

Implementing Lambdas with Environments: Closures

CS 350

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Broad Goals

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- Implement an interpreter for a Curly variant with functions

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Key Concepts

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Key Concepts

- Definition of a closure

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Key Concepts

- Definition of a closure
- Static and Dynamic Scope for first-class functions

The Details

Substitution to Environment, Review

- Interpreter takes environment argument

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- Interpreter takes environment argument

```
(define (interp [env : Env]
               [expr : Expr])
  : Value ;; Was Number
  ....)
```

- Function-calls evaluate body in environment containing argument

- Exact same as Curly-Lambda substitution version

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```
(define-type Expr
  ....
  (Fun [arg : Symbol]
       [body : Expr]))
```

- Goal is to interpret the same language, but with environments

A (Wrong) First Attempt: Values

- Define `Value` just like in substitution version

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A (Wrong) First Attempt: Values

- Define Value just like in substitution version
 - Functions consist of their argument and the body to execute

```
(define-type Value
  (NumV [num : Number])
  (FunV [arg : Symbol]
        [body : Expr]))
```

A Wrong First Attempt: Functions Interp

- As a first attempt, try building functions just like in substitution version

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- As a first attempt, try building functions just like in substitution version

```
(define (interp env expr)
  (type-case Expr interp
    ....
    [(Fun x body)
     (FunV x body)] ))
```

A Wrong First Attempt: Calls Interp

- Just like before

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- Interpret function body in the environment with the parameter bound to the argument's value

```
(define (interp env expr)
  (type-case Expr interp
    ....
    [(Call funExpr argExpr)
     (let* ([argVal (interp argExpr)]
            [funVal (checkAndGetFun (interp funExpr))]
            [funParam (fst funVal)]
            [funBody (snd funVal)])
       (interp (extendEnv (bind funParam argVal)
                          env) ;;<-----
               funBody))] )])
```


The problem

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- With a lambda, there could have been many substitutions that were applied to its free variables
 - With substitutions, the variables get replaced in the lambda
 - With environments, the variables aren't replaced *until we interpret the body*
- When we actually go to interpret the body, we don't have the environment that the function was created in
 - Just the environment from the time of the call
- We've implemented **dynamic scoping** by accident!

The Solution: Closures

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 - The combination of a function variable+body and an environment is called a **closure**

The Solution: Closures

- A function should be *closed* over its environment at the point it's created (interpreted)
- So we add an extra piece of data to the `Value` variant for functions: the environment at the time of creation
 - The combination of a function variable+body and an environment is called a **closure**
- Closures give environment interpreters the same behavior as substitution interpreters

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 - We can still create functions dynamically
 - But once created they're static

The New Value Type

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```
(define-type Value
  (NumV [num : Number])
  ;; Like FunV but with an environment
  (ClosureV [arg : Symbol]
             [body : Expr]
             [env : Env]))
```


A New Dynamic Type Checker

- Same idea as `checkAndGetFun`, just has an extra piece of data to retrieve

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```
(define (checkAndGetClosure [v : Value]) : ((Symbol * Expr) * Env)
  (type-case Value v
    [(ClosureV x body env)
     (pair (pair x body) env)]
    [else
     (error 'curlyTypeError
            (string-append "Expected Function, got number:"
                           (to-string v)))]))
```

Properly Interpreting Functions

- When we interpret a lambda, *package the current environment up with it*

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```
(define (interp env expr)
  (type-case Expr interp
    ....
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     (ClosureV x body env) ;;<-----
    ] ))
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- When we call a function, extend *the environment that was packaged up with it*

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```
(define (interp env expr)
  (type-case Expr interp
    ....
    [(Call funExpr argExpr)
     (let* ([argVal (interp argExpr)]
            [funVal (checkAndGetClosure (interp funExpr))]
            [funParam (fst (fst funVal))]
            [funBody (snd (fst funVal))]
            [funEnv (snd funVal)])
       (interp (extendEnv (bind funParam argVal)
                          funEnv) ;;<-----
                funBody))] )
```

Summary: Dynamic vs. Static Scope

- Free variables in a function body are variables that are not defined/bound in that function body

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- Free variables in a function body are variables that are not defined/bound in that function body
- Static scope gives free variables values from the environment when the function was *constructed*
- Dynamic scope gives variables values from the environment when the function was *called*

Example: Static Scope

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```
{letvar double {fun {x} {* x 2}}  
  {letvar quadruple {fun {y} {double {double y}}}  
    {letvar double 2  
      {quadruple 3}}}}
```

- {fun {y} {double {double x}}}
 has one free variable, double

Example: Static Scope

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{letvar double {fun {x} {* x 2}}  
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- {fun {y} {double {double x}}}
 variable, double
 - Functions and variables are in *the same namespace* in Curly-Lambda

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- {fun {y} {double {double x}}}
 variable, double
 - Functions and variables are in *the same namespace* in Curly-Lambda
- {fun {y} {double {double x}}}
 evaluates to closure

Example: Static Scope

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{letvar double {fun {x} {* x 2}}  
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      {quadruple 3}}}}
```

- `{fun {y} {double {double x}}}` has one free variable, `double`
 - Functions and variables are in *the same namespace* in Curly-Lambda
- `{fun {y} {double {double x}}}` evaluates to closure
 - Body is `{double {double x}}`

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```
{letvar double {fun {x} {* x 2}}  
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 - Functions and variables are in *the same namespace* in Curly-Lambda
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 - Body is `{double {double x}}`
 - Env is `double := {fun {x} {* x 2}}`

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{letvar double {fun {x} {* x 2}}  
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- `{fun {y} {double {double x}}}` has one free variable, `double`
 - Functions and variables are in *the same namespace* in Curly-Lambda
- `{fun {y} {double {double x}}}` evaluates to closure
 - Body is `{double {double x}}`
 - Env is `double := {fun {x} {* x 2}}`
- Env at call:

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{letvar double {fun {x} {* x 2}}  
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- `{fun {y} {double {double x}}}` has one free variable, `double`
 - Functions and variables are in *the same namespace* in Curly-Lambda
- `{fun {y} {double {double x}}}` evaluates to closure
 - Body is `{double {double x}}`
 - Env is `double := {fun {x} {* x 2}}`
- Env at call:
 - `double := 2`

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{letvar double {fun {x} {* x 2}}  
  {letvar quadruple {fun {y} {double {double y}}}  
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- `{fun {y} {double {double x}}}` has one free variable, `double`
 - Functions and variables are in *the same namespace* in Curly-Lambda
- `{fun {y} {double {double x}}}` evaluates to closure
 - Body is `{double {double x}}`
 - Env is `double := {fun {x} {* x 2}}`
- Env at call:
 - `double := 2`
 - `quadruple := {fun {y} {double {double x}}}`

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{letvar double {fun {x} {* x 2}}  
  {letvar quadruple {fun {y} {double {double y}}}  
    {letvar double 2  
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- `{fun {y} {double {double x}}}` has one free variable, `double`
 - Functions and variables are in *the same namespace* in Curly-Lambda
- `{fun {y} {double {double x}}}` evaluates to closure
 - Body is `{double {double x}}`
 - Env is `double := {fun {x} {* x 2}}`
- Env at call:
 - `double := 2`
 - `quadruple := {fun {y} {double {double x}}}`
 - `double := {fun {x} {* x 2}}`

Example: Static Scope ctd

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```
{letvar double {fun {x} {* x 2}}  
  {letvar quadruple {fun {y} {double {double x}}}  
    {letvar double 2  
      {quadruple 3}}}}
```

- Call evaluates quadruple to closure

Example: Static Scope ctd

```
{letvar double {fun {x} {* x 2}}  
  {letvar quadruple {fun {y} {double {double x}}}  
    {letvar double 2  
      {quadruple 3}}}}
```

- Call evaluates quadruple to closure
- Finally evaluates {double {double x}}

Example: Static Scope ctd

```
{letvar double {fun {x} {* x 2}}  
  {letvar quadruple {fun {y} {double {double x}}}  
    {letvar double 2  
      {quadruple 3}}}}}
```

- Call evaluates quadruple to closure
- Finally evaluates {double {double x}}
 - In extended closure environment:

Example: Static Scope ctd

```
{letvar double {fun {x} {* x 2}}  
  {letvar quadruple {fun {y} {double {double x}}}  
    {letvar double 2  
      {quadruple 3}}}}}
```

- Call evaluates `quadruple` to closure
- Finally evaluates `{double {double x}}`
 - In extended closure environment:
 - `x := 3`

Example: Static Scope ctd

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{letvar double {fun {x} {* x 2}}  
  {letvar quadruple {fun {y} {double {double x}}}  
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- Call evaluates `quadruple` to closure
- Finally evaluates `{double {double x}}`
 - In extended closure environment:
 - `x := 3`
 - `double := {fun {x} {* x 2}}`

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  {letvar quadruple {fun {y} {double {double x}}}  
    {letvar double 2  
      {quadruple 3}}}}
```

- Call evaluates `quadruple` to closure
- Finally evaluates `{double {double x}}`
 - In extended closure environment:
 - `x := 3`
 - `double := {fun {x} {* x 2}}`
- Result is 12

Example: Dynamic Scope

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{letvar double {fun {x} {* x 2}}  
  {letvar quadruple {fun {y} {double {double x}}}  
    {letvar double 2  
      {quadruple 3}}}}
```

- {fun {y} {double {double x}}}
 evaluates to
 closure

Example: Dynamic Scope

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{letvar double {fun {x} {* x 2}}  
  {letvar quadruple {fun {y} {double {double x}}}  
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```

- {fun {y} {double {double x}}}
 closure
 - Doesn't save environment

Example: Dynamic Scope

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 closure
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- Call evaluates {double {double x}}
 - In extended *call site* environment:

Example: Dynamic Scope

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 - In extended *call site* environment:
 - $x := 3$

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 closure
 - Doesn't save environment
- Call evaluates {double {double x}}
 - In extended *call site* environment:
 - x := 3
 - double := 2

Example: Dynamic Scope

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 closure
 - Doesn't save environment
- Call evaluates {double {double x}}
 - In extended *call site* environment:
 - $x := 3$
 - $\text{double} := 2$
 - $\text{quadruple} := \{\text{fun } \{y\} \{\text{double } \{\text{double } x\}\}\}$

Example: Dynamic Scope

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{letvar double {fun {x} {* x 2}}  
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 closure
 - Doesn't save environment
- Call evaluates {double {double x}}
 - In extended *call site* environment:
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 - double := 2
 - quadruple := {fun {y} {double {double x}}}
 - double := {fun {x} {* x 2}}

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- Call evaluates {double {double x}}
 - In extended *call site* environment:
 - `x := 3`
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 - `quadruple := {fun {y} {double {double x}}}`
 - `double := {fun {x} {* x 2}}`
- Dynamic type error

Example: Dynamic Scope

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 - In extended *call site* environment:
 - `x := 3`
 - `double := 2`
 - `quadruple := {fun {y} {double {double x}}}`
 - `double := {fun {x} {* x 2}}`
- Dynamic type error
 - Can't call 2 as a function

**But Professor, When Will I Ever
Use This?**

Python:

Python:

Static Scoping in the Wild

Python:

```
timesTwo = lambda x : 2 * x
quadruple = lambda y : timesTwo(timesTwo(y))
def mainFun(x):
    timesTwo = 2.0
    return quadruple(x)
return mainFun(3)
```

12

Result:

12

JavaScript:

JavaScript:

Static Scoping in the Wild

JavaScript:

```
var timesTwo = function (x) { return x * 2 };  
var quadruple =  
    function (x) {return timesTwo(timesTwo(x)) };  
function mainFun(x){  
    var timesTwo = 2.0;  
    return quadruple(x)}  
return mainFun(3)
```

12

Result:

12

Async in JavaScript

- From the w3schools async tutorial

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Async in JavaScript

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```
async function myFunction() {  
  return "Hello";  
}  
myFunction().then(  
  function(value) {myDisplayer(value);}  
);
```

- `myFunction.then` is a higher order function

Async in JavaScript

- From the w3schools async tutorial

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async function myFunction() {  
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 - Takes in another function as an argument

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 - Takes in another function as an argument
- They call the function argument the *callback*

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 - Takes in another function as an argument
- They call the function argument the *callback*
- `function(value)` is just the Javascript syntax for lambda

Async in JavaScript

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async function myFunction() {  
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- `myFunction.then` is a higher order function
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- They call the function argument the *callback*
- `function(value)` is just the Javascript syntax for lambda
 - Dynamically creates the function that is run when `myFunction` actually runs

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- `myFunction.then` is a higher order function
 - Takes in another function as an argument
- They call the function argument the *callback*
- `function(value)` is just the Javascript syntax for lambda
 - Dynamically creates the function that is run when `myFunction` actually runs
- Concurrency in JS is mostly just syntactic sugar for lambda/higher-order functions

And More

- Swift “Closures” are just lambdas

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- Swift “Closures” are just lambdas

```
names.sorted(by:
    { (s1: String, s2: String) -> Bool
        in return s1 > s2
    } )
```

- C++11 added anonymous functions

And More

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```
sort(V.begin(), V.end(), [](auto& a, auto& b)
{
    return a > b;
});
```

- Java 8 added anonymous functions

And More

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});
```

- Java 8 added anonymous functions

```
Arrays.sort(arr,  
    (String a, String b) ->  
        a.length() - b.length());
```

- This is all just lambda with different syntax