Exercises #2

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Exercise 1.1

- **a.** $M_1:q_1$ $M_2:q_1$
- **b.** $M_1:\{q_2\}$ $M_2:\{q_1,q_4\}$
- **c.** $M_1:q_1 \to q_2 \to q_3 \to q_1 \to q_1$ $M_2:q_1 \to q_1 \to q_1 \to q_2 \to q_4$
- **d.** M_1 : No M_2 : Yes
- e. M_1 : No M_2 : Yes

Exercise 1.2

$$\begin{aligned} M_1 &= (\{q_1,q_2,q_3\},\{\mathbf{a},\,\mathbf{b}\},\delta_1,q_1,\{q_2\}) \\ M_2 &= (\{q_1,q_2,q_3,q_4\},\{\mathbf{a},\,\mathbf{b}\},\delta_2,q_1,\{q_1,q_4\}) \end{aligned}$$

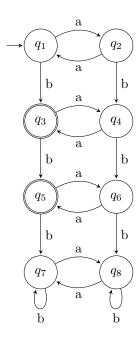
$$\begin{array}{c|cccc} \delta_1 & a & b \\ \hline q_1 & q_2 & q_1 \\ q_2 & q_3 & q_3 \\ q_3 & q_2 & q_1 \\ \end{array}$$

$$\begin{array}{c|cccc} \delta_2 & a & b \\ \hline q_1 & q_1 & q_2 \\ q_2 & q_3 & q_4 \\ q_3 & q_2 & q_1 \\ q_4 & q_3 & q_4 \\ \end{array}$$

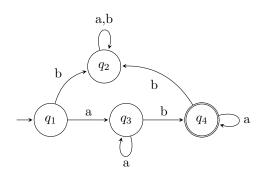
Exercise 1.3 $u q_1 d q_2$ $u d q_3 d$ $q_4 d q_3 d$ $q_5 d$

Exercise 1.4

c.



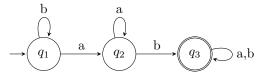
e.



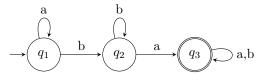
Exercise 1.5

 $\mathbf{c}.$

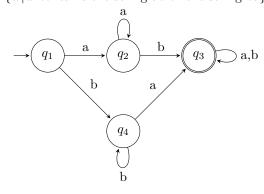
 $\{w|w \text{ contains the string ab}\}$



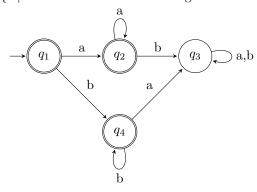
 $\{w|w \text{ contains the string ba}\}$



 $\{w|w \text{ contains the string ab or the string ba}\}$

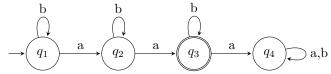


 $\{w|w \text{ does not contain the string ab nor the string ba}\}$

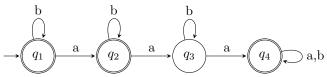


 \mathbf{g}

 $\{w|w \text{ contains exactly two a's}\}$

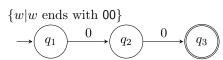


 $\{w|w \text{ doesn't contains exactly two a's}\}$



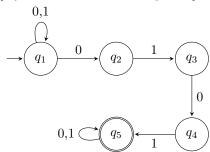
Exercise 1.7

a.

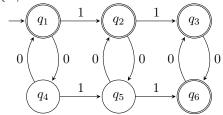


b

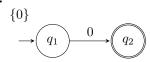
 $\{w|w \text{ contains the substring 0101}\}$



c. $\{w|w \text{ contains an even number of 0's or exactly two 1's}\}$



d.



ç.

