

Solution for Exercize 4

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Abstract

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1 Question 1

1.1 a)

Mean μ of givin points

$$x : \frac{1+2+4+5}{4} = \frac{12}{4} = 3$$

$$y : \frac{-1+1+-1+1}{4} = \frac{0}{4} = 0$$

$$\mu = \begin{pmatrix} 3 \\ 0 \end{pmatrix}$$

1.2 b)

The Covariancematrix C has the following form:

$$C = \begin{pmatrix} \text{covariance}(x, x) & \text{covariance}(x, y) \\ \text{covariance}(y, x) & \text{covariance}(y, y) \end{pmatrix} = \begin{pmatrix} \text{variance}(x) & \text{covariance}(x, y) \\ \text{covariance}(y, x) & \text{variance}(y) \end{pmatrix}$$

$$\text{covariance}(x, y) = \text{covariance}(y, x) = \frac{\sum_{i=0}^n (x_i - \bar{x}) * (y_i - \bar{y})}{n - 1}$$

$$\begin{aligned} \text{covariance}(x, y) &= \frac{(1 - 3) * (-1 - 0) + (2 - 3) * (1 - 0) + (4 - 3) * (-1 - 0) + (5 - 3) * (1 - 0)}{4 - 1} \\ &= \frac{2}{3} \end{aligned}$$

$$\text{variance}(x) = \frac{\sum_{i=0}^n (x_i - \bar{x})^2}{n - 1}$$

$$\text{variance}(x) = \frac{(1 - 3)^2 + (2 - 3)^2 + (4 - 3)^2 + (5 - 3)^2}{4 - 1} = \frac{4 + 1 + 1 + 4}{3} = \frac{10}{3}$$

$$\text{variance}(y) = \frac{(-1 - 0)^2 + (1 - 0)^2 + (-1 - 0)^2 + (1 - 0)^2}{4 - 1} = \frac{1 + 1 + 1 + 1}{3} = \frac{4}{3}$$

$$C = \begin{pmatrix} \frac{10}{3} & \frac{2}{3} \\ \frac{2}{3} & \frac{4}{3} \end{pmatrix}$$

2 Previous work

3 Results

In this section we describe the results.

4 Conclusions

We worked hard, and achieved very little.