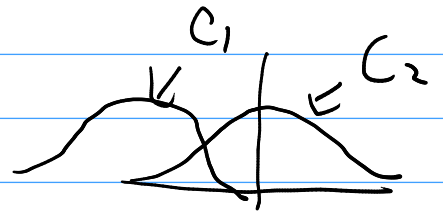


$$f(x|\mu, \sigma^2) = \frac{1}{\sqrt{2\pi}\sigma} \exp \left\{ -\frac{(x-\mu)^2}{2\sigma^2} \right\}$$

MLE



170 780

C_1 0.9 0.01 0.009

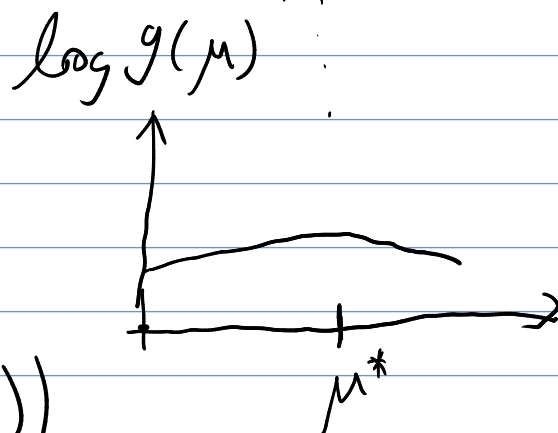
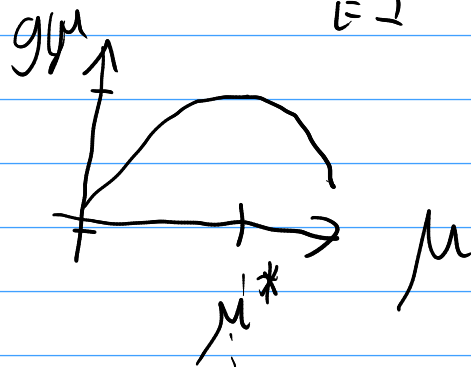
C_2 0.6 0.3 0.18 ✓

$x_1, x_2, x_3, \dots, x_n$

$P(x_1), P(x_2), \dots, P(x_n)$

$$P(x_1)P(x_2) \dots P(x_n) = \prod_{i=1}^N P(x_i)$$

$$g(\mu) = \prod_{i=1}^N P(x_i)$$



$$\begin{aligned} \log \left(\prod P(x_i) \right) \\ = \sum \log P(x_i) \end{aligned}$$

$$\log(ab) = \log a + \log b$$

$$f(x|\mu, \sigma^2) = \frac{1}{\sqrt{2\pi}\sigma} \exp \left\{ -\frac{(x-\mu)^2}{2\sigma^2} \right\}$$

$$x_1, x_2, x_3, \dots, x_N$$

$$g = \prod_{\sigma^{-N}} f(x_i|\mu, \sigma) = \left(\frac{1}{\sqrt{2\pi}} \right)^N \left(\frac{1}{\sigma} \right)^N \prod \exp \left\{ \frac{-(x_i-\mu)^2}{2\sigma^2} \right\}$$

$$\log(g) = \log \left(\frac{1}{\sqrt{2\pi}} \right)^N - N \log \sigma + \sum \log \left[\exp \left\{ \frac{-(x_i-\mu)^2}{2\sigma^2} \right\} \right]$$

$$l(\mu, \sigma) = \log \left(\frac{1}{\sqrt{2\pi}} \right)^N - N \log \sigma + \sum_{i=1}^N \left\{ \frac{-(x_i-\mu)^2}{2\sigma^2} \right\}$$

$\log e^a = a$

$$\frac{\partial l}{\partial \mu} = 0, \quad \frac{\partial l}{\partial \sigma} = 0$$

$$\frac{\partial l}{\partial \mu} = 0 + 0 + \sum \frac{\partial}{\partial \mu} \left[\frac{-(x_i-\mu)^2}{2\sigma^2} \right]$$

$$= \sum \frac{-(x_i-\mu)^2}{2\sigma^2} (-1) = 0$$

$$\frac{2(-1)(-1)}{2\sigma^2} \sum (x_i - \mu) = 0$$

$$\sum (x_i - \mu) = 0$$

$$\sum x_i - \sum_{i=1}^N \mu = 0$$

$$\sum x_i - N\mu = 0 \Rightarrow \mu = \frac{\sum x_i}{N} = \bar{x}$$

$$\sigma^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$$

$$x_1, x_2, x_3, \dots, x_n$$

$$P(x_1), P(x_2), \dots, P(x_n)$$

$$\prod P(x_i)$$

$$-\log \prod P(x_i) = l(w)$$

