

Functional model: the basics

The Sequential model

- organizes layers as an ordered list
- restricts the input to layer $(l + 1)$ to be the output of layer l .

The computation of a Sequential model is easy to describe and picture

- a graph
- each node represents the computation of a layer
- the nodes are connected sequentially in a straight line
- single input, single output
 - mostly true
 - can have inputs/outputs that are arrays, each element representing a different input/output value

The Functional model

- imposes **no** ordering on layers
- imposes **no** restriction on connect outputs of one layer to the input of another

The computation of a Functional model can be pictured as a general graph

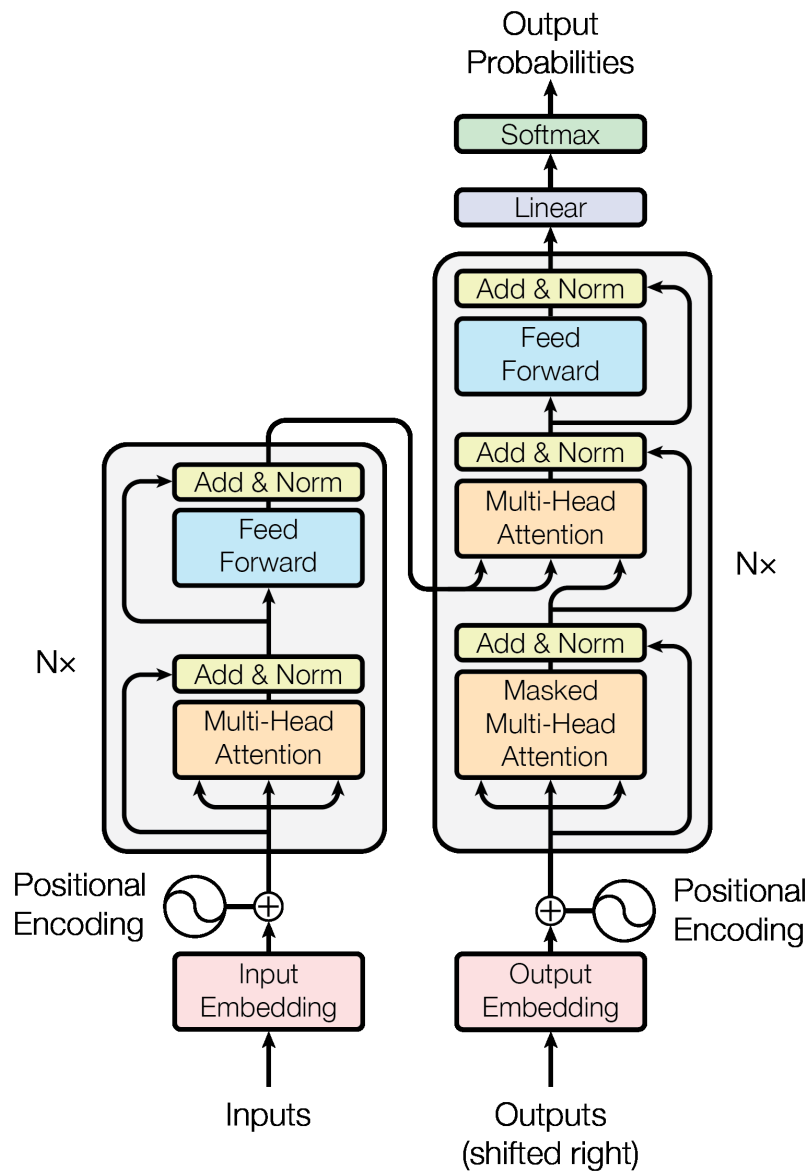
- each node represents a computation
- edges can flow from any node to any other
 - non-cyclic
- multiple inputs, multiple outputs possible

To illustrate the Functional model let's take a first look at model implementing a single Transformer block

- we will revisit this code later to illustrate other concepts

Here is the picture of a Transformer block

Transformer (Encoder/Decoder)



We can identify some connections that *don't* flow sequentially between adjacent nodes

- the *skip connection* that bypasses
 - the Multi-Head Attention node in the Encoder and the top Multi-Head Attention node in the Decoder
 - the Masked Multi-Head Attention node in the Decoder
- the connection from the output of the Encoder (top left) to the input of the Decoder Multi-Head Attention node

The Functional Model architecture, in code

reference (<https://www.tensorflow.org/guide/keras/functional>).

In the Sequential model, the output of the node representing layer l is *always* fed to the input of the node representing layer $(l + 1)$

- So can describe the computation graph as a sequence of nodes (each node a Layer type)

In the Functional model a node represents a function that takes one or more inputs and produces an output

- the node does not need to be a Layer
 - any TensorFlow op
- we connect the output of node N_a to the input of node N_b
 - by assigning the output of N_a to a variable (typically denoted as x)
 - calling the computation of N_b with the variable as actual parameter

Here is an example ([source](https://www.tensorflow.org/api_docs/python/tf/keras/Model)
(https://www.tensorflow.org/api_docs/python/tf/keras/Model))

```
import tensorflow as tf

inputs = tf.keras.Input(shape=(3,))
x = tf.keras.layers.Dense(4, activation=tf.nn.relu)(inputs)
outputs = tf.keras.layers.Dense(5, activation=tf.nn.softmax)(x)
model = tf.keras.Model(inputs=inputs, outputs=outputs)
```


- There is an Input layer (a function with no argument) whose output is assigned to variable `inputs`
- There is a Dense layer (a function with a single argument and single output)
 - that is called with parameter `inputs`
 - assigns its result to variable `x`

In general, these variables could be used as arguments (i.e., node inputs) anywhere in the computation

- not necessarily the next function appearing sequentially

The collection (not necessarily a sequence) of function calls defines a *Directed Acyclic Graph*

- one or more *root* nodes representing graph inputs
- one or more *leaf* nodes representing graph outputs

The graph encodes a complex function mapping inputs to outputs, composed of simpler functions.

The graph can be used to implement

- a new Layer
- a complete Model

To turn this collection into a Model

- we specify the input nodes
- we specify the output nodes

For example, for the above graph:

```
model = tf.keras.Model(inputs=inputs, outputs=outputs)
```

When `model` is *called*

- the actual parameters are bound to the nodes identified as inputs
 - i.e., `inputs`
- the result of the call are the values associated with the nodes identified as
 - i.e., `outputs``

Since a graph can have multiple inputs and outputs

- the input and output parameters of the `Model` statement can be *lists*

Model reference (https://www.tensorflow.org/api_docs/python/tf/keras/Model).

Example: multiple inputs and outputs

Here is an example (taken from [the reference](https://www.tensorflow.org/guide/keras/functional#models_with_multiple_inputs_and_outputs)
(https://www.tensorflow.org/guide/keras/functional#models_with_multiple_inputs_and_outputs))

- Takes three inputs: title, body, tags
 - title: sequence of `int`
 - body: sequence of `int`
 - tags: binary vector (of length `num_tags`)
 - Reduces each variable length sequence to a fixed length representation (final state of an LSTM)
 - Concatenates the fixed length representations of title and body with the tags
 - Feeds the concatenated vector to **two separate classifiers**
 - Produces two outputs
 - priority: the output of one classifier
 - department: the output of the other classifier
-


```
In [3]: num_tags = 12  # Number of unique issue tags
num_words = 10000  # Size of vocabulary obtained when preprocessing text data
num_departments = 4  # Number of departments for predictions

title_input = keras.Input(
    shape=(None,), name="title"
)  # Variable-length sequence of ints
body_input = keras.Input(shape=(None,), name="body")  # Variable-length sequence
of ints
tags_input = keras.Input(
    shape=(num_tags,), name="tags"
)  # Binary vectors of size `num_tags`

# Embed each word in the title into a 64-dimensional vector
title_features = layers.Embedding(num_words, 64)(title_input)
# Embed each word in the text into a 64-dimensional vector
body_features = layers.Embedding(num_words, 64)(body_input)

# Reduce sequence of embedded words in the title into a single 128-dimensional v
ector
title_features = layers.LSTM(128)(title_features)
# Reduce sequence of embedded words in the body into a single 32-dimensional vec
tor
body_features = layers.LSTM(32)(body_features)

# Merge all available features into a single large vector via concatenation
x = layers.concatenate([title_features, body_features, tags_input])

# Stick a logistic regression for priority prediction on top of the features
priority_pred = layers.Dense(1, name="priority")(x)
# Stick a department classifier on top of the features
department_pred = layers.Dense(num_departments, name="department")(x)

# Instantiate an end-to-end model predicting both priority and department
model = keras.Model(
```



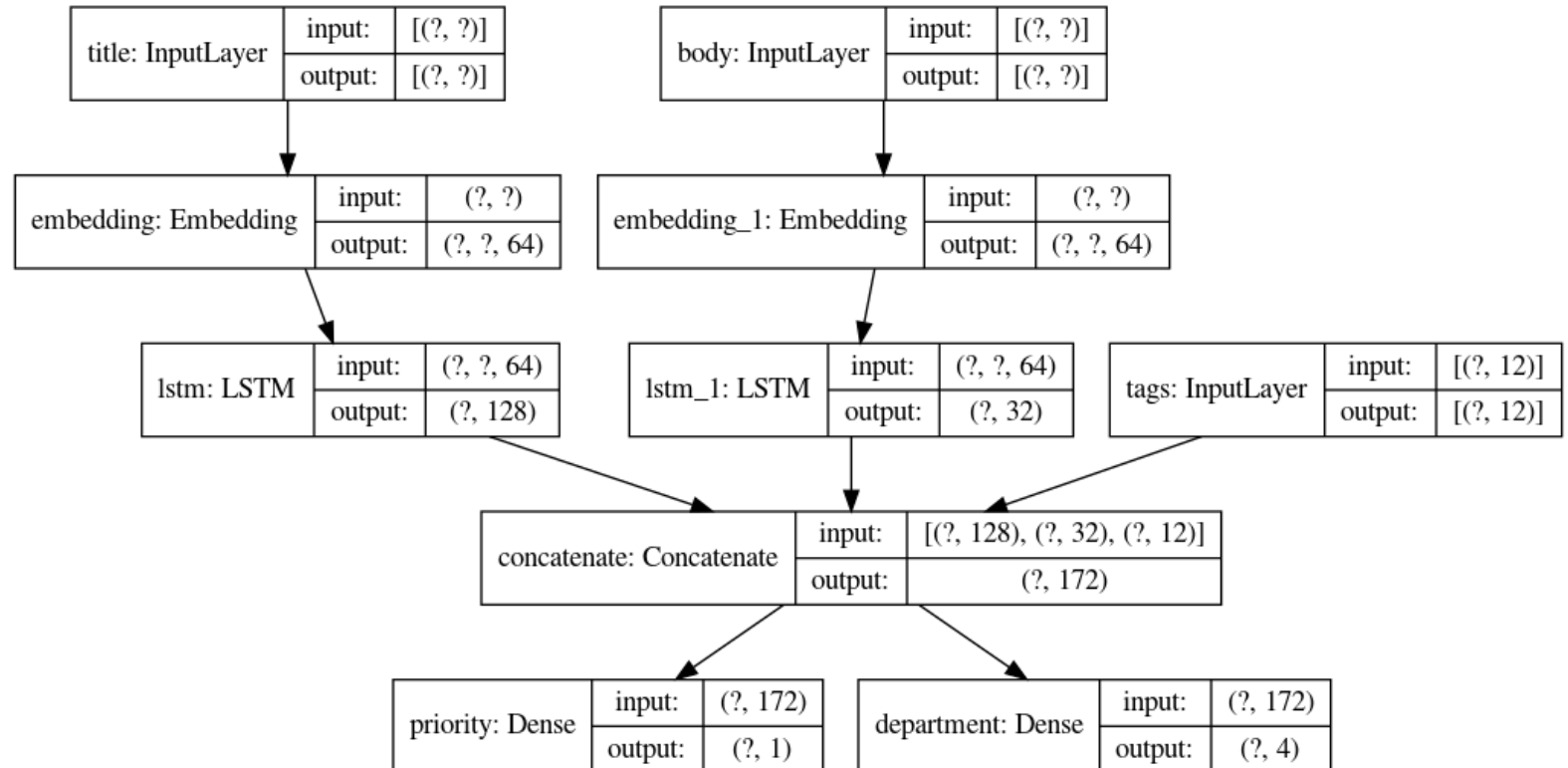
```

inputs=[title_input, body_input, tags_input],
outputs=[priority_pred, department_pred],
)

```

In [4]: `keras.utils.plot_model(model, os.path.join(tempdir, "multi_input_and_output_model.png"), show_shapes=True)`

Out[4]:



Observe

- The 3 input nodes
 - separate processing path
- The 2 output nodes
 - separate classifiers

Sub-classing models/layers

One can create a new `Model` / `Layer` by sub-classing from the base types `tf.keras.Model` / `tf.keras.layers.Layer`

- can override existing methods of a `Model`
 - e.g., a custom training step (invoked by `fit`)
- can build new `Layer` types

Here is an example (taken from [the reference](https://www.tensorflow.org/guide/keras/functional#functional_api_strengths)
(https://www.tensorflow.org/guide/keras/functional#functional_api_strengths))

```
In [11]: class MLP(keras.Model):

    def __init__(self, **kwargs):
        super(MLP, self).__init__(**kwargs)
        self.dense_1 = layers.Dense(64, activation='relu')
        self.dense_2 = layers.Dense(10)

    def call(self, inputs):
        x = self.dense_1(inputs)
        return self.dense_2(x)

# Instantiate the model.
mlp = MLP()
# Necessary to create the model's state.
# The model doesn't have a state until it's called at least once.
_ = mlp(tf.zeros((1, 32)))
```

Key points:

- Notice that the components of the Model
 - are instantiated in the **constructor** (`__init__`)
 - invoked in the `call`
 - the `call` method is invoked when you apply actual parameters to the Model

`_ = mlp(tf.zeros((1, 32)))`

- What would happen if you instantiated the components in the `call`?

```
def call(self, inputs):  
    x = layers.Dense(64, activation  
='relu')(inputs)  
    return layers.Dense(10)(x)
```


It would probably **not** be what you expected

- Instantiating the components in `__init__` results in them being defined **once**
- Instantiating the components in `call` results in them being defined separately **each time** the `Model` is called
 - weights **are not shared** between component instances
 - `call` is invoked for each step in training
 - would not learn weights of the component since they would be initialized for each batch of examples

Fitting a model with multiple inputs, multiple outputs

There is a technical question as to how we distinguish among the `Input` s so we can connect it to the desired variable.

In our basic introduction to Keras, the `fit` method described its training data simply

- Two numpy arrays: one for features, one for labels
 - an element of the first array are features of a single example
 - an element of the second array is the label of a single example (for supervised learning)

A careful examination of the [fit method](https://keras.io/api/models/model_training_apis/#fit-method) (https://keras.io/api/models/model_training_apis/#fit-method) describes *multiple* ways to pass train examples (and labels) to a model

- The common `x=...`, `y=...`
 - In its simplest form:
 - `x` and `y` are `numpy`` arrays (one element per example)
- More general form
 - both the `x` and `y` can be lists
 - Functional models may define multiple *positional* (first, second, etc.) inputs and outputs
 - The `x` list: one element per input
 - The `y` list: one element per output
 - models with multiple unnamed inputs or model outputs
 - `x` can be a `dict`
 - A Functional model with multiple *named* inputs
 - the keys of the `dict` are the names of the inputs
- Tensors
 - can pass the Tensor to a *non-Input* layer
- Dataset
- Generator
 - for (feature, label) pairs when training

Specifying batches

Also: remember that Models process *batches* of examples (in fitting and predicting

- So the variables passed to Input layers should be *groups* of examples, not a single example
 - a single example is represented as a group of size 1

Creating batches is **done for you** when using the common `x= . . . , y= . . . , batch_size= . .` calling method

- The Dataset **needs to create the batches** when used as the calling method
 - there is always a "batch" dimension, even if the batch size is 1
 - there is no `batch_size` argument when the inputs are Dataset's
 - we will learn about the batch operator for transforming an un-batched Dataset into one with batches

Example: Multiple Loss functions from multiple outputs

In discussing multiple outputs, we skipped over an important point

- Loss is associated with an output
- When there are multiple outputs
 - there is a separate loss per output

Technical issue

- How do we specify the loss per output
- How do we combine multiple losses into a single loss, for training

Referring back to our example of multiple inputs/outputs (solving for priority and department)

- we specify a loss for each output
 - with a `dict` that maps a node name to a loss
 - the outputs have been named "priority" and "department"

```
priority_pred = layers.Dense  
(1, name="priority")(x)  
department_pred = layers.Den  
se(num_departments, name="depa  
rtment")(x)
```

Note how in the `fit` call

- we identify the multiple inputs by the names of their `Input` nodes
- using a `dict` as parameter

```
In [12]: model.compile(
    optimizer=keras.optimizers.RMSprop(1e-3),
    loss={
        "priority": keras.losses.BinaryCrossentropy(from_logits=True),
        "department": keras.losses.CategoricalCrossentropy(from_logits=True),
    },
    loss_weights={"priority": 1.0, "department": 0.2},
)
```


Note the `loss_weights` parameter

- specifying the relative weight of each loss within the total loss

Here is the call to fit the model:

```
In [13]: # Dummy input data
title_data = np.random.randint(num_words, size=(1280, 10))
body_data = np.random.randint(num_words, size=(1280, 100))
tags_data = np.random.randint(2, size=(1280, num_tags)).astype("float32")

# Dummy target data
priority_targets = np.random.random(size=(1280, 1))
dept_targets = np.random.randint(2, size=(1280, num_departments))

model.fit(
    {"title": title_data, "body": body_data, "tags": tags_data},
    {"priority": priority_targets, "department": dept_targets},
    epochs=2,
    batch_size=32,
)
```

Train on 1280 samples

Epoch 1/2

WARNING:tensorflow:Entity <function Function._initialize_uninitialized_variables.<locals>.initialize_variables at 0x7f632c00e3b0> could not be transformed and will be executed as-is. Please report this to the AutoGraph team. When filing the bug, set the verbosity to 10 (on Linux, `export AUTOGRAPH_VERBOSITY=10`) and attach the full output. Cause: No module named 'tensorflow_core.estimator'

WARNING: Entity <function Function._initialize_uninitialized_variables.<locals>.initialize_variables at 0x7f632c00e3b0> could not be transformed and will be executed as-is. Please report this to the AutoGraph team. When filing the bug, set the verbosity to 10 (on Linux, `export AUTOGRAPH_VERBOSITY=10`) and attach the full output. Cause: No module named 'tensorflow_core.estimator'

1280/1280 [=====] - 5s 4ms/sample - loss: 1.3019 - priority_loss: 0.7016 - department_loss: 3.0018

Epoch 2/2

1280/1280 [=====] - 2s 1ms/sample - loss: 1.2898 - priority_loss: 0.6993 - department_loss: 2.9525

```
Out[13]: <tensorflow.python.keras.callbacks.History at 0x7f62f80a1a50>
```

Gradients

Gradient Descent is the fundamental tool used for optimizing the Loss Function.

When the `fit` method of a `Model` object is called, it runs a *training step* of the `Model` on a mini-batch of training examples.

The default training step of a `Model`

- Runs the *forward* calculation:
 - presenting an input example to the NN inputs
 - calculating the NN outputs by Forward Propagation through the network
 - computing the Loss
 - computing the gradients of the Loss with respect to the NN weights
 - updating the weights in the negative direction of the Gradient

Here is an example (from the notebook on [VAE](https://colab.research.google.com/github/keras-team/keras-io/blob/master/examples/generative/ipynb/vae.ipynb) (<https://colab.research.google.com/github/keras-team/keras-io/blob/master/examples/generative/ipynb/vae.ipynb>) that we will study in depth in the future).

It defines a `Model` sub-type, with its own training step.

```
def train_step(self, data):
    with tf.GradientTape() as tape:
        z_mean, z_log_var, z = self.encoder(data)
        reconstruction = self.decoder(z)
        reconstruction_loss = tf.reduce_mean(
            tf.reduce_sum(
                keras.losses.binary_crossentropy(data, reconstruction), axis=
s=(1, 2)
            )
        )
        kl_loss = -0.5 * (1 + z_log_var - tf.square(z_mean) - tf.exp(z_log_
var))
        kl_loss = tf.reduce_mean(tf.reduce_sum(kl_loss, axis=1))
        total_loss = reconstruction_loss + kl_loss
        grads = tape.gradient(total_loss, self.trainable_weights)
        self.optimizer.apply_gradients(zip(grads, self.trainable_weights))
        self.total_loss_tracker.update_state(total_loss)
        self.reconstruction_loss_tracker.update_state(reconstruction_loss)
        self.kl_loss_tracker.update_state(kl_loss)
    return {
```

In the above example, we override the default training step

- How to override a `Model`'s methods will be a future topic
- The mathematics of the VAE will be a future topic

For now, we focus on the code of the custom training step/

Note

We **didn't** create a `call` method for the `Model`

- we won't ever "call" the VAE model
 - only its encoder and decoder sub-components

The Loss (`total_loss`) consists of two parts

- `kl_loss`
- `reconstruction_loss`

We manually invoke the computation of the Gradient of the Loss

- with respect to the model's weights (`self.trainable_weights`)

```
grads = tape.gradient(total_loss,  
self.trainable_weights)
```

- In order to signal to TensorFlow that gradients are to be calculated for an expression
 - the expression must occur within the scope of a `tf.GradientTape` block

```
with tf.GradientTape() as tape:
```

We manually update the weights in the negative direction of the gradients

```
self.optimizer.apply_gradients(zip(grads,  
self.trainable_weights))
```


We track the total loss as well as it's subparts

```
self.total_loss_tracker.update_state(total_loss)
    self.reconstruction_loss_tracker.update_state(reconstruction_loss)
    self.kl_loss_tracker.update_state(kl_loss)
```

We return 3 losses

```
return {
    "loss": self.total_loss_tracker.result(),
    "reconstruction_loss": self.reconstruction_loss_tracker.result(),
    "kl_loss": self.kl_loss_tracker.result(),
}
```

But the calculation of gradients is powerful apart from deriving a model's weights.

TensorFlow allows you to compute the gradient of any expression with respect to any value on which the expression depends.

Let's visit this notebook on [Gradient Ascent \(Gradient_ascent.ipynb\)](#) to see how gradients can be used to visualize which inputs the various layers of a NN respond to most highly.

```
In [14]: print("Done")
```

Done

