#### Problem 1B

```
# Save the data
X = diabetes.data
X_transpose = X.T
y = diabetes.target

# Closed form solution
X_transpose_X = np.dot(X_transpose, X) # https://numpy.org/doc/stable/reference/generated/numpy.dot.html
X_transpose_X_inv = np.linalg.inv(X_transpose_X) # https://numpy.org/doc/stable/reference/routines.linalg.html
X_transpose_y = np.dot(X_transpose, y)
w_star = np.dot(X_transpose_X_inv, X_transpose_y)
```

### Problem 1C

```
# Linear solver
from sklearn.linear_model import LinearRegression

# Load data and fit to model, extract w_star: https://scikit-learn.org/stable/modules/generated/sklearn.linear_model.LinearRegression.html
diabetes = load_diabetes()
X = diabetes.data
y = diabetes.target
regressionModel = LinearRegression()
regressionModel.fit(X, y)
w_star_solver = regressionModel.coef_
```

# Sanity Check

```
# https://stackoverflow.com/questions/10580676/comparing-two-numpy-arrays-for-equality-element-wise assert np.allclose(w_star, w_star_solver), "Numpy arrays are not close elementwise to one another"

# Closed form print("My solution: ") print(w_star)

# Sklearn solver print("\nSklearn: ") print(w_star_solver)

# y solution: [ -10.0098663 -239.81564367 519.84592005 324.3846455 -792.17563855 476.73902101 101.04326794 177.06323767 751.27369956 67.62669218]

Sklearn: [ -10.0098663 -239.81564367 519.84592005 324.3846455 -792.17563855 476.73902101 101.04326794 177.06323767 751.27369956 67.62669218]
```

### Problem 2C

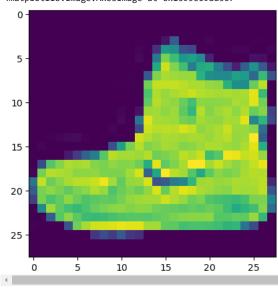
```
from sklearn.linear_model import LogisticRegression
from sklearn.datasets import load_wine
from sklearn.datasets import load_iris
from sklearn.model_selection import train_test_split
# Load dataset
X, y = load_wine(return_X_y=True)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2)
# Fit our model
model = LogisticRegression()
model.fit(X_train, y_train)
🚁 c:\Users\liemj\anaconda3\envs\ASLenv\Lib\site-packages\sklearn\linear_model\_logistic.py:460: ConvergenceWarning: lbfgs failed to conver
    STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
    Increase the number of iterations (max_iter) or scale the data as shown in:
        https://scikit-learn.org/stable/modules/preprocessing.html
    Please also refer to the documentation for alternative solver options:
        https://scikit-learn.org/stable/modules/linear_model.html#logistic-regression
      n_iter_i = _check_optimize_result(
     ▼ LogisticRegression
     LogisticRegression()
y_true = y_test
y_pred = model.predict(X_test)
print("Model coef: ")
print(model.coef_)
print("\nGround truth: ")
print(y_true)
print("\nPredicted")
print(y_pred)

→ Model coef:
     [[-1.71720584e-02 1.49617205e-01 1.25232870e-01 -2.25825380e-01
      -3.19189734e-02 1.80023530e-01 4.02454060e-01 -1.80556348e-02
       7.23346435e-02 -2.19815151e-02 1.60663612e-02 3.03674641e-01
       7.74886272e-031
     [ 3.97803158e-01 -5.70976516e-01 -1.05541699e-01 1.42490944e-01
       1.56126453e-02 2.92111209e-01 4.43766844e-01 3.16179559e-02
       3.16850041e-01 -1.10306732e+00 2.17536302e-01 4.11674292e-01
      -8.07889407e-03]
     [-3.80631099e-01 4.21359311e-01 -1.96911709e-02 8.33344361e-02
       1.63063281e-02 -4.72134739e-01 -8.46220904e-01 -1.35623212e-02
      -3.89184685e-01 1.12504884e+00 -2.33602663e-01 -7.15348933e-01
       3.30031346e-04]]
    Ground truth:
```

#### Problem 3A

```
import torchvision
import torch
import matplotlib.pyplot as plt
from sklearn.model_selection import train_test_split
from torch.utils.data import DataLoader
from torch.utils.data import TensorDataset

# Download and load the data
data = torchvision.datasets.FashionMNIST('./FashionMNIST', train=True, download=True, transform=torchvision.transforms.ToTensor())
```



```
train_length = int(0.8 * len(data))
test_length = int(0.2 * len(data))

# Prepare into dataloader
train_dataset, test_dataset = torch.utils.data.random_split(data, (train_length, test_length))
train_loader = DataLoader(train_dataset, batch_size=32, shuffle=True)
test_loader = DataLoader(test_dataset, batch_size=32)
```

### Problem 3B

```
from torch.nn import Module
from torch.nn import CrossEntropyLoss
from torch.optim import SGD
from torch.nn import Linear
from torch.nn import ReLU
from torch.nn import Sequential
from tqdm import tqdm
class JosefNet(Module):
 def __init__(self, inshape=(28, 28), num_classes=10):
   super(JosefNet, self).__init__()
   self.inshape = inshape
   input_size = self.inshape[0] * self.inshape[1]
   self.layer1 = self.JosefLayer(input_size, input_size + 10)
   self.layer2 = self.JosefLayer(input_size + 10, input_size + 20)
   self.layer3 = self.JosefLayer(input_size + 20, input_size + 10)
   self.layer4 = Linear(input_size + 10, num_classes)
 def JosefLayer(self, in_channels, out_channels):
   layer = Sequential(
        Linear(in_channels, out_channels),
        ReLU(),
   return layer
 def forward(self, x):
   x = x.view(-1, self.inshape[0] * self.inshape[1])
```

```
x = self.layer1(x)
    x = self.layer2(x)
    x = self.layer3(x)
    x = self.layer4(x)
    return x
# 1. Model 2. Loss 3. Optimization
model = JosefNet(inshape=(28, 28), num_classes=10)
criterion = CrossEntropyLoss()
optimizer = SGD(model.parameters(), lr=0.01)
device = torch.device('cuda' if torch.cuda.is_available() else 'cpu')
print(f'Using {device}...')
model = model.to(device)
→ Using cpu...
n_{epochs} = 10
train losses = []
test_losses = []
for epoch in range(n_epochs):
 train_loss = 0
 test_loss = 0
 model.train()
  for imgs, lbls in tqdm(train_loader, desc=f"Epoch {epoch+1}/{n_epochs} - Training"):
    imgs = imgs.to(device)
    lbls = lbls.to(device)
    # get prediction and calculate training loss on batch
    preds = model(imgs)
    loss = criterion(preds, lbls)
    loss.backward() # Backward pass
    optimizer.step() # Gradient update
    optimizer.zero_grad() \# Zero gradient for next run
    train_loss += loss.item()
  # calculate the loss
  train_loss /= len(train_loader)
  train_losses.append(train_loss)
 model.eval()
  with torch.no_grad():
    # do the same on test data each epoch
    for imgs, lbls in tqdm(test_loader, desc=f"Epoch {epoch+1}/{n_epochs} - Testing"):
     imgs = imgs.to(device)
     lbls = lbls.to(device)
     # get preds and calculate batchwise loss
      preds = model(imgs)
     loss = criterion(preds, lbls)
      test_loss += loss.item()
    # Calculate test loss
    test_loss /= len(test_loader)
    test_losses.append(test_loss)
  print(f'Training Loss: {train_loss} \t Test Loss: {test_loss}')
Epoch 1/10 - Training: 100%| 1500/1500 [00:12<00:00, 115.80it/s]
     Epoch 1/10 - Testing: 100%
                                      375/375 [00:01<00:00, 199.58it/s]
     Training Loss: 1.2783720241983731
                                              Test Loss: 0.7180028606255849
     Epoch 2/10 - Training: 100%
                                          | 1500/1500 [00:12<00:00, 120.83it/s]
     Epoch 2/10 - Testing: 100%
                                           375/375 [00:01<00:00, 202.13it/s]
     Training Loss: 0.6391100450754166
                                              Test Loss: 0.5531621694564819
     Epoch 3/10 - Training: 100%
                                            1500/1500 [00:12<00:00, 120.18it/s]
     Epoch 3/10 - Testing: 100%|
                                           375/375 [00:01<00:00, 202.75it/s]
     Training Loss: 0.535347327152888
                                              Test Loss: 0.5120111543337504
     Epoch 4/10 - Training: 100%
                                          | 1500/1500 [00:12<00:00, 119.75it/s]
     Epoch 4/10 - Testing: 100%
                                           375/375 [00:01<00:00, 206,03it/s]
     Training Loss: 0.4817542056838671
                                              Test Loss: 0.48389638829231263
     Epoch 5/10 - Training: 100%
                                            1500/1500 [00:12<00:00, 120.13it/s]
     Epoch 5/10 - Testing: 100%
                                     375/375 [00:02<00:00, 185.58it/s]
```

```
Test Loss: 0.4513076793750127
Training Loss: 0.4507949015696843
                                       1500/1500 [00:12<00:00, 119.91it/s]
Epoch 6/10 - Training: 100%
Epoch 6/10 - Testing: 100%
                                      375/375 [00:01<00:00, 199.35it/s]
Training Loss: 0.4271812918086847
                                         Test Loss: 0.4186215761701266
Epoch 7/10 - Training: 100%
                                       1500/1500 [00:12<00:00, 121.31it/s]
Epoch 7/10 - Testing: 100%
                                       375/375 [00:01<00:00, 201.48it/s]
                                         Test Loss: 0.398398036022981
Training Loss: 0.40905945078035194
Epoch 8/10 - Training: 100%
                                       1500/1500 [00:12<00:00, 120.33it/s]
Epoch 8/10 - Testing: 100%
                                      375/375 [00:01<00:00, 200.26it/s]
Training Loss: 0.39271588702499866
                                         Test Loss: 0.3925811664263407
Epoch 9/10 - Training: 100%
                                       1500/1500 [00:12<00:00, 120.47it/s]
Epoch 9/10 - Testing: 100%
                                      375/375 [00:01<00:00, 202.14it/s]
Training Loss: 0.3788658427745104
                                         Test Loss: 0.37457411682605746
Epoch 10/10 - Training: 100%
                                        1500/1500 [00:12<00:00, 119.54it/s]
Epoch 10/10 - Testing: 100%|
                                       375/375 [00:01<00:00, 204.16it/s]Training Loss: 0.3653795603265365
                                                                                                                 Test Loss: 0.3734455082
```

### Problem 3C

₹

```
#plot the losses
plt.plot(train_losses, label='Training loss')
plt.plot(test_losses, label='Testing loss')
plt.xlabel('Epoch')
plt.ylabel('Loss')
plt.title('Training and Testing Loss')
plt.legend()
plt.show()
```



```
# sample prediction
model.eval()
sample_img, sample_lbl = test_dataset[1]
sample_img = sample_img.to(device)

with torch.no_grad():
    sample_pred = model(sample_img.unsqueeze(0))
    sample_pred = torch.argmax(sample_pred, dim=1)

print(f'Predicted: {sample_pred.item()} \t Ground Truth: {sample_lbl}')
plt.imshow(sample_img.squeeze().cpu().numpy())
```

```
Predicted: 8 Ground Truth: 8 (matplotlib.image.AxesImage at 0x16959d62e10)
```

```
# accuracy
correct = 0
total = 0
model.eval()

with torch.no_grad():
    for imgs, lbls in test_loader:
        imgs = imgs.to(device)
        lbls = lbls.to(device)

        preds = model(imgs)
        preds = torch.argmax(preds, dim=1)

        total += lbls.size(0)
        correct += (preds == lbls).sum().item()

print(f'Accuracy: {correct/total * 100}%')

Accuracy: 86.908333333333333%
```

Training loss and testing losss are relatively comparable in my training process, thus it seems like it isn't really over or underfitting. That said, an accuracy of 87% can be improved some more. Tweaking with the number of channels and observing consequent performance indicates it is likely a problem of too large a number of parameters for a rather simple dataset.

### Problem 4A

```
import torchvision
import torch
import matplotlib.pyplot as plt
from sklearn.model_selection import train_test_split
from torch.utils.data import DataLoader
from torch.utils.data import TensorDataset
from torch.nn import Module
from torch.nn import CrossEntropyLoss
from torch.optim import SGD
from torch.nn import Linear
from torch.nn import ReLU
from torch.nn import Sequential
from tqdm import tqdm
import numpy as np
class JosefNet(Module):
 def __init__(self, inshape=(28, 28), num_classes=10):
   super(JosefNet, self).__init__()
   self.inshape = inshape
```

```
input_size = self.inshape[0] * self.inshape[1]
    self.layer1 = self.JosefLayer(input_size, input_size + 24)
    self.layer2 = self.JosefLayer(input_size + 24, input_size + 16)
    self.layer3 = Linear(input_size + 16, num_classes)
  def JosefLayer(self, in_channels, out_channels):
    layer = Sequential(
        Linear(in_channels, out_channels),
        ReLU(),
    return layer
 def forward(self, x):
    x = x.view(-1, self.inshape[0] * self.inshape[1])
    x = self.layer1(x)
    x = self.layer2(x)
    x = self.layer3(x)
    return x
# Download and load the data
data = torchvision.datasets.FashionMNIST('./FashionMNIST', train=True, download=True, transform=torchvision.transforms.ToTensor())
train_length = int(0.8 * len(data))
test_length = int(0.2 * len(data))
# Prepare a subsample into dataloader
train_dataset, test_dataset = torch.utils.data.random_split(data, (train_length, test_length))
subsampled_train_dataset = torch.utils.data.Subset(train_dataset, range(25000))
sample_train_loader = DataLoader(subsampled_train_dataset, batch_size=32, shuffle=True)
test_loader = DataLoader(test_dataset, batch_size=32)
# What is the size of our subsample?
print(f"Shape of subsample training data: {len(sample_train_loader.dataset)}")
Shape of subsample training data: 25000
```

#### Problem 4B

```
def train_benchmarker(optimizer, model, n_epochs = 10):
 criterion = CrossEntropyLoss()
 # Move model to device
 device = torch.device('cuda' if torch.cuda.is_available() else 'cpu')
 model = model.to(device)
 # Track losses over epochs
 train_losses = []
 test_losses = []
  for epoch in range(n_epochs):
   train_loss = 0
   test_loss = 0
   model.train()
   for imgs, lbls in tqdm(sample train loader, desc=f"Epoch {epoch+1}/{n epochs} - Training"):
      imgs = imgs.to(device)
      lbls = lbls.to(device)
      \ensuremath{\text{\#}} get prediction and calculate training loss on batch
      preds = model(imgs)
      loss = criterion(preds, lbls)
      loss.backward() # Backward pass
      optimizer.step() # Gradient update
      {\tt optimizer.zero\_grad()} \ {\tt \# Zero \ gradient \ for \ next \ run}
      train_loss += loss.item()
   # calculate the loss
   train_loss /= len(train_loader)
   train losses.append(train loss)
```

```
model.eval()
with torch.no_grad():
    # do the same on test data each epoch
    for imgs, lbls in tqdm(test_loader, desc=f"Epoch {epoch+1}/{n_epochs} - Testing"):
    imgs = imgs.to(device)
    lbls = lbls.to(device)

    # get preds and calculate batchwise loss
    preds = model(imgs)
    loss = criterion(preds, lbls)

    test_loss += loss.item()

# Calculate test loss
    test_loss /= len(test_loader)
    test_losses.append(test_loss)

print(f'Training Loss: {train_loss} \t Test Loss: {test_loss}')
return (train_losses, test_losses)
```

## Problem 4C

```
# SGD optim
n_epochs = 10
SGD_test_losses = []

for i in range(5):
    model = JosefNet(inshape=(28, 28), num_classes=10)
    optimizer = torch.optim.SGD(model.parameters(), lr=0.01)
    _, SGD_test_loss = train_benchmarker(optimizer, model, n_epochs=n_epochs)
    SGD_test_losses.append(SGD_test_loss)
```

```
Test Loss: 0.491/924040913/825
     iraining LOSS: 0.251320/143346468/
                                          | 782/782 [00:09<00:00, 84.93it/s]
     Epoch 7/10 - Training: 100%
     Epoch 7/10 - Testing: 100%
                                          | 375/375 [00:02<00:00, 140.96it/s]
     Training Loss: 0.2427383978466193
                                              Test Loss: 0.49242932720979055
    Epoch 8/10 - Training: 100%|
Epoch 8/10 - Testing: 100%|
                                             782/782 [00:09<00:00, 82.12it/s]
                                            375/375 [00:02<00:00, 148.17it/s]
     Training Loss: 0.23422922939062119
                                              Test Loss: 0.46829562246799467
                                             782/782 [00:09<00:00, 83.02it/s]
     Epoch 9/10 - Training: 100%
     Epoch 9/10 - Testing: 100%
                                            375/375 [00:02<00:00, 144.48it/s]
     Training Loss: 0.22837601993481318
                                              Test Loss: 0.4565233874320984
     Epoch 10/10 - Training: 100%
                                              782/782 [00:10<00:00, 77.86it/s]
     Epoch 10/10 - Testing: 100%
                                           | 375/375 [00:02<00:00, 145.13it/s]Training Loss: 0.2224973182529211
                                                                                                                       Test Loss: 0.4492346:
# Calculate average test losses
average_SGD_test_losses = np.mean(SGD_test_losses, axis=0)
# Adam optim
n_{epochs} = 10
Adam_test_losses = []
for i in range(5):
 model = JosefNet(inshape=(28, 28), num_classes=10)
 optimizer = torch.optim.Adam(model.parameters(), lr=0.01)
 _, Adam_test_loss = train_benchmarker(optimizer, model, n_epochs=n_epochs)
 Adam_test_losses.append(Adam_test_loss)
₹
```

```
Epocn 10/10 - Iraining: 100%|■
                                           | /82//82 | WU:31<WU:WU, Z5.191T/S
                                         375/375 [00:02<00:00, 134.70it/s]Training Loss: 0.2116421319829921
                                                                                                                      Test Loss: 0.46040644
    Epoch 10/10 - Testing: 100%
# Calculate average test losses
average_Adam_test_losses = np.mean(Adam_test_losses, axis=0)
# Adam optim
n_epochs = 10
RMS_test_losses = []
for i in range(5):
 model = JosefNet(inshape=(28, 28), num_classes=10)
 optimizer = torch.optim.RMSprop(model.parameters(), lr=0.01)
  _, RMS_test_loss = train_benchmarker(optimizer, model, n_epochs=n_epochs)
 RMS test losses.append(RMS test loss)
    Training Loss: 3.16783631447951
                                              Test Loss: 0.6961359899044037
    Epoch 2/10 - Training: 100%
                                            782/782 [00:15<00:00, 51.20it/s]
    Epoch 2/10 - Testing: 100%
                                            375/375 [00:02<00:00, 142.39it/s]
    Training Loss: 0.32685648160551983
                                              Test Loss: 0.6004725130796432
    Epoch 3/10 - Training: 100%|
                                            782/782 [00:15<00:00, 51.12it/s]
    Epoch 3/10 - Testing: 100%
                                            375/375 [00:02<00:00, 143.30it/s]
    Training Loss: 0.3055389421880245
                                              Test Loss: 1.0797079923152924
    Epoch 4/10 - Training: 100%|
                                            782/782 [00:15<00:00, 51.57it/s]
    Epoch 4/10 - Testing: 100%
                                            375/375 [00:04<00:00, 93.30it/s]
    Training Loss: 0.32157494181394575
                                              Test Loss: 0.8298569944699605
    Epoch 5/10 - Training: 100%
                                            782/782 [00:15<00:00, 50.27it/s]
    Epoch 5/10 - Testing: 100%
                                            375/375 [00:02<00:00, 142.55it/s]
    Training Loss: 0.2914831153303385
                                              Test Loss: 0.5993122043609619
    Epoch 6/10 - Training: 100%
                                            782/782 [00:19<00:00, 40.77it/s]
    Epoch 6/10 - Testing: 100%
                                            375/375 [00:03<00:00, 98.49it/s]
    Training Loss: 0.27585549017290273
                                              Test Loss: 0.5378888872861862
    Epoch 7/10 - Training: 100%
                                            782/782 [00:25<00:00, 30.60it/s]
    Epoch 7/10 - Testing: 100%
                                            375/375 [00:02<00:00, 128.60it/s]
    Training Loss: 0.2719623350203037
                                              Test Loss: 0.5339740462700526
    Epoch 8/10 - Training: 100%
                                             782/782 [00:30<00:00, 25.49it/s]
    Epoch 8/10 - Testing: 100%
                                            375/375 [00:02<00:00, 137.03it/s]
    Training Loss: 0.2664204407334328
                                              Test Loss: 0.5773544978300731
                                            782/782 [00:41<00:00, 18.88it/s]
    Epoch 9/10 - Training: 100%
    Epoch 9/10 - Testing: 100%
                                            375/375 [00:03<00:00, 104.37it/s]
    Training Loss: 0.2661888409157594
                                              Test Loss: 0.5212955634991328
                                             782/782 [00:44<00:00, 17.73it/s]
    Epoch 10/10 - Training: 100%
    Epoch 10/10 - Testing: 100%
                                            375/375 [00:02<00:00, 137.36it/s]
    Training Loss: 0.26102608639001845
                                              Test Loss: 0.7628260831038157
    Epoch 1/10 - Training: 100%
                                            782/782 [00:15<00:00, 51.67it/s]
    Epoch 1/10 - Testing: 100%
                                            375/375 [00:02<00:00, 145.47it/s]
    Training Loss: 5.822545525372028
                                              Test Loss: 0.5917075935999553
    Epoch 2/10 - Training: 100%
                                            782/782 [00:15<00:00, 49.36it/s]
    Epoch 2/10 - Testing: 100%
                                            375/375 [00:03<00:00, 119.03it/s]
    Training Loss: 0.29796630357205867
                                              Test Loss: 0.5649822023510933
                                            782/782 [00:15<00:00, 50.65it/s]
    Epoch 3/10 - Training: 100%
    Epoch 3/10 - Testing: 100%
                                            375/375 [00:02<00:00, 143.43it/s]
    Training Loss: 0.27856097034116584
                                              Test Loss: 0.4943006470998128
                                            782/782 [00:15<00:00, 49.97it/s]
    Epoch 4/10 - Training: 100%
    Epoch 4/10 - Testing: 100%
                                            375/375 [00:03<00:00, 121.11it/s]
    Training Loss: 0.27168866800765196
                                              Test Loss: 0.512252598643303
    Epoch 5/10 - Training: 100%
                                            782/782 [00:16<00:00, 46.86it/s]
    Epoch 5/10 - Testing: 100%
                                            375/375 [00:02<00:00, 139.84it/s]
    Training Loss: 0.2668871119270722
                                              Test Loss: 0.5534438116550445
    Epoch 6/10 - Training: 100%
                                            782/782 [00:19<00:00, 40.25it/s]
    Epoch 6/10 - Testing: 100%
                                            375/375 [00:03<00:00, 94.86it/s]
    Training Loss: 0.24255538199841975
                                              Test Loss: 0.5044092157681783
    Epoch 7/10 - Training: 100%|
                                            782/782 [00:25<00:00, 30.78it/s]
    Epoch 7/10 - Testing: 100%
                                            375/375 [00:03<00:00, 120.91it/s]
    Training Loss: 0.23655242166419824
                                              Test Loss: 0.6205205432573955
    Epoch 8/10 - Training: 100%
                                            782/782 [00:31<00:00, 25.13it/s]
    Epoch 8/10 - Testing: 100%
                                            375/375 [00:02<00:00, 138.64it/s]
    Training Loss: 0.23216824392974378
                                              Test Loss: 0.4737894734342893
    Epoch 9/10 - Training: 100%|
                                            782/782 [00:40<00:00, 19.51it/s]
    Epoch 9/10 - Testing: 100%
                                            375/375 [00:03<00:00, 107.57it/s]
    Training Loss: 0.23211938532193502
                                              Test Loss: 0.5611137472391129
    Epoch 10/10 - Training: 100%
                                             782/782 [00:43<00:00, 17,90it/s]
    Epoch 10/10 - Testing: 100%
                                            375/375 [00:02<00:00, 140.28it/s]Training Loss: 0.22849595892926058
                                                                                                                      Test Loss: 0.71767442
```

```
# Calculate average test losses
average_RMS_test_losses = np.mean(RMS_test_losses, axis=0)

plt.plot(average_SGD_test_losses, label='SGD')
plt.plot(average_Adam_test_losses, label='Adam')
plt.plot(average_RMS_test_losses, label='RMSprop')
plt.title('Average Test Loss per Epoch')
plt.xlabel('Epoch')
plt.ylabel('Average Test Loss')
plt.legend()
plt.show()
```



