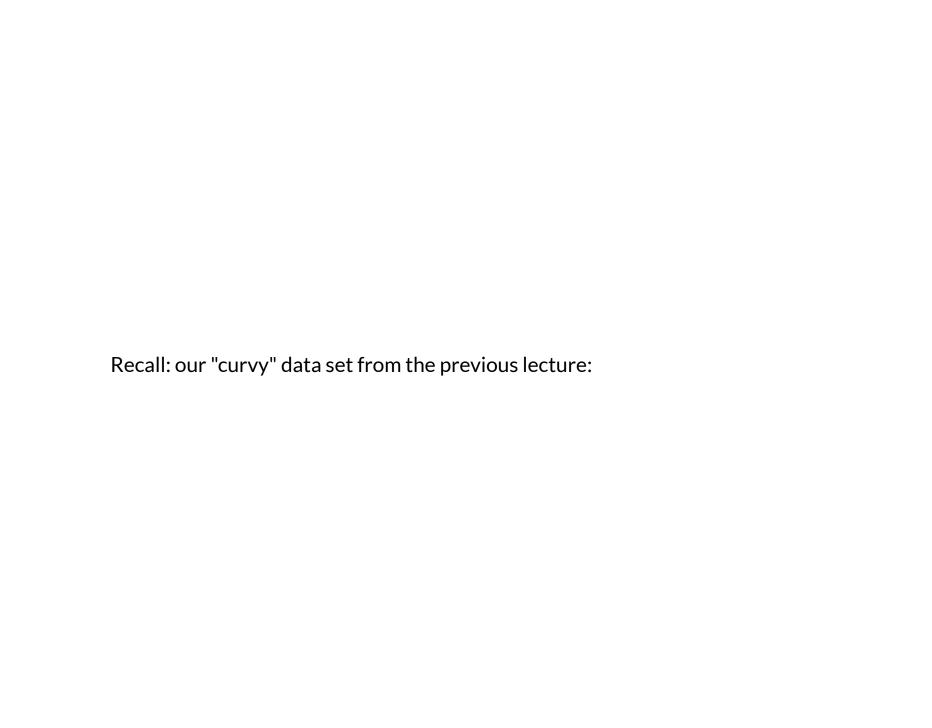
Prepare data: transformations

Transforming data (Recipe C.3) may be **the most important** step of the multi-step Recipe

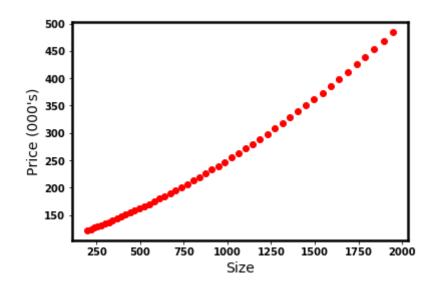
Recipe for Machine Learning

It is often the case that the "raw" features given to us don't suffice

- we may need to create "synthetic" features.
- This is called **feature engineering**.



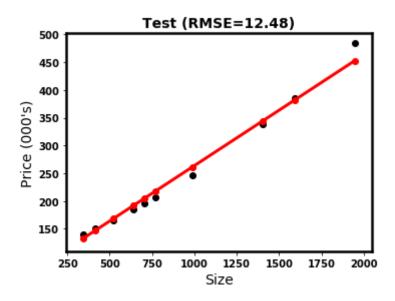
```
In [5]: (xlabel, ylabel) = ("Size", "Price (000's)")
v1, a1 = 1, .005
v2, a2 = v1, a1*2
curv = recipe_helper.Recipe_Helper(v = v2, a = a2)
X_curve, y_curve = curv.gen_data(num=50)
_= curv.gen_plot(X_curve,y_curve, xlabel, ylabel)
```

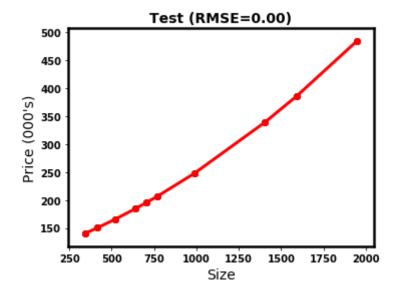


And compare the out of sample performance on this data set

- On a linear model (single, raw feature)
- On a model with a second feature (squared version of raw feature)

In [6]: model_results = curv.compare_regress(X_curve, y_curve, xlabel=xlabel, ylabel=yla
 bel, visible=True, plot_train=False)





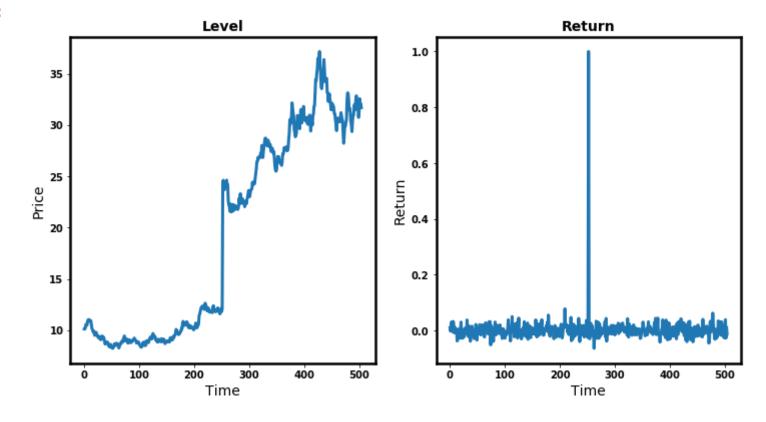




In [7]: | fig

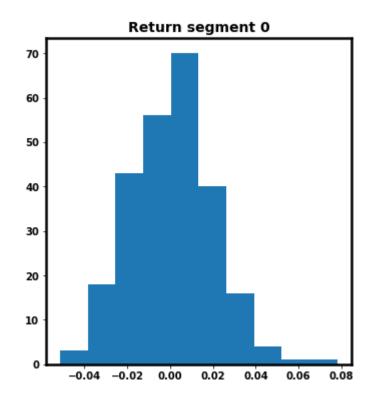
fig_data

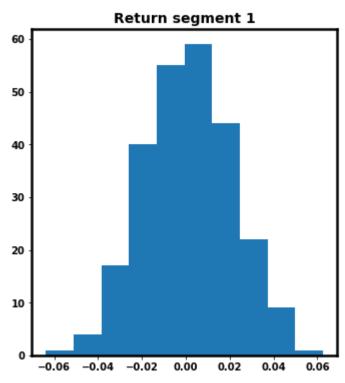
Out[7]:



In [8]: | fig_segs

Out[8]:





We would probably have better luck

- predicting future *returns* from past returns
- compared to predicting future *prices* from past prices

That is: the synthetic feature ("Return") replaces the raw feature ("Price").

We could also argue that adding an additional synthetic feature might facilitate using Price as a feature:
 a time index or indicator (true/false) that identifies examples as being either pre or post jump

It will still be better using Return rather than Level and a segment indicator

- A jump can occur within the training data
 - or each example could drift weakly over time
- Excluding the jump: Returns are stable over time
 - but Price (and Price changes) are not
 - same return applied to a larger Price results in a larger Price change

In order to learn, it helps to have *training* data be more homogeneous

- Can more easily learn a pattern from many examples rather than a handful
- So can benefit from making the training examples more similar to one another
 - not just making training and test examples look similar

Either way: transforming the raw features is key to successful modeling and prediction.

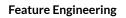
Feature engineering (transformations)

- takes an example: vector $\mathbf{x^{(i)}}$ with n features
- produces a new vector $\tilde{\mathbf{x}}^{(i)}$, with n' features

We ultimately fit the model with the transformed training examples.

We can apply multiple transformations, each

- Adding new synthetic features
- Further transforming synthetic features



The above diagram shows multiple transformations

ullet organized as a sequence (sometimes called a *pipeline*) of independent transformations T_1, T_2, \ldots, T_t

$$egin{align} ilde{\mathbf{x}}_{(1)} &= T_1(\mathbf{x}) \ ilde{\mathbf{x}}_{(2)} &= T_2(ilde{\mathbf{x}}_{(1)}) \ dots \ ilde{\mathbf{x}}_{(l+1)} &= T_{(l+1)}(ilde{\mathbf{x}}_{(l)}) \ \end{aligned}$$

We write the final transformed $\tilde{\mathbf{x}}$ as a function T that is the composition of each transformation function

$$\tilde{\mathbf{x}} = T(\mathbf{x}) = T_t(T_{t-1}(\dots T_1(\mathbf{x})\dots))$$

The length of the final transformed vector $ ilde{\mathbf{x}}$ may differ from the n , the length of the input
• may add features
may drop features

The predictions are now a function of $\tilde{\mathbf{x}}$ rather than \mathbf{x}

$$\hat{\mathbf{y}} = h_{\Theta}(ilde{\mathbf{x}})$$

Example transformation: Missing data imputation

The first transformation we encountered added a feature (\mathbf{x}^2 term) that improved prediction.

Some transformations alter existing features rather than adding new ones.

Transformations in detail will be the subject of a separate lecture but let's cover the basics.

Let's consider a second reason for transformation: filling in (imputing) missing data for a feature.

#	\mathbf{x}_1	$\mathbf{x_2}$
1	1.0	10
2	2.0	20
:	:	:
i	2.0	NaN
:	:	:
m		

In the above: feature ${f x}_2$ is missing a value in example i: ${f x}_2^{({f i})}={
m NaN}$

We will spend more time later discussing the various ways to deal with missing data imputation.

For now: let's adopt the common strategy of replacing it with the median of the defined values:

$$\operatorname{median}(\mathbf{x}_2) = \operatorname{median}(\{\mathbf{x}_2^{(\mathbf{i})} | 1 \leq i \leq m, \mathbf{x}_2^{(\mathbf{i})} \neq \operatorname{NaN}\})$$

"Fitting" transformations

The behavior of our models for prediction have parameters Θ .

It might not be obvious that transformations have parameters $\Theta_{\mathrm{transform}}$ as well

$$ilde{\mathbf{x}} = T_{\Theta_{ ext{transform}}}(\mathbf{x})$$

For example: when missing data imputation for a feature substitutes the mean/median feature value

• $\Theta_{
m transform}$ stores this value

We use the term "fitting" to describe the process of solving for $\Theta_{\rm transform}$

 $\bullet~$ Unlike $\Theta,$ one doesn't usually find a "optimal" value for $\Theta_{transform}$

Our prediction is thus

$$egin{array}{lll} \hat{\mathbf{y}} &=& h_{\Theta}(ilde{\mathbf{x}}) \ &=& h_{\Theta}(\,T_{\Theta_{ ext{transform}}}(\mathbf{x})\,) \end{array}$$

The process of Transformations is similar to fitting a model and predicting.

The parameters in $\Theta_{transform}$

- ullet are "fit" by examining all training data $oldsymbol{X}$
- once fit, we can transform ("predict") *any* example (whether it be training/validation or test)

Applying transformations consistently

Since the prediction is now

$$\hat{\mathbf{y}} = h_{\Theta}(\, ilde{\mathbf{x}} \,) \quad ext{where } ilde{\mathbf{x}} = T_{\Theta_{ ext{transform}}}(\mathbf{x})$$

each and every input ${f x}$ must be transformed

- Training examples
- Test examples

That is: the transformation is applied consistently across all examples, regardless of their source
If we didn't apply the same transformation to both training and test examples
We would violate the Fundamental Assumption of Machine Learning

However

- $\bullet \ \ \Theta_{transform}$ is fit **only** to training examples
- It is **not** recalculated on a set of test examples

Here's the picture



There are several reasons not to re-fit on test examples

- It would be a kind of "cheating" to see all test examples (required to fit)
- You should assume that you only encounter one test example at a time, not as a group

Pipelines in sklearn

We will see a real use case for Pipelines in a subsequent lecture.

For now, we only give a preview to illustrate the highlights.

Transformations in sklearn respond to the methods fit and transform sklearn provides a Pipeline object

- a container for a list of objects that respond to fit and transform (e.g., Transformations)
- applying fit (resp., transform) to a Pipeline object will apply the method to each element of the list, in sequence

So the Pipeline object in sklearn is a convenient way of bundling multiple transformations.

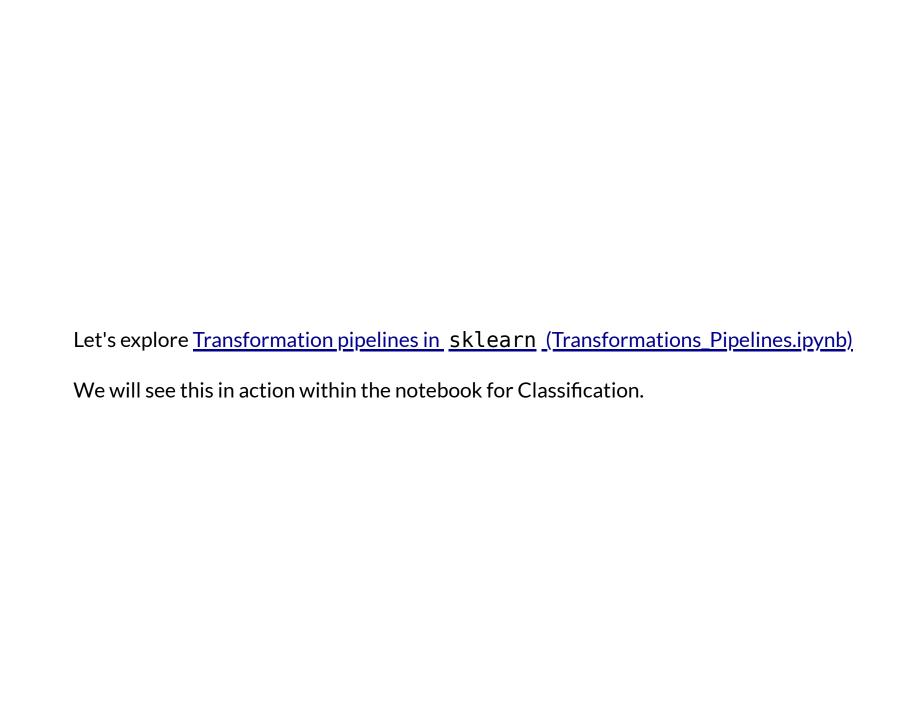
This will make it easier to apply the entire set of transformations consistently (to insample and out of sample examples)

You may also recall that models in sklearn also respond to methods fit and transform.

We will see that you can also place a model object in a Pipeline (usually as the last element of the list).

One benefit of doing so is that the entire process of (transformations + modeling) is neatly wrapped into a single object (promoting consistency).

But we will also see that it facilitates the avoidance of the subtle problem of "cheating in cross validation".



Using pipelines to avoid cheating in cross validation

Although we start off with the best intentions, it is easy to accidentally "cheat"

- When we combine transformations and cross-validation (to measure out of sample performance)
- Is surprisingly common!

k-fold cross-validation:

- ullet Divides the training examples into k "folds"
- A model is fit *k* times
- Each fit
 - Uses (k-1) folds for training
 - The remaining fold is considered "out of sample" for that fit
- ullet This gives us k Performance Metrics: a distribution of out of sample performance

Cross Validation/Test split

Consider the difference between fitting $\Theta_{\mathrm{transform}}$

- Once, on all the training examples, before applying cross-validation
- ullet Separately for each of the k fits of Cross-Validation
 - Using the (k-1) folds used for training in this fit

For example, when Fold_k is out of sample

 $\Theta_{ ext{transform}} = f([ext{Fold}_1, ext{Fold}_2, \dots ext{Fold}_{k-1}, ext{Fold}_k])$

versus

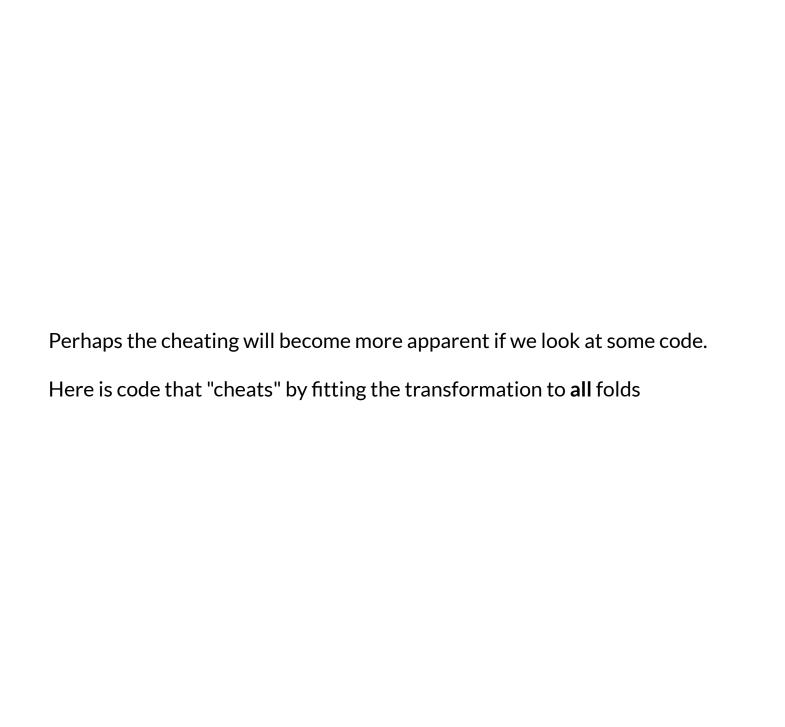
 $\Theta_{ ext{transform}} = f([ext{Fold}_1, ext{Fold}_2, \dots ext{Fold}_{k-1})$

In the first case, we are cheating!

- ullet Fold k is out of sample for this fit
- ullet And should **not** influence $\Theta_{\mathrm{transform}}$

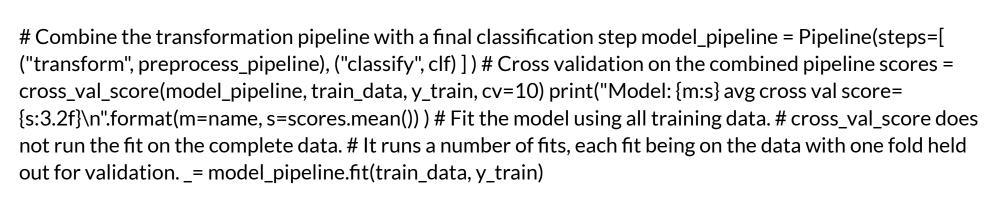
The second case avoids this problem

- With seemingly a lot more work
- $\bullet \;\; \mbox{Fitting} \; \Theta_{transform} \; \mbox{multiple times}$



Transform the data X_train = preprocess_pipeline.fit_transform(train_data) # Cross validation scores = cross_val_score(clf, X_train, y_train, cv=10) print("Model: $\{m:s\}$ avg cross val score= $\{s:3.2f\}$ \n".format(m=name, s=scores.mean())) # Fit the model using all training data. # cross_val_score does not run the fit on the complete data. # It runs a number of fits, each fit being on the data with one fold held out for validation. _= clf.fit(X_train, y_train)

And here is code that does not cheat: the transformation is fit only to the folds that a in-sample during cross validation



cross_val_score

- Divides train data into folds
- For each fold f
 - Splits train_datainto
 - \circ set of folds F excluding f
 - \circ uses f as out of sample
 - \blacksquare Applies the first argument (e.g., model_pipeline rather than the model object clf) to F
 - Resulting in the preprocess_pipeline and model object being applied to all folds except f
- The result is that there is one score (Performance metric) computed for each fold (when that fold is out of sample)

```
In [9]: print("Done")
```

Done