

VAE: Code

We discuss the highlights of the code in this [notebook \(vae.ipynb\)](#).

- derived from the [Keras examples \(https://keras.io/examples/generative/vae/\)](https://keras.io/examples/generative/vae/).

Deriving a new Model via sub-classing

Similar to the code for the Autoencoder , the VAE class

- is sub-classed from `Model`
- *contains* an Encoder `self.encoder` and a Decoder `self.decoder`
 - but these are defined *external* to the class
 - rather than within the class code

Custom `train_step`

Unlike the code for `Autoencoder`, the model for `VAE` implements the model behavior

- **not** by overriding the `call` method
- but by *overriding* the training step `train_step` method

So

- we can't actually "call" this model (e.g., $x = m(x)$)
- but, during training, we can make it behave in the desired manner
 - call encoder
 - call decoder

```
z_mean, z_log_var, z = self.encoder(data)
reconstruction = self.decoder(z)
```

Custom training step vs custom loss

The reason for overriding `train_step` rather than `call` may not be obvious at first glance.

The VAE has a *complex loss function* of two parts

$$\begin{aligned}\mathcal{L} &= -\log(p_{\Theta}(\mathbf{x})) + \mathbf{KL}(q_{\Phi}(\mathbf{z}|\mathbf{x}) \parallel q(\mathbf{z}|\mathbf{x})) \\ &= \mathcal{L}_R + \mathcal{L}_D\end{aligned}$$

- Reconstruction Loss \mathcal{L}_R
- KL loss \mathcal{L}_D

One could (in theory) create a custom loss

- an the ordinary training mechanism
- would compute the loss
- and the gradients of the loss

By overriding the `train_step`, *our code* becomes responsible for the gradient computation

```
with tf.GradientTape() as tape:
    z_mean, z_log_var, z = self.encoder(data)
    reconstruction = self.decoder(z)

    reconstruction_loss = ...
    kl_loss = ...
    total_loss = reconstruction_loss + kl_loss

grads = tape.gradient(total_loss, self.trainable_weights)
self.optimizer.apply_gradients(zip(grads, self.trainable_weights))
```

The computation of `total_loss`

- is performed within the scope of `tf.GradientTape()`
- which allows automatic differentiation of the loss

We then manually compute the gradients

```
grads = tape.gradient(total_loss, self.trainable_weights)
```

and update the weights through the gradients

```
self.optimizer.apply_gradients(zip(grads, self.trainable_weights))
```


So why go through this effort (as opposed to a custom loss) ?

The model *also* provides *custom metrics*

- values gathered during training
 - we are used to seeing Loss and Validation Loss

These metrics are

- total loss
- reconstruction loss
- KL loss

```
@property
def metrics(self):
    return [
        self.total_loss_tracker,
        self.reconstruction_loss_tracker,
        self.kl_loss_tracker,
    ]
```

The reason for overriding `train_step` is so that *we can update the custom metrics* during training

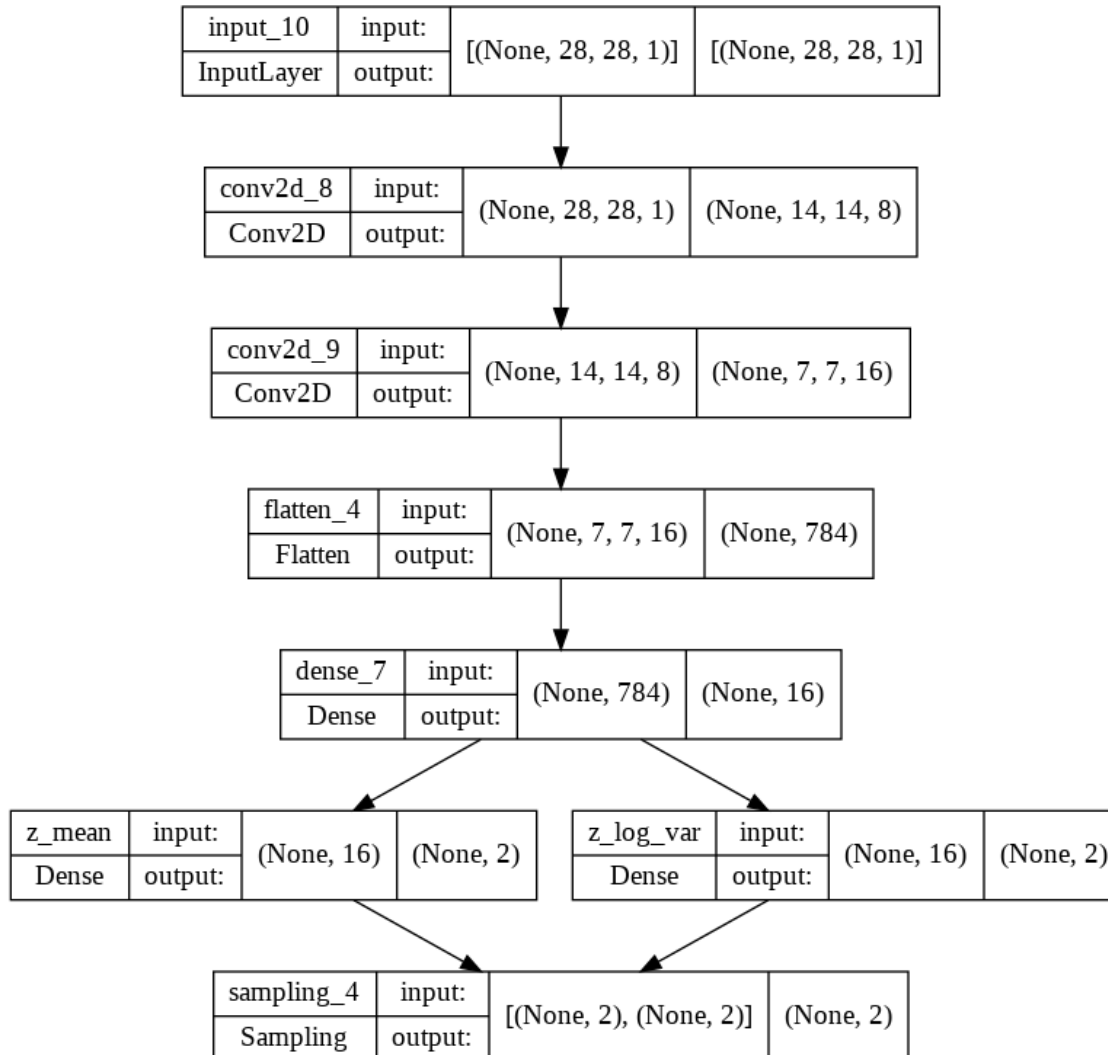
```
self.total_loss_tracker.update_state(total_loss)
self.reconstruction_loss_tracker.update_state(reconstruction_loss)
self.kl_loss_tracker.update_state(kl_loss)
```

Here is the complete code for the method

```
def train_step(self, data):
    with tf.GradientTape() as tape:
        z_mean, z_log_var, z = self.encoder(data)
        reconstruction = self.decoder(z)
        reconstruction_loss = tf.reduce_mean(
            tf.reduce_sum(
                keras.losses.binary_crossentropy(data, reconstruction), axis=
(1, 2)
            )
        )
        kl_loss = -0.5 * (1 + z_log_var - tf.square(z_mean) - tf.exp(z_log_va
r))
        kl_loss = tf.reduce_mean(tf.reduce_sum(kl_loss, axis=1))
        total_loss = reconstruction_loss + kl_loss
        grads = tape.gradient(total_loss, self.trainable_weights)
        self.optimizer.apply_gradients(zip(grads, self.trainable_weights))
        self.total_loss_tracker.update_state(total_loss)
        self.reconstruction_loss_tracker.update_state(reconstruction_loss)
        self.kl_loss_tracker.update_state(kl_loss)
    return {
```

Encoder architecture

We can see the Encoder architecture



The input image ($28 \times 28 \times 1$)

- is processed by 2 Convolutional layers
- creating a representation with the *same spatial dimensions* as the input
- but with many more (16 versus 1) features

It is likely that this representation is richer than the alternative

- of initial flattening
- processing by Dense layers

You can see (in components `z_mean` and `z_log_var`)

- that the final representation of the input
- is used to derive the moments ($\mu^{(i)}$ and $\sigma_{(i)}$) of the *distribution* for example i

The final layer samples from this *multivariate* distribution

- to produce the latent representation
- a *vector* of length `latent_dim`

Note

In our code `latent_dim = 2`

- this is a sample from a *bivariate* distribution with mean $\mu^{(i)}$ and standard deviation $\sigma^{(i)}$
- don't confuse the length of the sample vector with the pair of moments

Decoder Architecture

We can see the Encoder architecture

input_11	input:	[(None, 2)]	[(None, 2)]
InputLayer	output:		



dense_8	input:	(None, 2)	(None, 1568)
Dense	output:		



reshape_3	input:	(None, 1568)	(None, 7, 7, 32)
Reshape	output:		



conv2d_transpose_9	input:	(None, 7, 7, 32)	(None, 14, 14, 16)
Conv2DTranspose	output:		



conv2d_transpose_10	input:	(None, 14, 14, 16)	(None, 28, 28, 8)
Conv2DTranspose	output:		



conv2d_transpose_11	input:	(None, 28, 28, 8)	(None, 28, 28, 1)
Conv2DTranspose	output:		

You can see that the Decoder

- takes a latent vector of length `latent_dim` as input
- Inverts the Encoder's Convolutional layers (Conv2DTranspose)

These steps are *almost* exactly the inverse of

- reverse of the Encoder's operation sequence

Kernel size of 1

The final Conv2DTranspose layer

- is an example of a Convolution with kernel size **one** [discussed in Intro course \(CNN Space and Time.ipynb#Kernel-size-1\)](#)
- whose sole purpose is to "re-size" the channel dimension
 - in this case: to 1 channel, just like the input

Deriving a new Layer via sub-classing

Sampling from the multivariate distribution comes from a *new layer type* Sampling

- sub-class of the generic Layer class

Similar to sub-classing a Model the work of sub-classing a Layer

- comes from overriding the call method

There is one sample drawn from *each example* in the batch

- each with it's own $\mu^{(i)}$ and $\sigma^{(i)}$

```
class Sampling(layers.Layer):  
    """Uses (z_mean, z_log_var) to sample z, the vector encoding a dig  
    it."""  
  
    def call(self, inputs):  
        z_mean, z_log_var = inputs  
        batch = tf.shape(z_mean)[0]  
        dim = tf.shape(z_mean)[1]  
        epsilon = tf.keras.backend.random_normal(shape=(batch, dim))  
        return z_mean + tf.exp(0.5 * z_log_var) * epsilon
```

Exploring the latent space

The notebook runs some experiments

- [explore the latent space \(vae.ipynb#Display-a-grid-of-sampled-digits\)](#)

Conditional VAE

The [code for the Conditional VAE \(vae.ipynb#Conditional-VAE\)](#) is very similar to that of the unconditional VAE.

The main difference is that both the Encoder and Decoder inputs are now *pairs* where

- the second element of the pair is the desired label
- the first element is the same as the unconditional VAE

The label arguments

- are implemented One Hot Encoded vectors
- not categorical constants

The way that an image with a *specific* label gets generated is not obvious

- puzzling in its simplicity

The Encoder

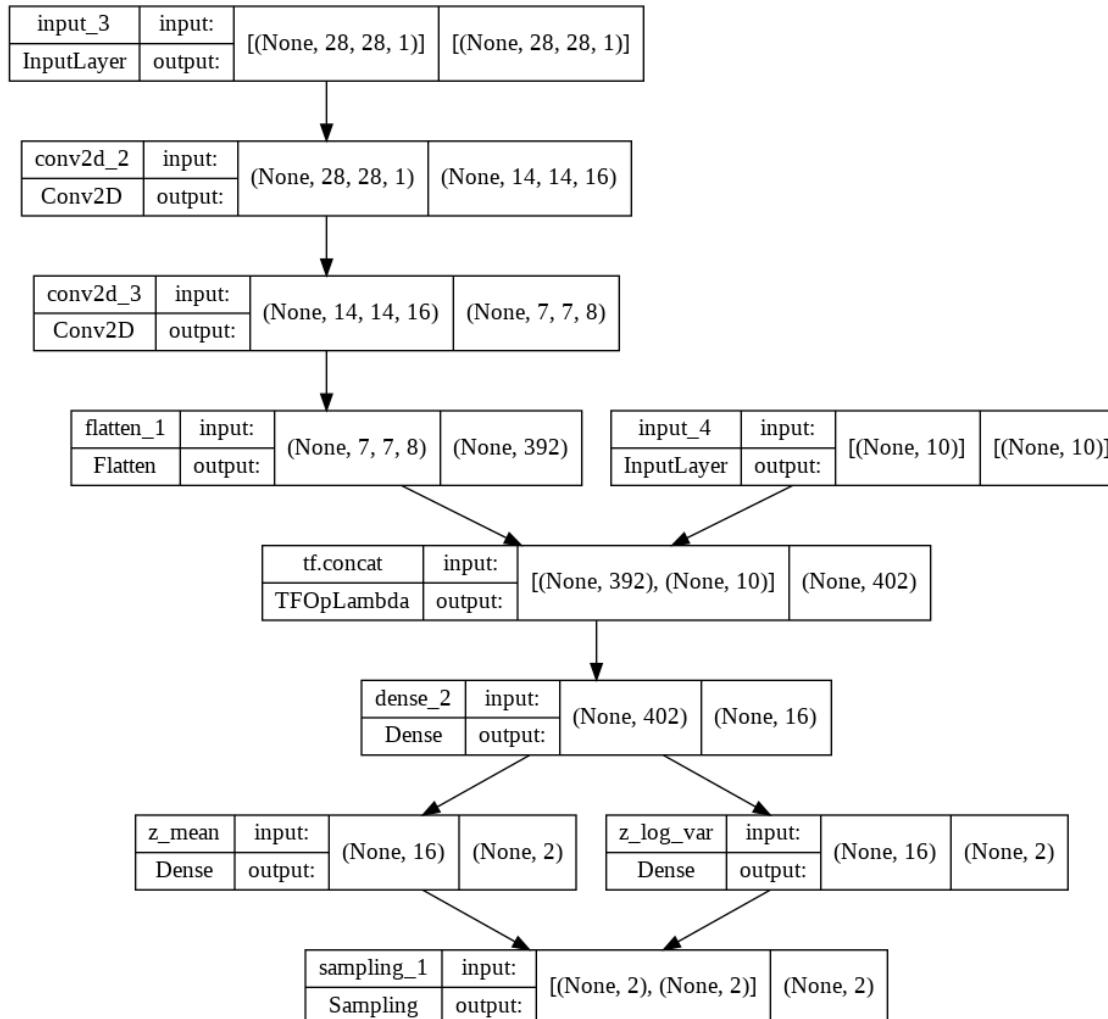
- ignores the label for most of its processing of the input
- uses the label
 - to modify the alternate representation of the input
 - immediately before creating $\mu^{(i)}$ and $\sigma^{(i)}$

Thus, $\mu^{(i)}$ and $\sigma^{(i)}$ are *conditioned* on both

- the alternate representation that the unconditional VAE would produce
- **and** the label

Here is the Encoder

- notice the two distinct Input layers



The Decoder

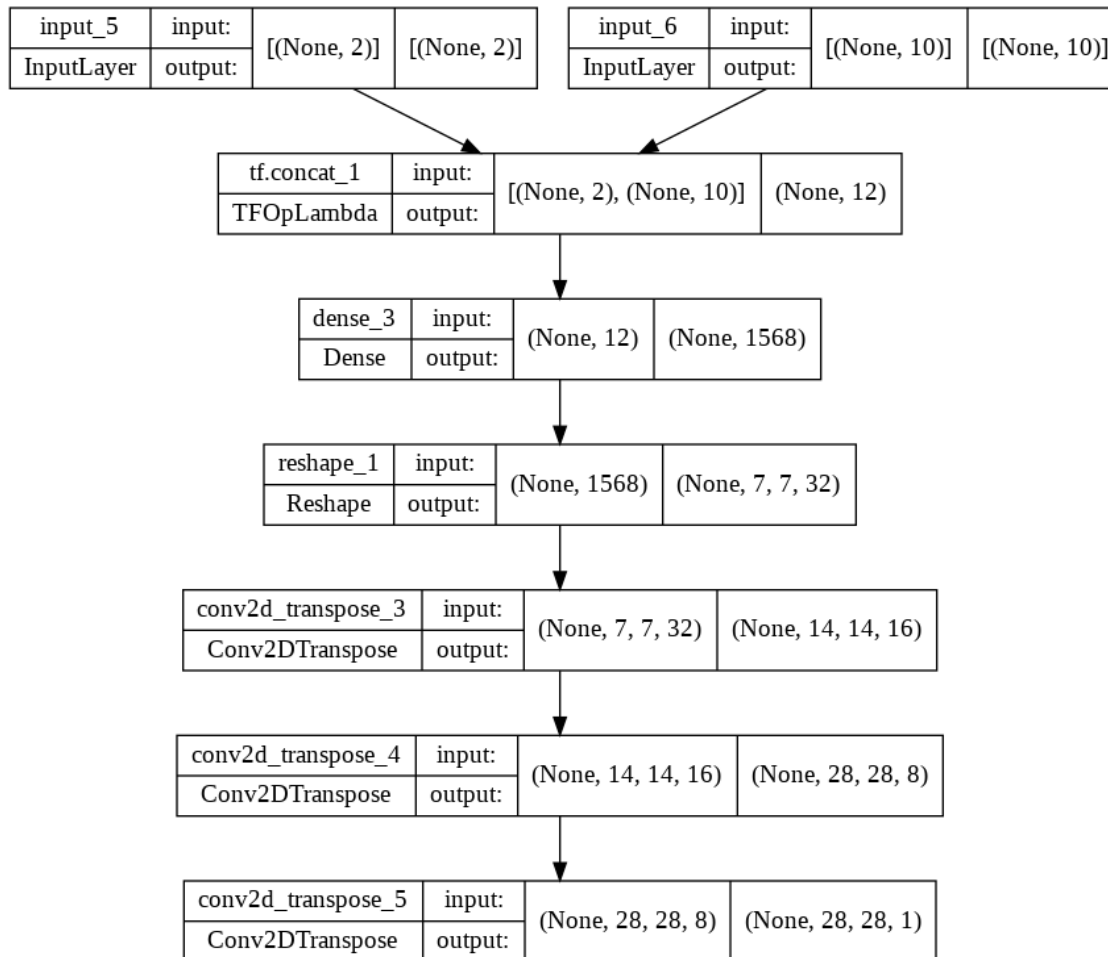
- concatenates the OHE of the label to the latent created by the Encoder
- to create a "longer" latent representation
 - length is: `latent_dim + number of classes`
 - versus `latent_dim` for the unconditional VAE

The CVAE Decoder is almost exactly the same as the unconditional VAE Decoder

- just with a longer latent

Here is the Decoder

- notice the two distinct Input layers



So how does the Decoder produce an image with the chosen label ?

During training it learns

- the "meaning" of the label part of the elongated latent
- by observing a larger representation loss
 - when it creates an output that doesn't match the label

That is, consider training example i with label C

- the Decoder reconstruction loss is large if its output is very different than the input
- So the Decoder learns (i.e., its weights associate) a relationship between
 - the OHE of the label
 - the desired output

This is the mantra of Deep Learning

- you don't guide or program the model with specific instructions on **how** to achieve a task
- it **learns** the association between input and output
 - through Loss minimization

In [2]: `print("Done")`

Done

