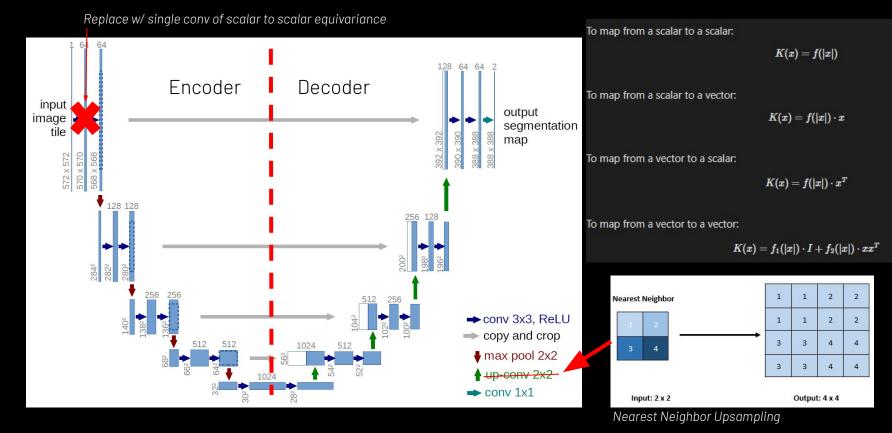
Core problem:

How can we use large FOV context to improve smaller FOV classification?

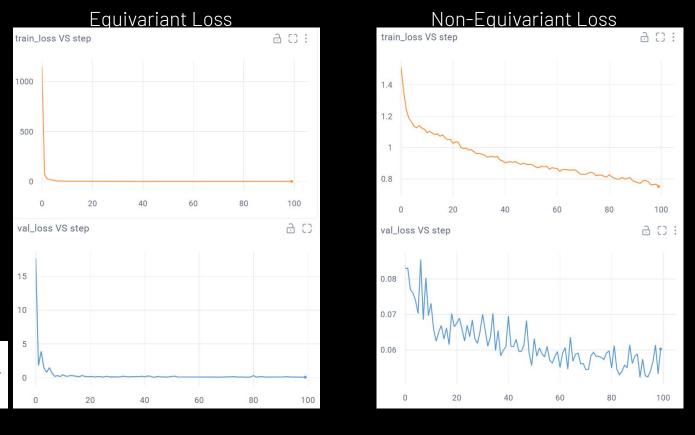
Symmetries are evident on a cellular and tissue level. How can we take advantage of these symmetries?

We have limited medical data, and data augmentation will only get us so far... Equivariance?

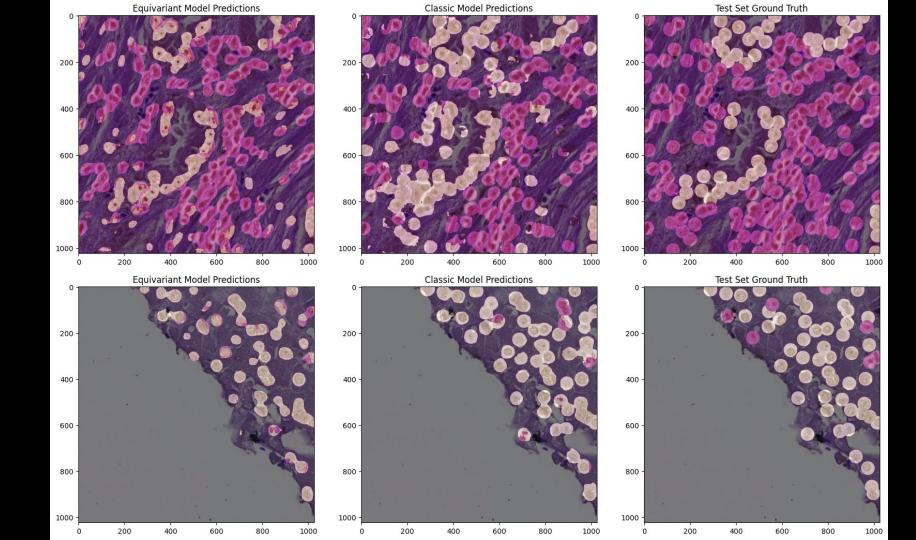
Proposed solution: Use equivariant convolution to improve segmentation of histopathology slides, potentially in place of heavy data augmentation. Compare against the non-equivariant equivalent with data augmentation.

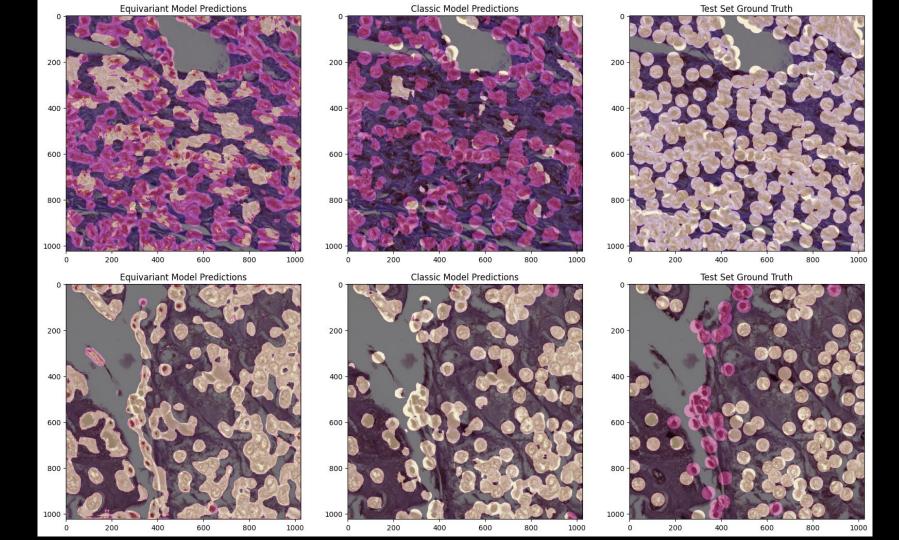


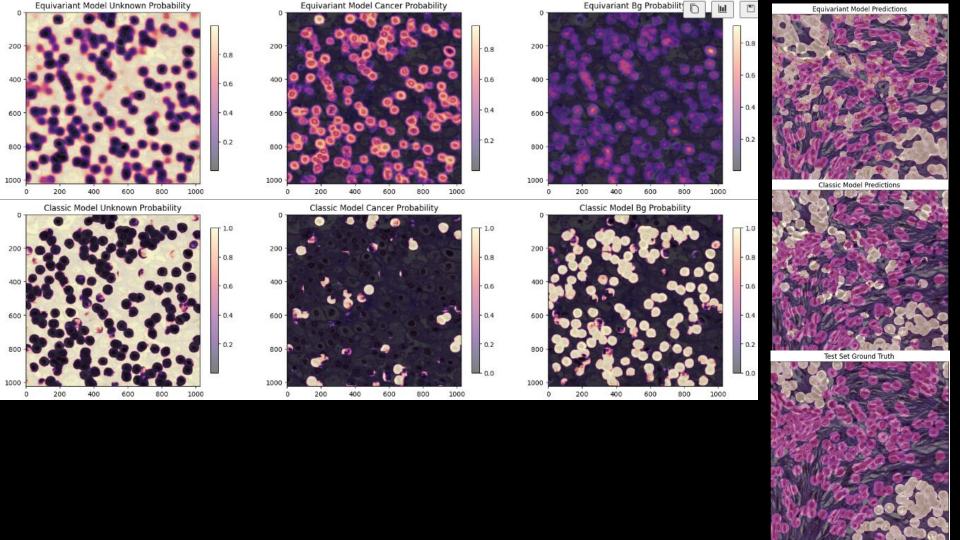
Dice Cross Entropy Loss



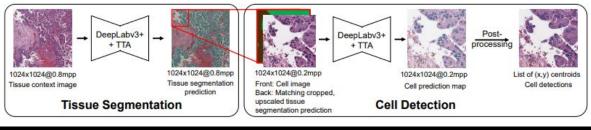
Equivariant Model Loss: 1.1681814392407734 Classic Model Loss: 2.2941786273131295 Equivariant Model Dice Score: 0.6273064613342285 Classic Model Dice Score: 0.6840800642967224







Takeaways



SoftCTM

- Many building blocks, but how do we put them together?
- Potential to expand on tissue/cell patch pair problem
- Consider a combination of data augmentation AND equivariance?
- Good data his hard to come by in certain domains

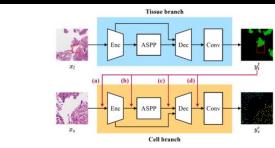
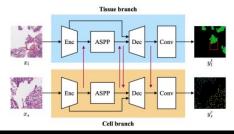


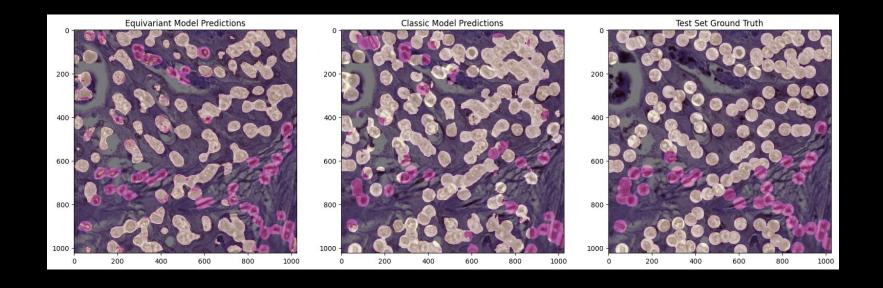
Figure 2.3.: Tissue prediction injection models. (Figure taken from Ryu et al. [2023]).

Cell-Tissue feature sharing model

To introduce greater diversity and flexibility in the flow of cell-tissue information, the OCELOT team developed an additional set of models for cell-tissue feature sharing. These models enable information exchange between the cell detection model and the tissue segmentation model at various feature representation levels in each network. This approach allows for fluid and dynamic information sharing between the two models. The resulting best model is illustrated in Figure 2.4.



THANK YOU



There are many ways (representations) for achieving equivariance. Some representations allow for equivariance to more group actions, but sometimes at a high cost (training & compute)...



On Invariance, Equivariance, Correlation and Convolution of Spherical Harmonic Representations for Scalar and Vectorial Data. Janis Keuper keuper@imla.ai1,2 ¹Institute for Machine Learning and Analytics (IMLA), Offenburg University ²CC-HPC, Fraunhofer ITWM, Kaiserslautern July 10, 2023

POLAR TRANSFORMER NETWORKS

Carlos Esteves, Christine Allen-Blanchette, Xiaowei Zhou, Kostas Daniilidis GRASP Laboratory, University of Pennsylvania

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Neural Fourier Transform: A General Approach to Equivariant Representation Learning

Masanori Koyama, Kenji Fukumizu, Kohei Hayashi, Takeru Miyato

^{*}I won't be able to tell you how some of these other representations work... Please don't ask...