# **Arithmetic: Our First Interpreter**

CS 350

Dr. Joseph Eremondi

Last updated: July 9, 2024

# Interpreters: Overview







Alonzo Church

Kurt Gödel

Alan Turing

(lambda calculus) (general recursive functions)

(Turing machines)

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All Turing Complete Languages can simulate each other

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  - Sometimes you can piggyback on the implementation language features, but that's a matter what's convenient, not what's possible

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  - We'll call them "Curly" because we write them with curly brackets
  - Write Curly programs in Racket files using quotation

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  - Initially we have no context arguments, and Value is very simple
  - o Will get more complicated as we go through the course

```
(define-type Expr
  (NumLit [n : Number])
  (Plus [left : Expr]
        [right : Expr])
  (Times [left : Expr]
        [right : Expr]))
```

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    - Interpret sub-expressions recursively
    - Combine according to value version of the operation

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```
3
7
15
```

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- Example: {ifo cond x y}
  - o Evaluates to x if cond evaluates to 0
  - Evaluates to y if cond evaluates to anything else

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```
[(s-exp-match? `{ifo ANY ANY ANY} s)
  (Ifo (parse (second (s-exp->list s)))
            (parse (third (s-exp->list s))
            (parse (fourth (s-exp->list s))]
```

# **Updating the interpreter**

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```
(define (interp [e : Expr] ) : Number
 (type-case Expr e
             [(NumLit n) n]
             [(Plus l r)
                (+ (interp l) (interp r))]
             [(Times l r)
                (* (interp l) (interp r))])
             [(Ifo test thenBranch elseBranch)
               (if (= ⊙ (interp test))
                 (interp thenBranch)
                 (interp elseBranch)
               )])
```