

Complete_RDD2

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Causal Inference Replication 2

Load data from the RDD2 repository and add additional variables

```
# Create a path to read data from the source
read_data <- function(df)
{
  full_path <- paste("https://raw.githubusercontent.com/Joey-Herrera/Causal_inference/main/RDD2/Data/",
                     df, sep = "")
  df <- read_dta(full_path)
  return(df)
}

nsw_dw <- read_dta("https://raw.githubusercontent.com/Joey-Herrera/Causal_inference/main/RDD2/Data/nsw_mixture.dta")

nsw_dw <- nsw_dw %>%
  filter(treat == 1)

# Append variables as necessary
nsw_lm <- read_dta("https://raw.githubusercontent.com/Joey-Herrera/Causal_inference/main/RDD2/Data/cps_mixture.dta")
bind_rows(nsw_dw) %>%
  mutate(agesq = age^2,
         agecube = age^3,
         educsq = educ*educ,
         educcube = educ^3,
         u74 = case_when(re74 == 0 ~ 1, TRUE ~ 0),
         u75 = case_when(re75 == 0 ~ 1, TRUE ~ 0),
         re74sq = re74^2,
         re74cube = re74^3,
         re75sq = re75^2,
         re75cube = re75^3,
         re78sq = re78^2,
         re75cube = re78^3,
         interaction1 = educ*re74,
         interaction2 = u74*hispan)

nsw_logit <- read_dta("https://raw.githubusercontent.com/Joey-Herrera/Causal_inference/main/RDD2/Data/cps_mixture.dta")
bind_rows(nsw_dw) %>%
  mutate(agesq = age^2,
         agecube = age^3,
         educsq = educ*educ,
         educcube = educ^3,
```

```

u74 = case_when(re74 == 0 ~ 1, TRUE ~ 0),
u75 = case_when(re75 == 0 ~ 1, TRUE ~ 0),
re74sq = re74^2,
re74cube = re74^3,
re75sq = re75^2,
re75cube = re75^3,
re78sq = re78^2,
re75cube = re78^3,
interaction1 = educ*re74,
interaction2 = u74*hisp)

```

Question 1

```

# Question 1A
# fitting model using a logit regression
logit_nsw <- glm(treat ~ age + agesq + agecube + educ + educsq +
  marr + nodegree + black + hisp + re74 + re75 + u74 +
  u75 + interaction1, family = binomial(link = "logit"),
  data = nsw_logit)

logit_nsw

```

```

##
## Call:  glm(formula = treat ~ age + agesq + agecube + educ + educsq +
##      marr + nodegree + black + hisp + re74 + re75 + u74 + u75 +
##      interaction1, family = binomial(link = "logit"), data = nsw_logit)
##
## Coefficients:
## (Intercept)      age      agesq      agecube      educ
## -3.522e+01    2.425e+00   -6.724e-02    5.685e-04    9.248e-01
##      educsq      marr      nodegree      black      hisp
## -5.720e-02   -1.556e+00    9.271e-01    3.851e+00    1.674e+00
##      re74      re75      u74      u75  interaction1
## -2.203e-04   -1.969e-04    1.750e+00    9.440e-03    2.222e-05
##
## Degrees of Freedom: 16176 Total (i.e. Null);  16162 Residual
## Null Deviance:      2022
## Residual Deviance: 808.3    AIC: 838.3

```

```

# estimating model using linear probability model
OLS_nsw <- lm(treat ~ age + agesq + agecube + educ + educsq +
  marr + nodegree + black + hisp + re74 + re75 + u74 +
  u75 + interaction1, data = nsw_lm)

OLS_nsw

```

```

##
## Call:
## lm(formula = treat ~ age + agesq + agecube + educ + educsq +
##      marr + nodegree + black + hisp + re74 + re75 + u74 + u75 +
##      interaction1, data = nsw_lm)
##
## Coefficients:
## (Intercept)      age      agesq      agecube      educ
## -3.714e-01    3.241e-02   -8.975e-04    7.795e-06    6.558e-03

```

##	educsq	marr	nodegree	black	hisp
##	-4.434e-04	-2.352e-02	2.151e-02	1.030e-01	6.795e-03
##	re74	re75	u74	u75	interaction1
##	-3.064e-06	-1.458e-07	4.535e-02	2.094e-02	2.853e-07

Question 1B

Fit a propensity score using a quadratic for every variable and another with a cubic for every variable

#####

Logit

quadratic max

take out age cubed

```
logit_model_quad <- glm(treat ~ age + agesq + educ + educsq +
  marr + nodegree + black + hisp + re74 + re74sq + re75 + re75sq +
  u74 + u75, family = binomial(link = "logit"),
  data = nsw_logit)
```

Fit propensity score to quad model

```
nsw_logit_quad <- nsw_logit %>%
  mutate(pscore = logit_model_quad$fitted.values)
```

mean pscore control

```
pscore_control_logit_quad <- nsw_logit_quad %>%
  filter(treat == 0) %>%
  pull(pscore) %>%
  mean()
```

0.00691

mean pscore treated

```
pscore_treated_logit_quad <- nsw_logit_quad %>%
  filter(treat == 1) %>%
  pull(pscore) %>%
  mean()
```

0.4025

#####

cube max

```
logit_model_cube <- glm(treat ~ age + agesq + agecube + educ + educsq + educcube +
  marr + nodegree + black + hisp + re74 + re74sq + re74cube + re75 + re75sq + re75cube
  u75, family = binomial(link = "logit"),
  data = nsw_logit)
```

Fit propensity score to cubic model

```
nsw_logit_cube <- nsw_logit %>%
  mutate(pscore = logit_model_cube$fitted.values)
```

mean pscore control

```
pscore_control_cube <- nsw_logit_cube %>%
  filter(treat == 0) %>%
  pull(pscore) %>%
  mean()
```

0.00662

mean pscore treated

```
pscore_treated_cube <- nsw_logit_cube %>%
  filter(treat == 1) %>%
```

```

pull(pscore) %>%
mean()
# 0.4279

#####
#Linear probability model
# Quad max
OLS_model_quad <- lm(treat ~ age + agesq + educ + educsq +
  marr + nodegree + black + hisp + re74 + re74sq + re75 + re75sq + u74 +
  u75,data = nsw_lm)

# Fit propoensity score to quad model
nsw_OLS_quad <- nsw_lm %>%
  mutate(pscore = OLS_model_quad$fitted.values)

# mean pscore control
pscore_control_quad <- nsw_OLS_quad %>%
  filter(treat == 0) %>%
  pull(pscore) %>%
  mean()

# 0.00993

# mean pscore treated
pscore_treated_quad <- nsw_OLS_quad %>%
  filter(treat == 1) %>%
  pull(pscore) %>%
  mean()
# 0.14128

#####
# Cube max
OLS_model_cube <- lm(treat ~ age + agesq + agecube + educ + educsq + educcube +
  marr + nodegree + black + hisp + re74 + re74sq + re74cube +
  re75 + re75sq + re75cube + u74 +
  u75,data = nsw_lm)

# Fit propoensity score to cubic model
nsw_OLS_cube <- nsw_lm %>%
  mutate(pscore = OLS_model_cube$fitted.values)

# mean pscore control
pscore_control_OLScube <- nsw_OLS_cube %>%
  filter(treat == 0) %>%
  pull(pscore) %>%
  mean()

# 0.00985

# mean pscore treated
pscore_treated_OLScube <- nsw_OLS_cube %>%
  filter(treat == 1) %>%

```

```
pull(pscore) %>%
mean()
# 0.14828
```

The propensity scores for the four models are as follows:

quadratic linear probability model treatment pscore: 0.14128 control pscore: 0.00993

cubic linear probability model treatment pscore: 0.14828 control pscore: 0.00985

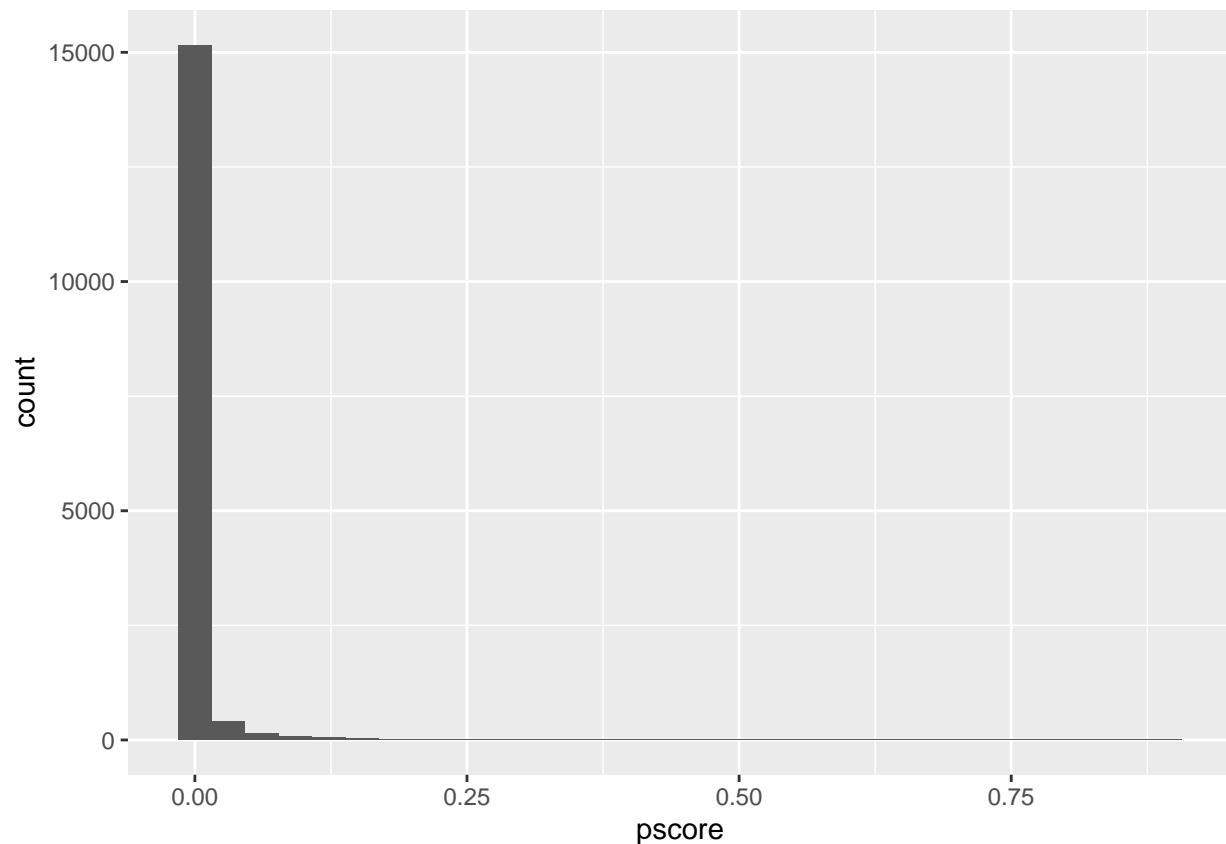
quadratic logit model treatment pscore: 0.4025 control pscore: 0.00691

cubic logit model treatment pscore: 0.4279 control pscore: 0.00662

Question 1C Histograms

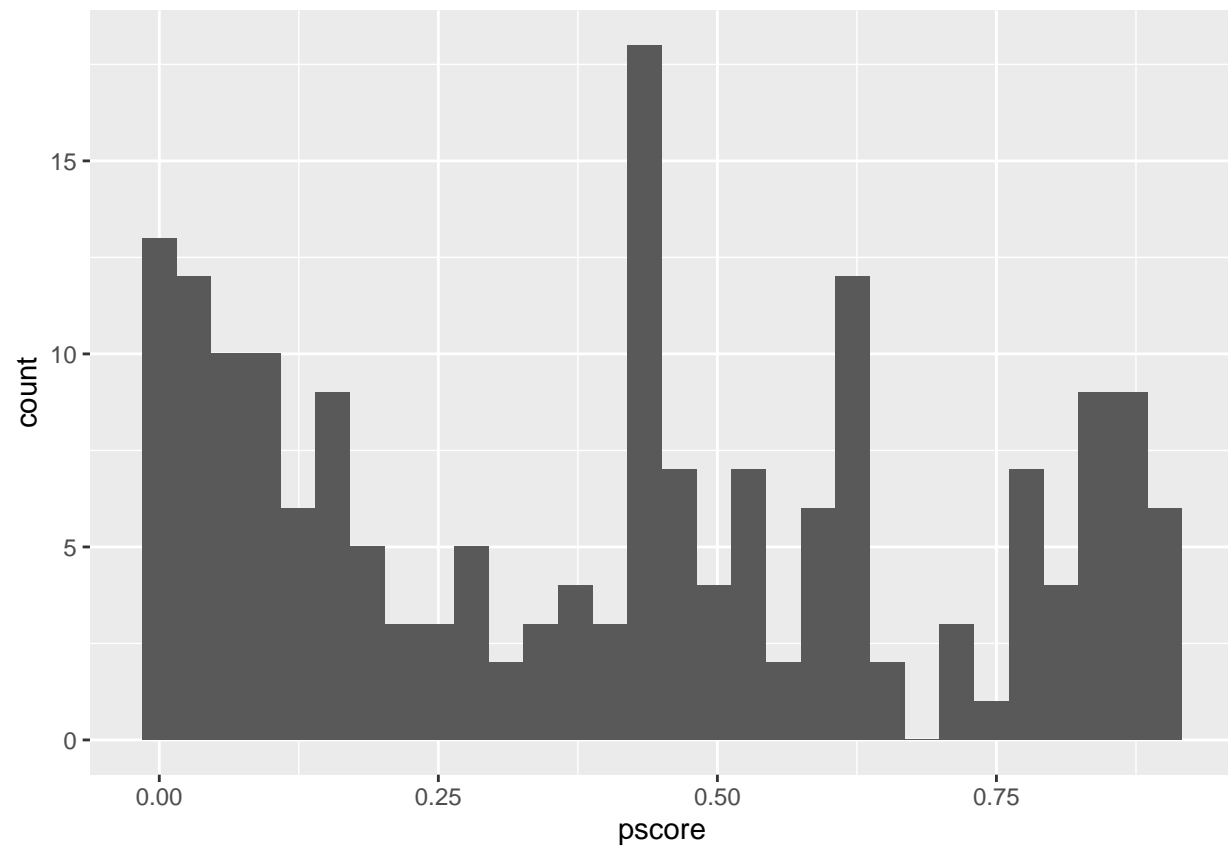
```
# logit quad control
nsw_logit_quad %>%
  filter(treat == 0) %>%
  ggplot() +
  geom_histogram(aes(x = pscore))
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



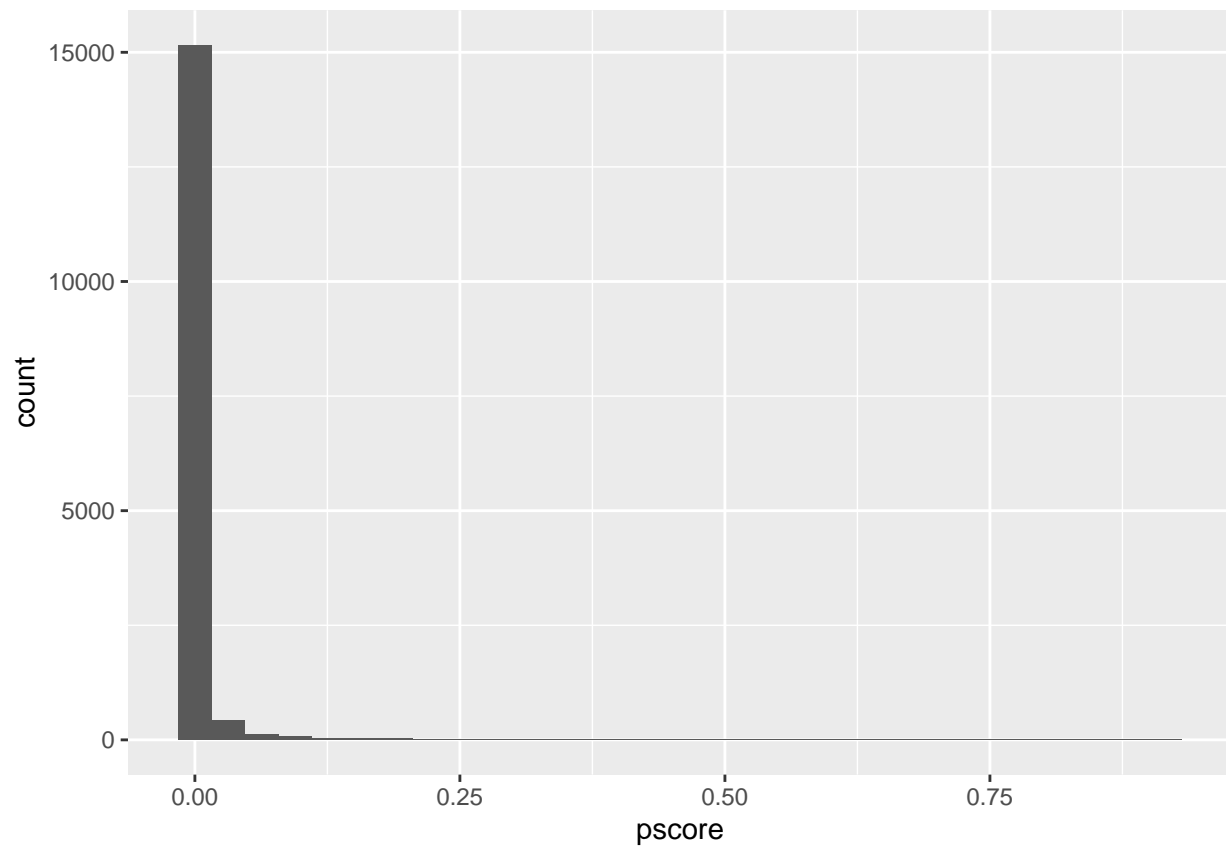
```
# logit quad treatment
nsw_logit_quad %>%
  filter(treat == 1) %>%
  ggplot() +
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



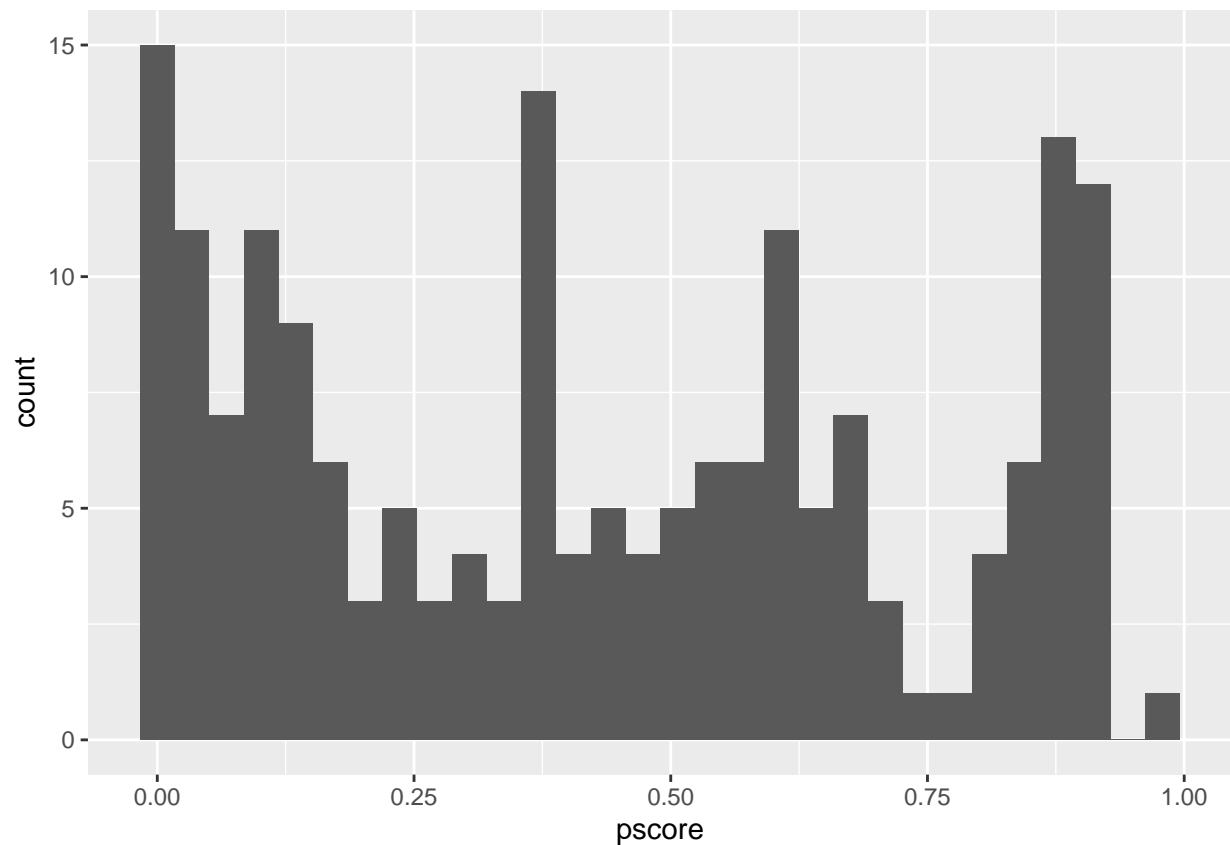
```
# logit cube control  
nsw_logit_cube %>%  
  filter(treat == 0) %>%  
  ggplot() +  
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



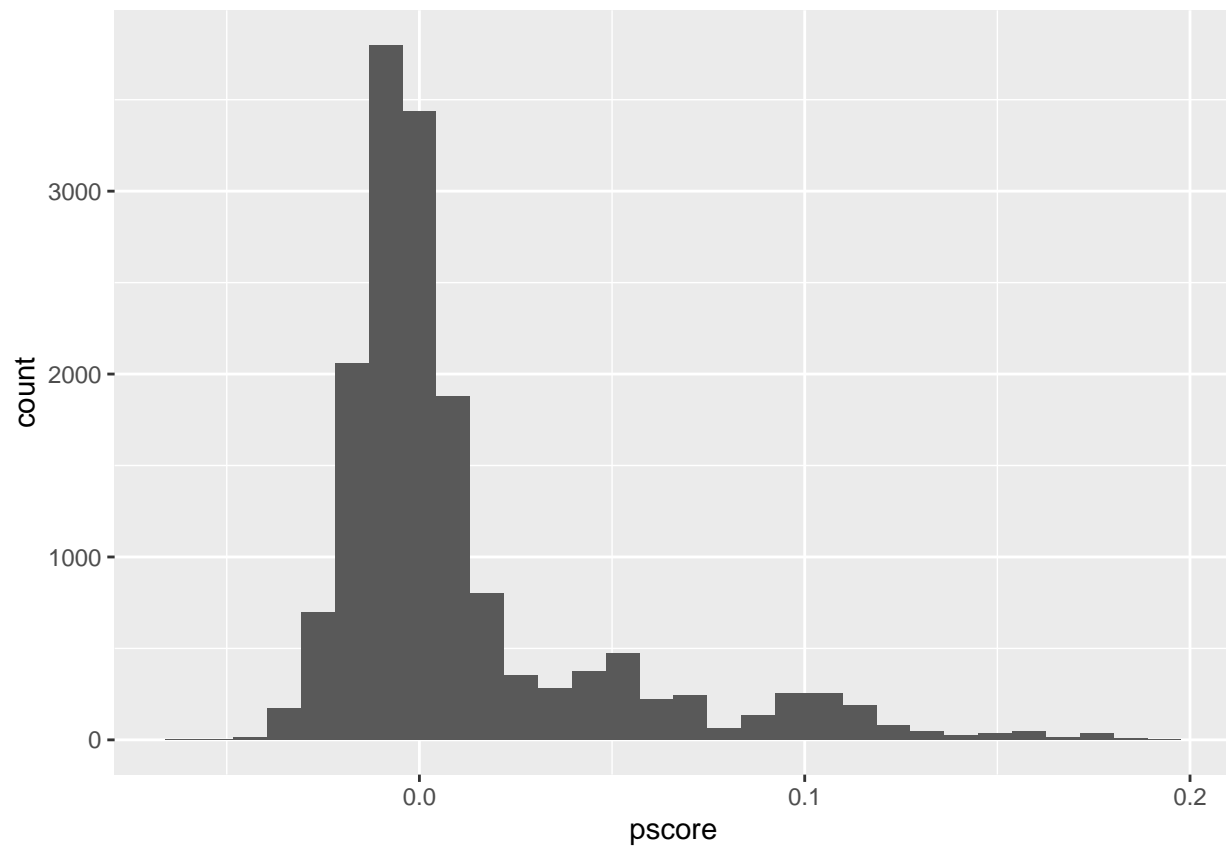
```
# logit cube treatment
nsw_logit_cube %>%
  filter(treat == 1) %>%
  ggplot() +
  geom_histogram(aes(x = pscore))

## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



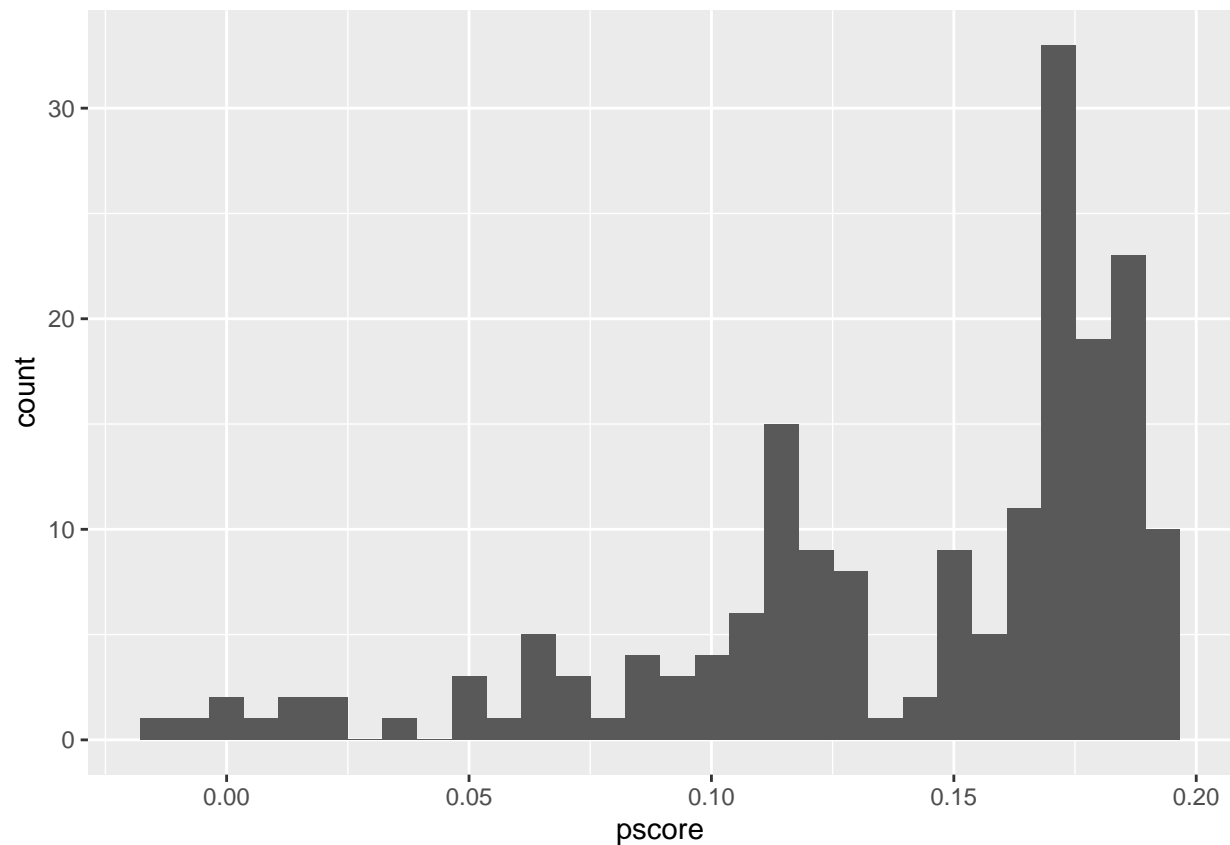
```
# linear probability model (quadratic) control
nsw_OLS_quad %>%
  filter(treat == 0) %>%
  ggplot() +
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

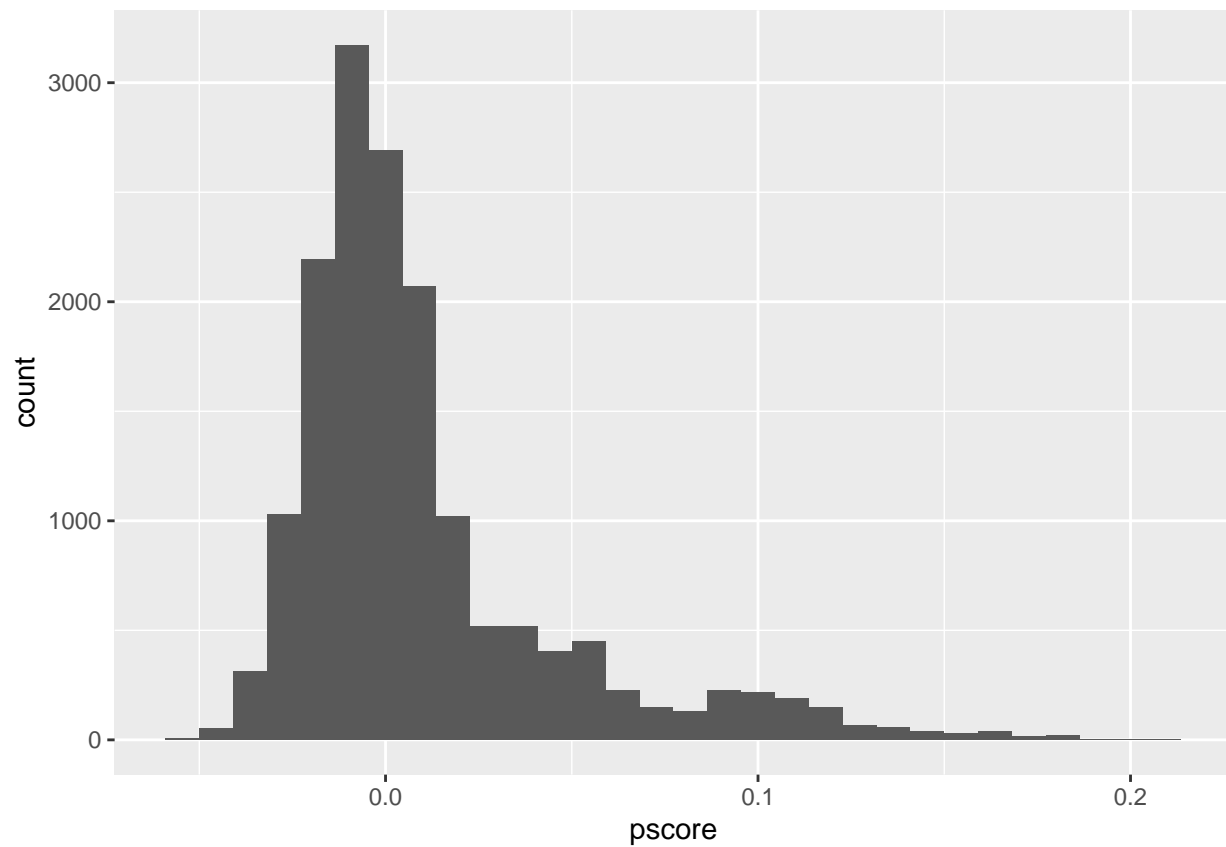
```
# linear probability model (quadratic) treatment  
nsw_OLS_quad %>%  
  filter(treat == 1) %>%  
  ggplot() +  
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



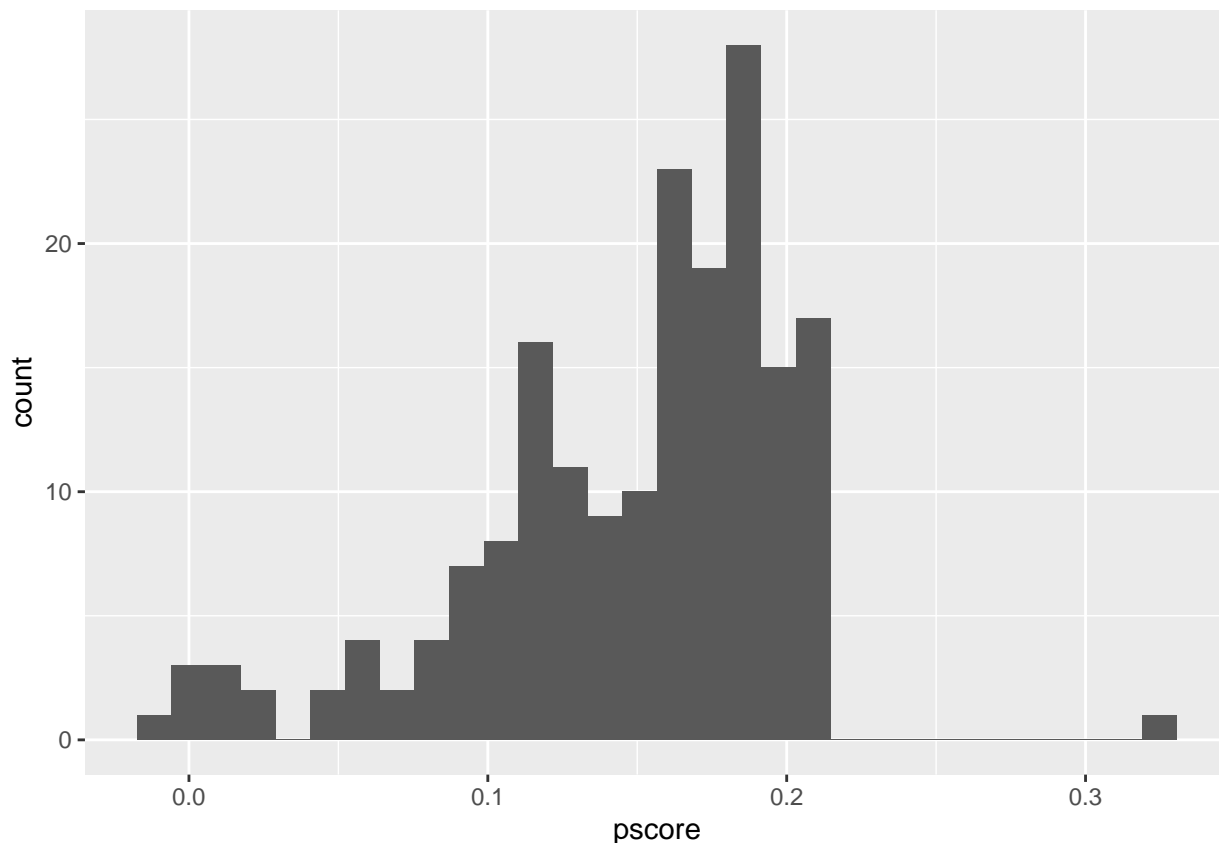
```
# linear probability model (cubic) control
nsw_OLS_cube %>%
  filter(treat == 0) %>%
  ggplot() +
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```
# linear probability model (cubic) treatment  
nsw_OLS_cube %>%  
  filter(treat == 1) %>%  
  ggplot() +  
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



The histograms for the control groups for the logistic models have minimum pscores of 0 and a maximum pscore of about 0.4. The treatment groups for the logistic models have treatment groups with minimum pscores of 0 and a maximum pscore of 1. The linear probability models have control groups with minimum pscores of about -0.05 and a maximum of 0.2. The treatment groups have minimum pscores of -0.02 and a maximum of about 0.2.

Question 1D. trim the propensity scores and recreate the histograms from 1C

trimming propensity score for logit and OLS data

logit model (quadratic)

```
nsw_logit_quad_trim <- nsw_logit_quad %>%
```

```
  filter(!(pscore >= 0.9)) %>%
```

```
  filter(!(pscore <= 0.1))
```

logit model (cubic)

```
nsw_logit_cube_trim <- nsw_logit_cube %>%
```

```
  filter(!(pscore >= 0.9)) %>%
```

```
  filter(!(pscore <= 0.1))
```

linear probability model (quadratic)

```
nsw_OLS_quad_trim <- nsw_OLS_quad %>%
```

```
  filter(!(pscore >= 0.9)) %>%
```

```
  filter(!(pscore <= 0.1))
```

linear probability model (cubic)

```
nsw_OLS_cube_trim <- nsw_OLS_cube %>%
```

```
  filter(!(pscore >= 0.9)) %>%
```

```
  filter(!(pscore <= 0.1))
```

```
#####
# Rerun Question 1B
#### Logit
### quadratic max

# mean pscore control
pscore_control_logit_quad_trim <- nsw_logit_quad_trim %>%
  filter(treat == 0) %>%
  pull(pscore) %>%
  mean()
# 0.2506

# mean pscore treated
pscore_treated_logit_quad_trim <- nsw_logit_quad_trim %>%
  filter(treat == 1) %>%
  pull(pscore) %>%
  mean()
# 0.2768
#####
### cube max

# mean pscore control
pscore_control_cube_trim <- nsw_logit_cube_trim %>%
  filter(treat == 0) %>%
  pull(pscore) %>%
  mean()
# 0.2516

# mean pscore treated
pscore_treated_cube_trim <- nsw_logit_cube_trim %>%
  filter(treat == 1) %>%
  pull(pscore) %>%
  mean()
# 0.2902

#####
#Linear probability model
# Quad max
# mean pscore control
pscore_control_quad_trim <- nsw_OLS_quad_trim %>%
  filter(treat == 0) %>%
  pull(pscore) %>%
  mean()

# 0.1286

# mean pscore treated
pscore_treated_quad_trim <- nsw_OLS_quad_trim %>%
  filter(treat == 1) %>%
  pull(pscore) %>%
  mean()
# 0.1374
```

```
#####
#linear probability model (cubic)
# mean pscore control
pscore_control_OLS_cube_trim <- nsw_OLS_cube_trim %>%
  filter(treat == 0) %>%
  pull(pscore) %>%
  mean()

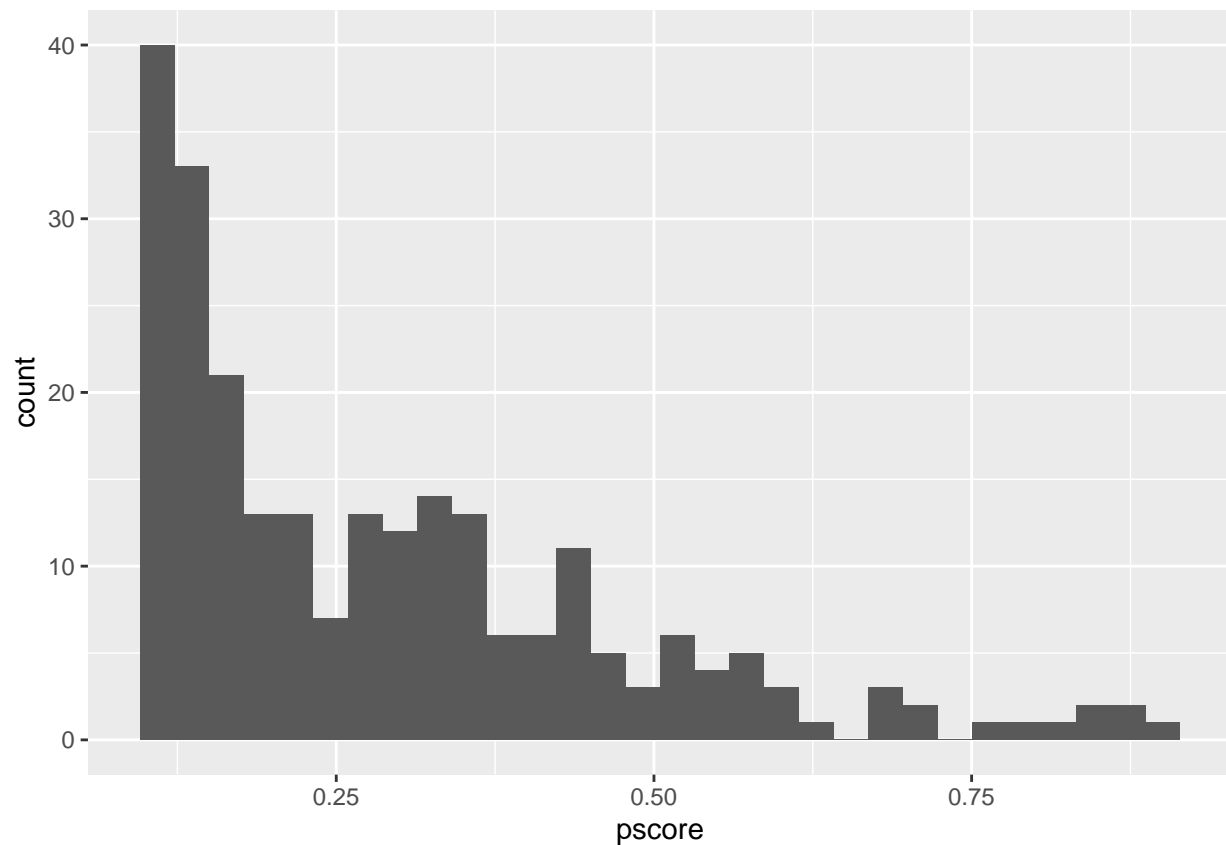
# 0.1294

# mean pscore treated
pscore_treated_OLS_cube_trim <- nsw_OLS_cube_trim %>%
  filter(treat == 1) %>%
  pull(pscore) %>%
  mean()
# 0.1404

#####
# rerun the histograms from 1C

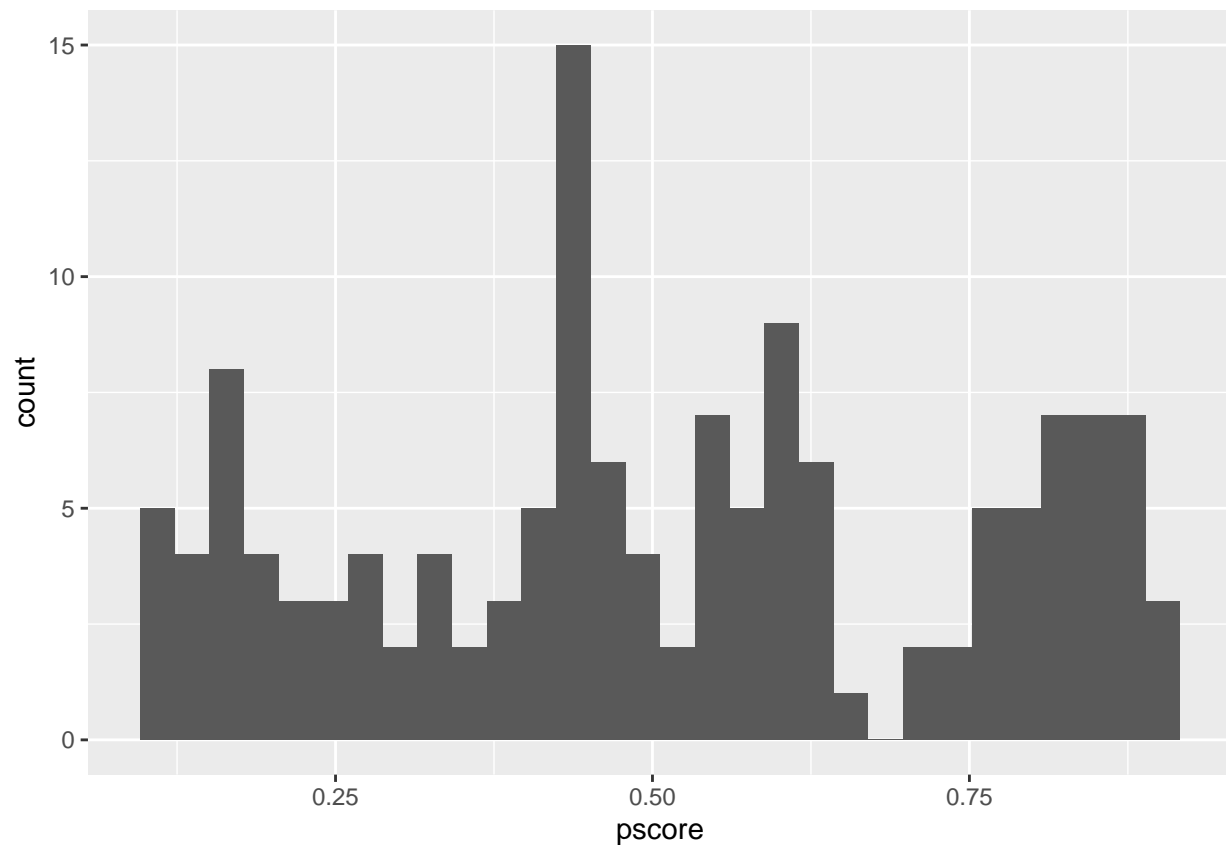
# logit quad control
nsw_logit_quad_trim %>%
  filter(treat == 0) %>%
  ggplot() +
  geom_histogram(aes(x = pscore))

## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



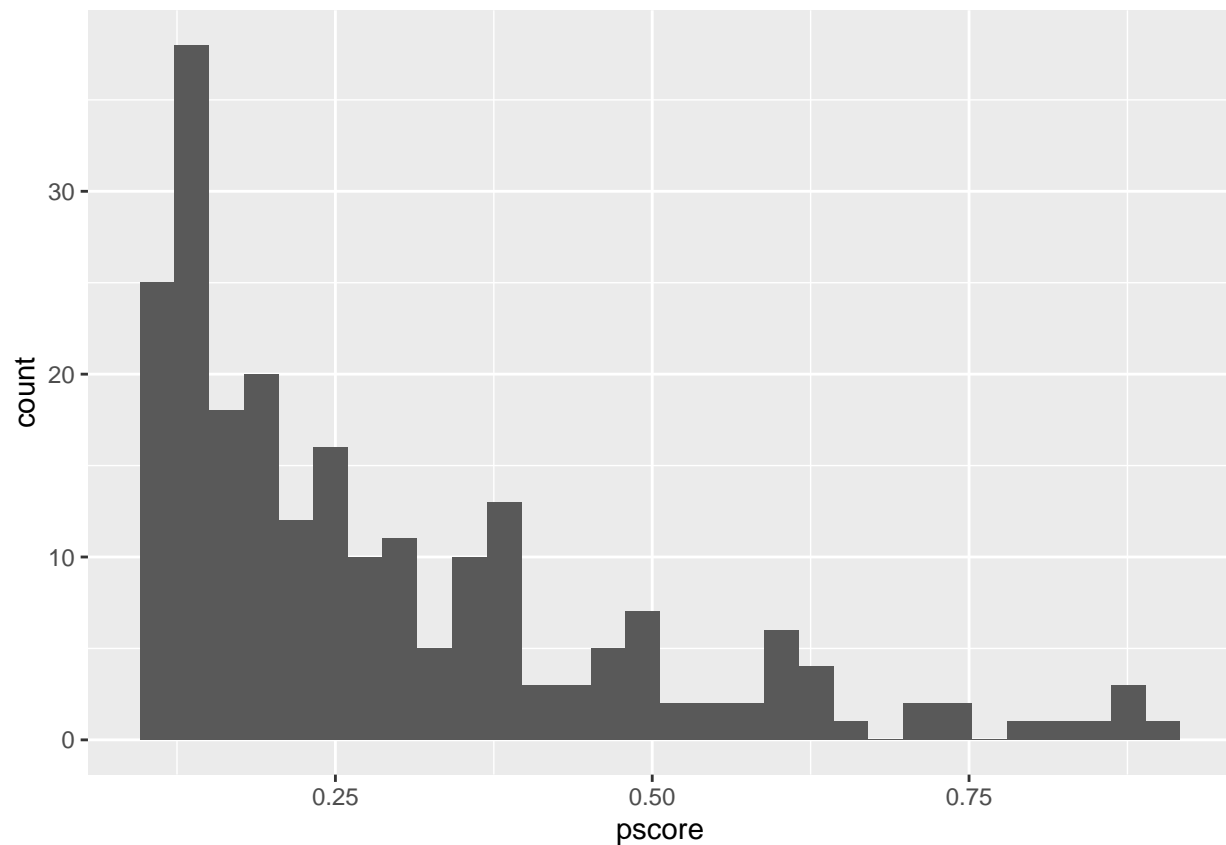
```
# logit quad treatment
nsw_logit_quad_trim %>%
  filter(treat == 1) %>%
  ggplot() +
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



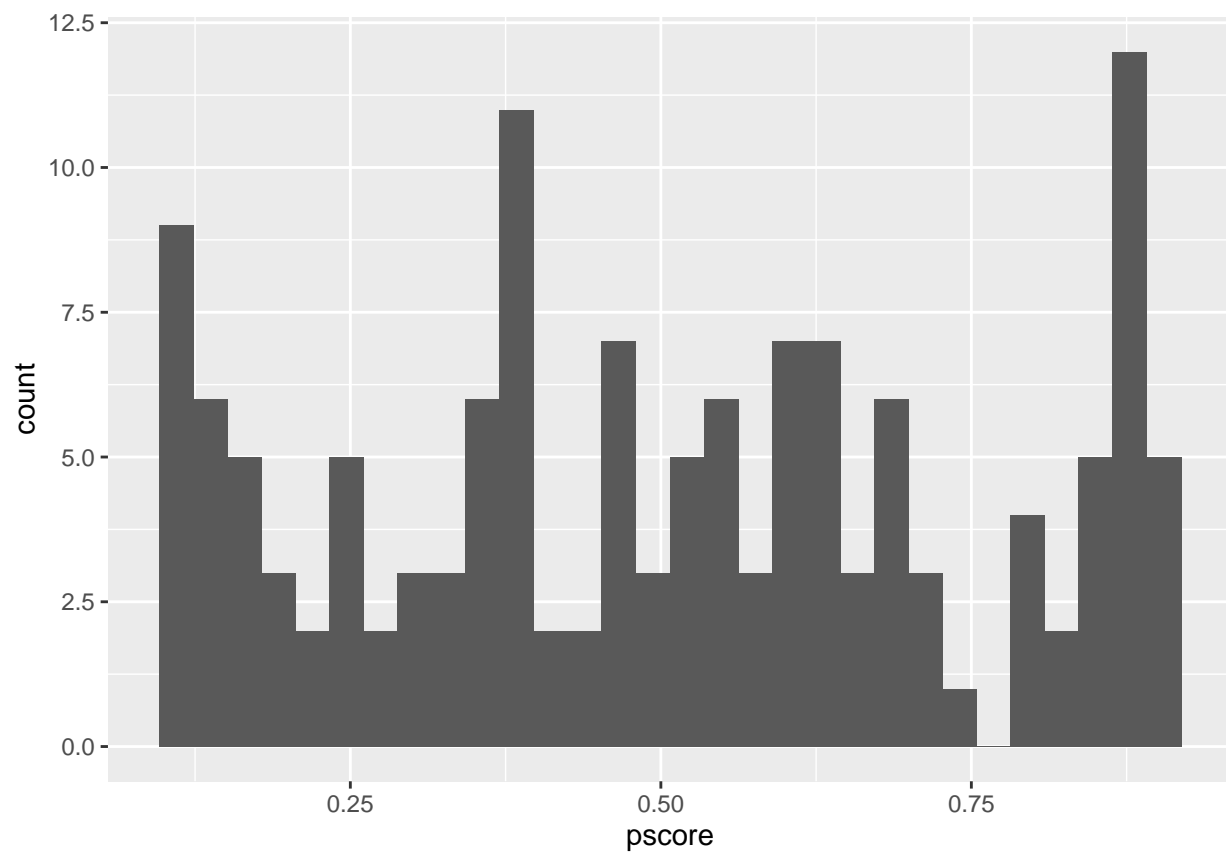
```
# logit cube control
nsw_logit_cube_trim %>%
  filter(treat == 0) %>%
  ggplot() +
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

```
# logit cube treatment
nsw_logit_cube_trim %>%
  filter(treat == 1) %>%
  ggplot() +
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```
# linear probability model (quadratic) control
```

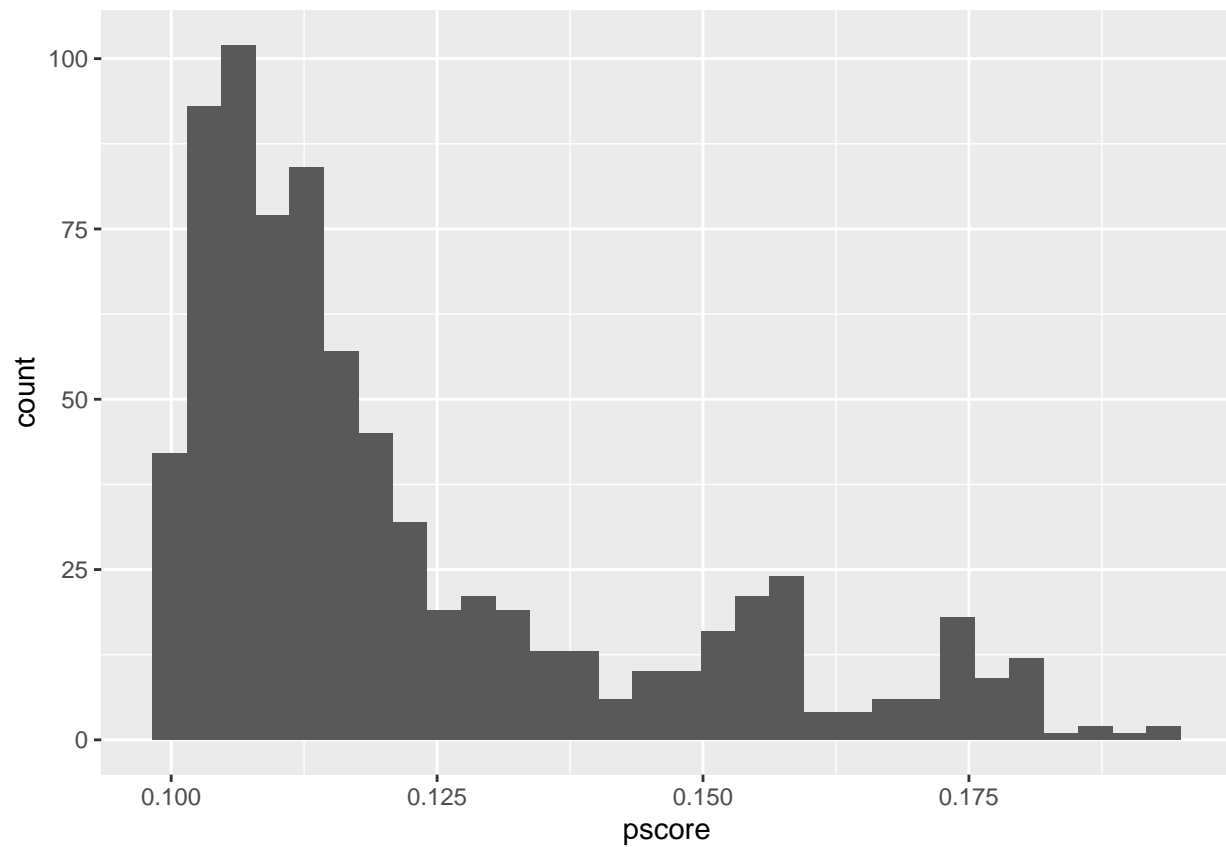
```
nsw_OLS_quad_trim %>%
```

```
  filter(treat == 0) %>%
```

```
  ggplot() +
```

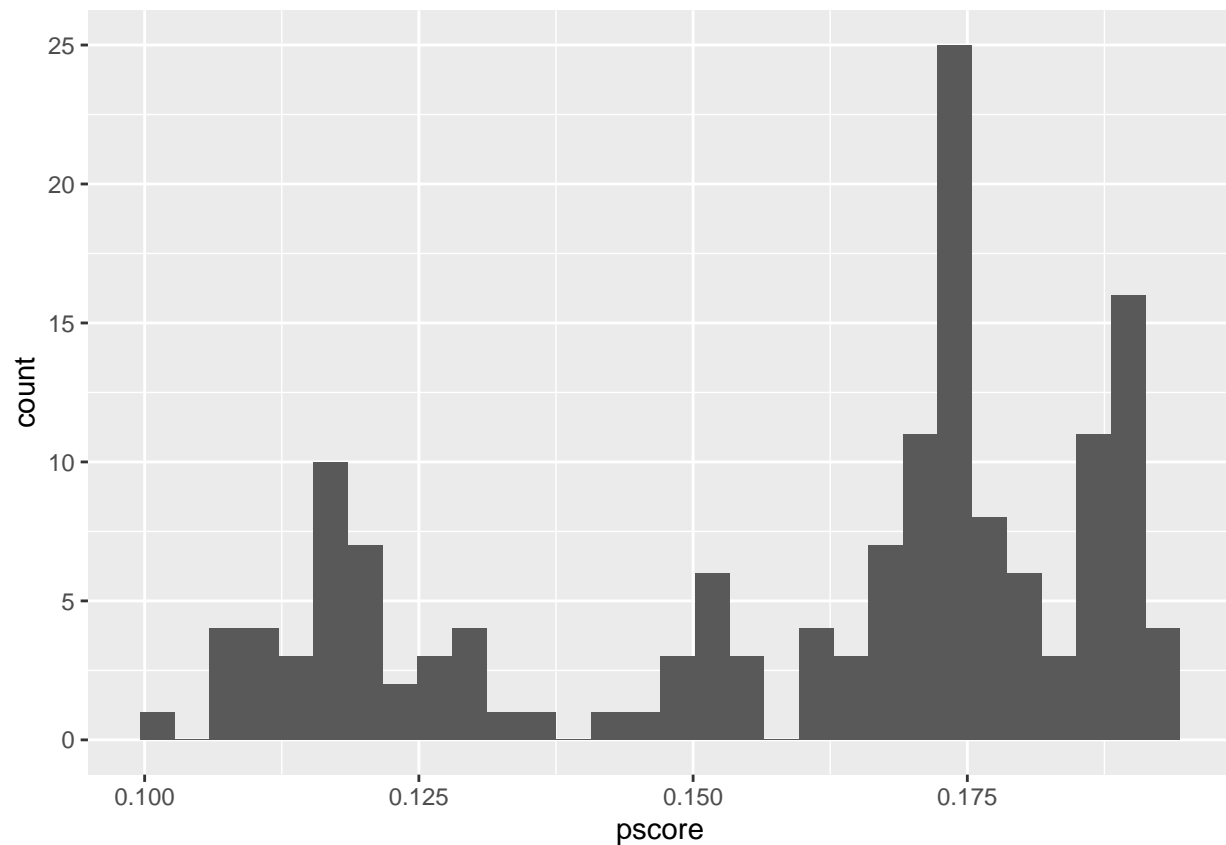
```
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



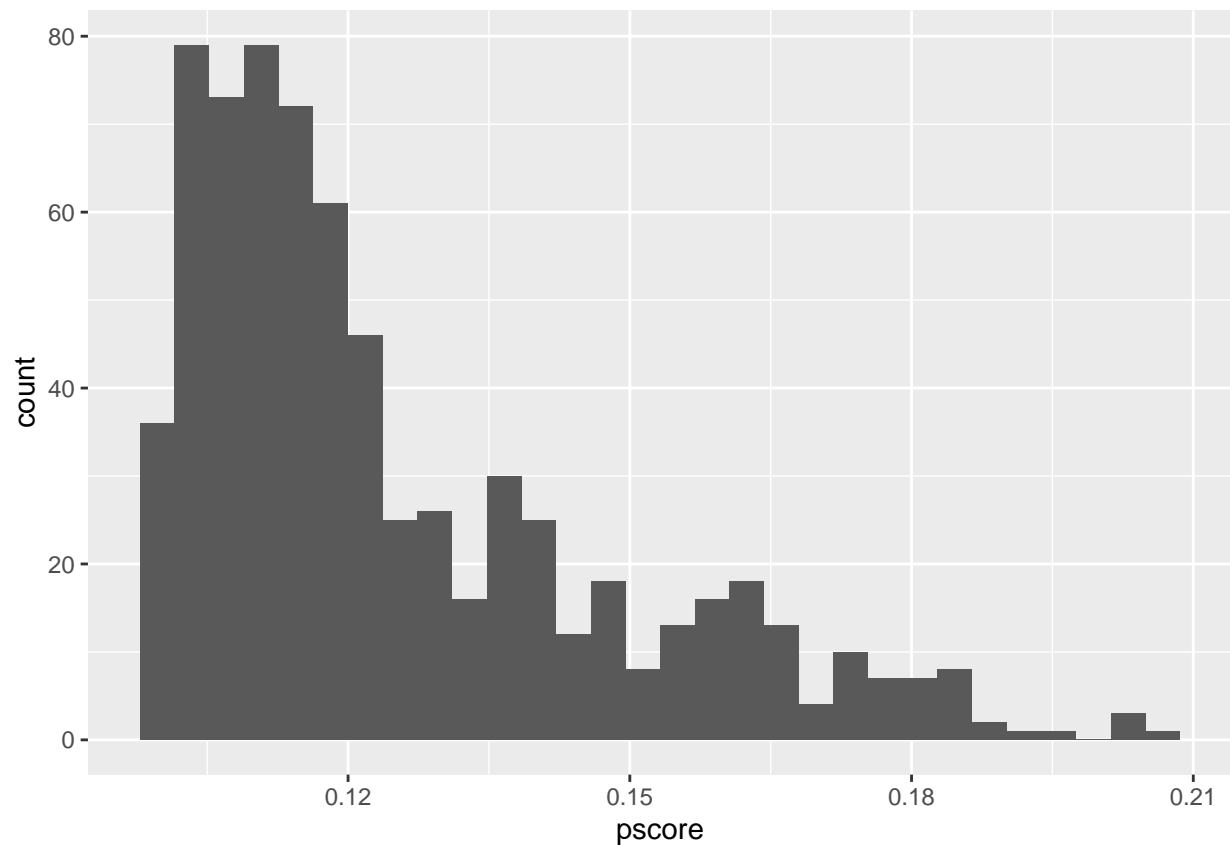
```
# linear probability model (quadratic) treatment
nsw_OLS_quad_trim %>%
  filter(treat == 1) %>%
  ggplot() +
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



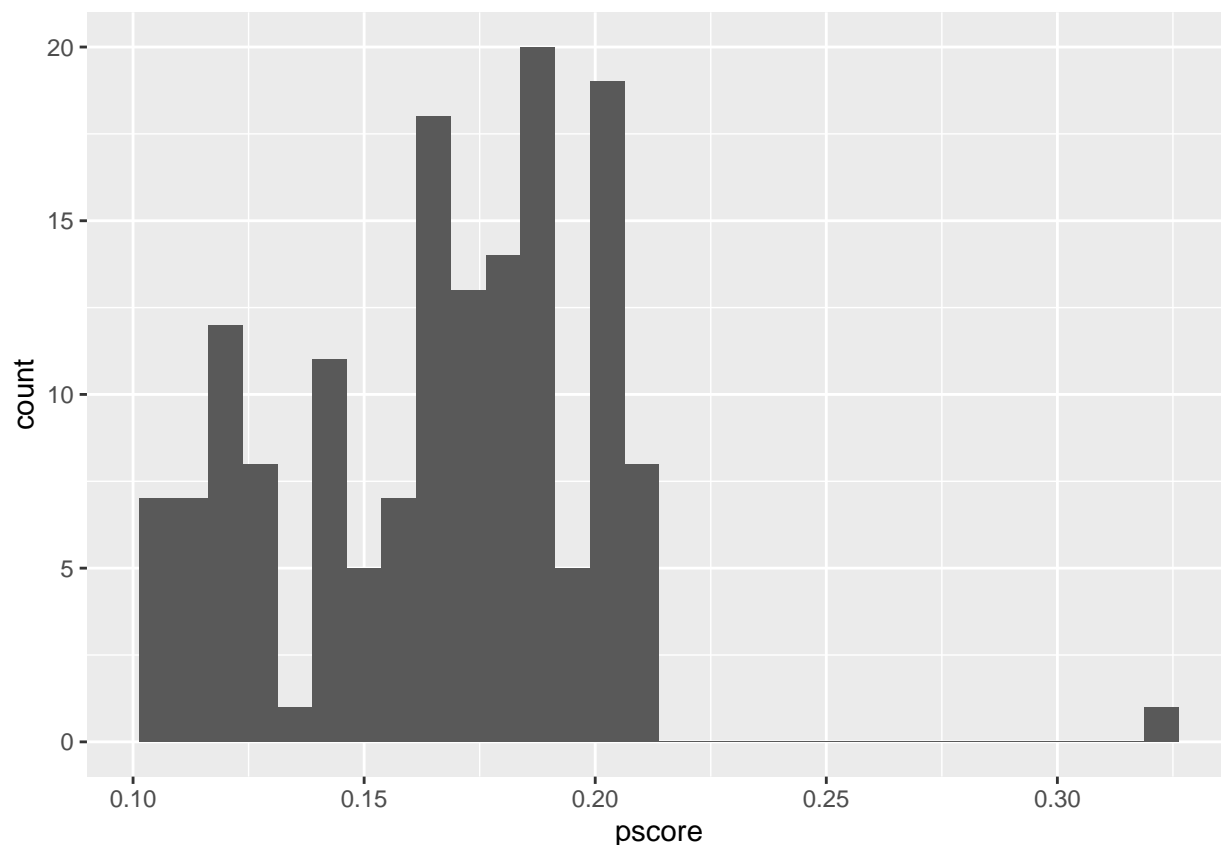
```
# linear probability model (cubic) control  
nsw_OLS_cube_trim %>%  
  filter(treat == 0) %>%  
  ggplot() +  
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```
# linear probability model (cubic) treatment  
nsw_OLS_cube_trim %>%  
  filter(treat == 1) %>%  
  ggplot() +  
  geom_histogram(aes(x = pscore))
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



For the following questions I will only use the trimmed data, cubic logit model, and the quadratic linear probability model.

Question 2

```
##### Question 2: First difference for the logit cubic model and quadratic linear probability model
### First difference for the logit cubic model
# Filter re78 to only include people in the treatment group
nsw_logit_cube_trim %>%
  filter(treat == 1) %>%
  summary(re78)
```

```
##      data_id      treat      age      educ      black
## Length:138      Min.   :1      Min.   :17.00      Min.   : 4.00      Min.   :0.000
## Class :character 1st Qu.:1      1st Qu.:20.00      1st Qu.: 9.00      1st Qu.:1.000
## Mode  :character Median :1      Median :25.00      Median :11.00      Median :1.000
##                      Mean  :1      Mean  :25.27      Mean  :10.26      Mean  :0.942
##                      3rd Qu.:1      3rd Qu.:28.00      3rd Qu.:11.00      3rd Qu.:1.000
##                      Max.   :1      Max.   :48.00      Max.   :15.00      Max.   :1.000
##      hisp      marr      nodegree      re74
## Min.   :0.00000      Min.   :0.0000      Min.   :0.0000      Min.   : 0
## 1st Qu.:0.00000      1st Qu.:0.0000      1st Qu.:1.0000      1st Qu.: 0
## Median :0.00000      Median :0.0000      Median :1.0000      Median : 0
## Mean   :0.03623      Mean   :0.1449      Mean   :0.7536      Mean   : 1788
## 3rd Qu.:0.00000      3rd Qu.:0.0000      3rd Qu.:1.0000      3rd Qu.: 0
## Max.   :1.00000      Max.   :1.0000      Max.   :1.0000      Max.   :35040
##      re75      re78      agesq      agecube
```

```
## Min. : 0 Min. : 0 Min. : 289.0 Min. : 4913
## 1st Qu.: 0 1st Qu.: 0 1st Qu.: 400.0 1st Qu.: 8000
## Median : 0 Median : 4003 Median : 625.0 Median : 15625
## Mean : 1084 Mean : 6095 Mean : 682.3 Mean : 19799
## 3rd Qu.: 1621 3rd Qu.: 9589 3rd Qu.: 784.0 3rd Qu.: 21952
## Max. : 11537 Max. : 36647 Max. : 2304.0 Max. : 110592
## educsq educcube u74 u75
## Min. : 16.0 Min. : 64 Min. : 0.0000 Min. : 0.0000
## 1st Qu.: 81.0 1st Qu.: 729 1st Qu.: 1.0000 1st Qu.: 0.0000
## Median : 121.0 Median : 1331 Median : 1.0000 Median : 1.0000
## Mean : 109.1 Mean : 1190 Mean : 0.7609 Mean : 0.6449
## 3rd Qu.: 121.0 3rd Qu.: 1331 3rd Qu.: 1.0000 3rd Qu.: 1.0000
## Max. : 225.0 Max. : 3375 Max. : 1.0000 Max. : 1.0000
## re74sq re74cube re75sq
## Min. : 0.000e+00 Min. : 0.000e+00 Min. : 0
## 1st Qu.: 0.000e+00 1st Qu.: 0.000e+00 1st Qu.: 0
## Median : 0.000e+00 Median : 0.000e+00 Median : 0
## Mean : 2.633e+07 Mean : 5.813e+11 Mean : 5279631
## 3rd Qu.: 0.000e+00 3rd Qu.: 0.000e+00 3rd Qu.: 2633251
## Max. : 1.228e+09 Max. : 4.302e+13 Max. : 133092455
## re75cube re78sq interaction1 interaction2
## Min. : 0.000e+00 Min. : 0.000e+00 Min. : 0 Min. : 0.00000
## 1st Qu.: 0.000e+00 1st Qu.: 0.000e+00 1st Qu.: 0 1st Qu.: 0.00000
## Median : 6.414e+10 Median : 1.602e+07 Median : 0 Median : 0.00000
## Mean : 1.818e+12 Mean : 8.909e+07 Mean : 19684 Mean : 0.03623
## 3rd Qu.: 8.816e+11 3rd Qu.: 9.194e+07 3rd Qu.: 0 3rd Qu.: 0.00000
## Max. : 4.922e+13 Max. : 1.343e+09 Max. : 490561 Max. : 1.00000
## pscore
## Min. : 0.1031
## 1st Qu.: 0.3040
## Median : 0.5097
## Mean : 0.5035
## 3rd Qu.: 0.6873
## Max. : 0.8985
```

```
# Filter and average on the treatment effect
```

```
mean1 <- nsw_logit_cube_trim %>%
  filter(treat == 1) %>%
  pull(re78) %>%
  mean()
```

```
# save the
```

```
nsw_logit_cube_trim$y1 <- mean1
```

```
# Average treatment effect on the untreated
```

```
nsw_logit_cube_trim %>%
  filter(treat == 0) %>%
  summary(re78)
```

```
## data_id treat age educ black
## Length:224 Min. :0 Min. :16.00 Min. : 2.00 Min. :0.000
## Class :character 1st Qu.:0 1st Qu.:19.00 1st Qu.: 9.00 1st Qu.:1.000
## Mode :character Median :0 Median :24.00 Median :11.00 Median :1.000
## Mean :0 Mean :26.08 Mean :10.38 Mean :0.942
## 3rd Qu.:0 3rd Qu.:31.00 3rd Qu.:12.00 3rd Qu.:1.000
```

```
##           Max.      :0      Max.      :55.00      Max.      :16.00      Max.      :1.000
##           hisp           marr           nodegree           re74
## Min.      :0.00000      Min.      :0.0000      Min.      :0.0000      Min.      : 0
## 1st Qu.:0.00000      1st Qu.:0.0000      1st Qu.:0.0000      1st Qu.: 0
## Median :0.00000      Median :0.0000      Median :1.0000      Median : 0
## Mean      :0.03571      Mean      :0.2054      Mean      :0.6295      Mean      : 2426
## 3rd Qu.:0.00000      3rd Qu.:0.0000      3rd Qu.:1.0000      3rd Qu.: 3511
## Max.      :1.00000      Max.      :1.0000      Max.      :1.0000      Max.      :22322
##           re75           re78           agesq           agecube
## Min.      : 0.00      Min.      : 0      Min.      : 256.0      Min.      : 4096
## 1st Qu.: 0.00      1st Qu.: 0      1st Qu.: 361.0      1st Qu.: 6859
## Median : 50.13      Median : 1632      Median : 576.0      Median : 13824
## Mean      : 1630.70      Mean      : 4633      Mean      : 748.2      Mean      : 23629
## 3rd Qu.: 2258.04      3rd Qu.: 7696      3rd Qu.: 961.0      3rd Qu.: 29791
## Max.      :13117.69      Max.      :25565      Max.      :3025.0      Max.      :166375
##           educsq           educcube           u74           u75
## Min.      : 4.0      Min.      : 8      Min.      :0.0000      Min.      :0.0000
## 1st Qu.: 81.0      1st Qu.: 729      1st Qu.:0.0000      1st Qu.:0.0000
## Median :121.0      Median :1331      Median :1.0000      Median :0.0000
## Mean      :112.7      Mean      :1264      Mean      :0.5759      Mean      :0.4911
## 3rd Qu.:144.0      3rd Qu.:1728      3rd Qu.:1.0000      3rd Qu.:1.0000
## Max.      :256.0      Max.      :4096      Max.      :1.0000      Max.      :1.0000
##           re74sq           re74cube           re75sq
## Min.      : 0      Min.      :0.000e+00      Min.      : 0
## 1st Qu.: 0      1st Qu.:0.000e+00      1st Qu.: 0
## Median : 0      Median :0.000e+00      Median : 2542
## Mean      : 23138265      Mean      :2.921e+11      Mean      : 10588462
## 3rd Qu.: 12345738      3rd Qu.:4.346e+10      3rd Qu.: 5098777
## Max.      :498268545      Max.      :1.112e+13      Max.      :172073802
##           re75cube           re78sq           interaction1           interaction2
## Min.      :0.000e+00      Min.      : 0      Min.      : 0      Min.      :0.00000
## 1st Qu.:0.000e+00      1st Qu.: 0      1st Qu.: 0      1st Qu.:0.00000
## Median :4.395e+09      Median : 2673567      Median : 0      Median :0.00000
## Mean      :8.944e+11      Mean      : 57217111      Mean      : 23727      Mean      :0.02232
## 3rd Qu.:4.559e+11      3rd Qu.: 59229890      3rd Qu.: 37942      3rd Qu.:0.00000
## Max.      :1.671e+13      Max.      :653552348      Max.      :267863      Max.      :1.00000
##           pscore           y1
## Min.      :0.1001      Min.      :6095
## 1st Qu.:0.1454      1st Qu.:6095
## Median :0.2300      Median :6095
## Mean      :0.2893      Mean      :6095
## 3rd Qu.:0.3766      3rd Qu.:6095
## Max.      :0.8935      Max.      :6095
```

```
mean0 <- nsw_logit_cube_trim %>%
  filter(treat == 0) %>%
  pull(re78) %>%
  mean()
```

```
nsw_logit_cube_trim$y0 <- mean0
```

```
ate_logit <- unique(nsw_logit_cube_trim$y1 - nsw_logit_cube_trim$y0)
# 1461.0585
nsw_logit_cube_trim <- nsw_logit_cube_trim %>%
```



```
filter(treat == 1) %>%
select(-y1, -y0)
```

```
### First difference for quadratic linear probability model
# Filter re78 to only include people in the treatment group
nsw_OLS_quad_trim %>%
  filter(treat == 1) %>%
  summary(re78)
```

```
##      data_id          treat          age          educ          black
## Length:152          Min.   :1      Min.   :17.00      Min.   : 4.00      Min.   :1
## Class :character    1st Qu.:1      1st Qu.:20.00      1st Qu.: 9.00      1st Qu.:1
## Mode  :character    Median :1      Median :25.00      Median :11.00      Median :1
##                               Mean   :1      Mean   :25.93      Mean   :10.26      Mean   :1
##                               3rd Qu.:1      3rd Qu.:29.00      3rd Qu.:12.00      3rd Qu.:1
##                               Max.   :1      Max.   :48.00      Max.   :16.00      Max.   :1
##      hisp      marr      nodegree      re74
## Min.   :0      Min.   :0.0000      Min.   :0.0000      Min.   : 0.0
## 1st Qu.:0      1st Qu.:0.0000      1st Qu.:0.0000      1st Qu.: 0.0
## Median :0      Median :0.0000      Median :1.0000      Median : 0.0
## Mean   :0      Mean   :0.1645      Mean   :0.7434      Mean   :1768.3
## 3rd Qu.:0      3rd Qu.:0.0000      3rd Qu.:1.0000      3rd Qu.: 989.3
## Max.   :0      Max.   :1.0000      Max.   :1.0000      Max.   :25929.7
##      re75      re78      agesq      agecube
## Min.   : 0      Min.   : 0      Min.   :289.0      Min.   : 4913
## 1st Qu.: 0      1st Qu.: 0      1st Qu.:400.0      1st Qu.: 8000
## Median : 0      Median :3880      Median :625.0      Median :15625
## Mean   :1342      Mean   :5942      Mean   :726.6      Mean   :22086
## 3rd Qu.:1674      3rd Qu.:9292      3rd Qu.:841.0      3rd Qu.:24389
## Max.   :25142      Max.   :60308      Max.   :2304.0      Max.   :110592
##      educsq      educcube      u74      u75
## Min.   :16.0      Min.   : 64      Min.   :0.0000      Min.   :0.0000
## 1st Qu.:81.0      1st Qu.:729      1st Qu.:0.0000      1st Qu.:0.0000
## Median :121.0      Median :1331      Median :1.0000      Median :1.0000
## Mean   :109.4      Mean   :1201      Mean   :0.7303      Mean   :0.6316
## 3rd Qu.:144.0      3rd Qu.:1728      3rd Qu.:1.0000      3rd Qu.:1.0000
## Max.   :256.0      Max.   :4096      Max.   :1.0000      Max.   :1.0000
##      re74sq      re74cube      re75sq
## Min.   : 0      Min.   :0.000e+00      Min.   : 0
## 1st Qu.: 0      1st Qu.:0.000e+00      1st Qu.: 0
## Median : 0      Median :0.000e+00      Median : 0
## Mean   :20091417      Mean   :3.012e+11      Mean   :11477633
## 3rd Qu.: 978651      3rd Qu.:9.681e+08      3rd Qu.:2803266
## Max.   :672348289      Max.   :1.743e+13      Max.   :632132244
##      re75cube      re78sq      interaction1      interaction2
## Min.   :0.000e+00      Min.   :0.000e+00      Min.   : 0      Min.   :0
## 1st Qu.:0.000e+00      1st Qu.:0.000e+00      1st Qu.: 0      1st Qu.:0
## Median :5.849e+10      Median :1.506e+07      Median : 0      Median :0
## Mean   :2.700e+12      Mean   :9.575e+07      Mean   :18271      Mean   :0
## 3rd Qu.:8.024e+11      3rd Qu.:8.635e+07      3rd Qu.: 9583      3rd Qu.:0
## Max.   :2.193e+14      Max.   :3.637e+09      Max.   :259297      Max.   :0
##      pscore
## Min.   :0.1018
## 1st Qu.:0.1310
```

```
## Median :0.1709
## Mean   :0.1598
## 3rd Qu.:0.1793
## Max.   :0.1935
```

```
# Filter and average on the treatment effect
```

```
mean1_OLS <- nsw_OLS_quad_trim %>%
  filter(treat == 1) %>%
  pull(re78) %>%
  mean()
```

```
# save the
```

```
nsw_OLS_quad_trim$y1_OLS <- mean1_OLS
```

```
# Average treatment effect on the untreated
```

```
nsw_OLS_quad_trim %>%
  filter(treat == 0) %>%
  summary(re78)
```

```
##      data_id      treat      age      educ      black
## Length:769      Min.    :0      Min.    :16.00      Min.    : 0.00      Min.    :1
## Class :character 1st Qu.:0      1st Qu.:22.00      1st Qu.: 9.00      1st Qu.:1
## Mode  :character Median :0      Median :29.00      Median :11.00      Median :1
##                               Mean  :0      Mean   :30.72      Mean   :10.89      Mean    :1
##                               3rd Qu.:0      3rd Qu.:38.00      3rd Qu.:12.00      3rd Qu.:1
##                               Max.   :0      Max.   :55.00      Max.   :18.00      Max.    :1
##      hisp      marr      nodegree      re74
## Min.    :0      Min.    :0.0000      Min.    :0.0000      Min.    : 0.0
## 1st Qu.:0      1st Qu.:0.0000      1st Qu.:0.0000      1st Qu.: 525.1
## Median :0      Median :0.0000      Median :1.0000      Median : 8060.4
## Mean    :0      Mean    :0.4499      Mean    :0.5267      Mean    : 9965.0
## 3rd Qu.:0      3rd Qu.:1.0000      3rd Qu.:1.0000      3rd Qu.:17827.4
## Max.    :0      Max.    :1.0000      Max.    :1.0000      Max.    :25862.3
##      re75      re78      agesq      agecube
## Min.    : 0.0      Min.    : 0.0      Min.    : 256      Min.    : 4096
## 1st Qu.: 136.1      1st Qu.: 731.5      1st Qu.: 484      1st Qu.: 10648
## Median : 6939.3      Median : 9339.2      Median : 841      Median : 24389
## Mean    : 9309.3      Mean    :10956.5      Mean    :1049      Mean    : 39104
## 3rd Qu.:17135.2      3rd Qu.:19265.1      3rd Qu.:1444      3rd Qu.: 54872
## Max.    :25243.6      Max.    :25564.7      Max.    :3025      Max.    :166375
##      educsq      educcube      u74      u75
## Min.    : 0.0      Min.    : 0      Min.    :0.0000      Min.    :0.000
## 1st Qu.: 81.0      1st Qu.: 729      1st Qu.:0.0000      1st Qu.:0.000
## Median :121.0      Median :1331      Median :0.0000      Median :0.000
## Mean    :125.3      Mean    :1504      Mean    :0.2146      Mean    :0.238
## 3rd Qu.:144.0      3rd Qu.:1728      3rd Qu.:0.0000      3rd Qu.:0.000
## Max.    :324.0      Max.    :5832      Max.    :1.0000      Max.    :1.000
##      re74sq      re74cube      re75sq
## Min.    : 0      Min.    :0.000e+00      Min.    : 0
## 1st Qu.: 275713      1st Qu.:1.448e+08      1st Qu.: 18514
## Median : 64970432      Median :5.237e+11      Median : 48153746
## Mean    :186586136      Mean    :3.972e+12      Mean    :169529862
## 3rd Qu.:317815090      3rd Qu.:5.666e+12      3rd Qu.:293614383
## Max.    :668859612      Max.    :1.730e+13      Max.    :637236856
##      re75cube      re78sq      interaction1      interaction2
```

```
## Min. :0.000e+00 Min. : 0 Min. : 0 Min. :0
## 1st Qu.:3.914e+08 1st Qu.: 535055 1st Qu.: 5167 1st Qu.:0
## Median :8.146e+11 Median : 87221262 Median : 82113 Median :0
## Mean :4.507e+12 Mean :209689105 Mean :108583 Mean :0
## 3rd Qu.:7.150e+12 3rd Qu.:371144816 3rd Qu.:174590 3rd Qu.:0
## Max. :1.671e+13 Max. :653552348 Max. :439659 Max. :0
## pscore y1_OLS
## Min. :0.1000 Min. :5942
## 1st Qu.:0.1065 1st Qu.:5942
## Median :0.1137 Median :5942
## Mean :0.1225 Mean :5942
## 3rd Qu.:0.1313 3rd Qu.:5942
## Max. :0.1935 Max. :5942
```

```
mean0_OLS <- nsw_OLS_quad_trim %>%
  filter(treat == 0) %>%
  pull(re78) %>%
  mean()

nsw_OLS_quad_trim$y0_OLS <- mean0_OLS

ate_OLS <- unique(nsw_OLS_quad_trim$y1_OLS - nsw_OLS_quad_trim$y0_OLS)
# -5014.1128
nsw_OLS_quad_trim <- nsw_OLS_quad_trim %>%
  filter(treat == 1) %>%
  select(-y1_OLS, -y0_OLS)
```

The average treatment effect for the cubic logit model is 1461.06 and the average treatment effect for the quadratic linear probability model is -5014.11.

Question 3

```
##### Question 3 weighted difference in difference regression
### Cubic logit model
N <- nrow(nsw_logit_cube_trim)
# Manual with non-normalized weights using trimmed data for the cubic logit model
nsw_logit_cube_trim <- nsw_logit_cube_trim %>%
  mutate(d1 = treat/pscore,
         d0 = (1-treat)/(1-pscore))

s1 <- sum(nsw_logit_cube_trim$d1)
s0 <- sum(nsw_logit_cube_trim$d0)

nsw_logit_cube_trim <- nsw_logit_cube_trim %>%
  mutate(y1 = treat * re78/pscore,
         y0 = (1-treat) * re78/(1-pscore),
         ht = y1 - y0)

nsw_logit_cube_trim %>%
  pull(ht) %>%
  mean()
```

```
## [1] 16029.51
```

The weighted difference in difference estimate for the cubic logit model is 16029.51.

```

### Quadratic linear probability model
# Manual with non-normalized weights using trimmed data for the cubic logit model
nsw_OLS_quad_trim <- nsw_OLS_quad_trim %>%
  mutate(d1 = treat/pscore,
         d0 = (1-treat)/(1-pscore))

s1 <- sum(nsw_OLS_quad_trim$d1)
s0 <- sum(nsw_OLS_quad_trim$d0)

nsw_OLS_quad_trim <- nsw_OLS_quad_trim %>%
  mutate(y1 = treat * re78/pscore,
         y0 = (1-treat) * re78/(1-pscore),
         ht = y1 - y0)

nsw_OLS_quad_trim %>%
  pull(ht) %>%
  mean()

```

```
## [1] 38049.65
```

The weighted difference in difference estimate for the quadratic linear probability model is -4047.76.