# Functional Programming 2: Defining Data Types

CS 350

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# Warmup: Pairs

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```
(define myPair : (Number * Boolean)
  (pair 2 #t))
(fst myPair) ;;Number
(snd myPair) ;;Boolean
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2
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**Algebraic Data Types** 

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- Racket lets us define our own types mixing AND and OR

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  - Depending on the tag

# **Auto-generated Functions**

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```
(Rectangle? tv)
(Circle? tv)
(Rectangle-length tv)
;; (test/exn (Circle-radius tv) "")
;;raises an error, no such field present
```

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```
144
3.14
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  - See Racket window

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(define-type (Optionof 'a)
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  (some [v : 'a]))
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- Pattern matching guarantees no null pointer errors
  - We'll see a more detailed example

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- e.g. Shape is (Either (Number \* Number) Number)

# Recursive Data

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- Data can be traversed using recursion

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```
(define-type Filesystem
  (File [name : String]
       [data : Number])
  (Folder [name : String]
       [contents : (Listof Filesystem)]))
```

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# **Testing the search**

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```
(define InnerSolarSystem
 (Folder "Sun"
          (list (File "Mercury" 1)
                (File "Venus" 2)
                (Folder "EarthSystem"
                        (list (File "Earth" 3)
                              (File "Moon" 3.5)))
                (Folder "MarsSystem"
                        (list (File "Mars" 4)
                              (File "Phobos" 4.3)
                              (File "Diemos" 4.6))))))
(search "Moon" InnerSolarSystem)
(search "Jupiter" InnerSolarSystem)
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(search "Moon" InnerSolarSystem)
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```

```
(some 3.5)
(none)
```