HW2 on Normal Forms (Due on Mar. 9)

1. Give the simplest DNF and CNF of the following statements:

1)
$$((P \rightarrow Q) \leftrightarrow (\neg Q \rightarrow \neg P)) \land R$$

2)
$$P \lor (\neg P \lor (Q \land \neg Q))$$

3)
$$(P \land (Q \land S)) \lor (\neg P \land (Q \land S))$$

2. Give the full DNF of the following statements:

$$1) (\neg P \vee \neg Q) \to (P \leftrightarrow \neg Q)$$

$$2) (\neg R \land (Q \rightarrow P)) \rightarrow (P \rightarrow (Q \lor R))$$

3)
$$(P \rightarrow (Q \land R)) \land (\neg P \rightarrow (\neg Q \land \neg R))$$

3. Give the prenex normal forms of the following statements:

1)
$$(\forall x)(P(x) \rightarrow (\exists y)Q(x,y))$$

2)
$$(\forall x)(\forall y)(((\exists z)P(x,y,z) \land (\exists u)Q(x,u)) \rightarrow (\exists v)Q(y,v))$$

4. Give the prenex DNF and CNF of the following statements:

1)
$$((\exists x)P(x) \lor (\exists x)Q(x)) \rightarrow (\exists x)(P(x) \lor Q(x))$$

2)
$$(\forall x)(P(x) \rightarrow Q(x,y)) \rightarrow$$

$$((\exists y)(P(y) \land (\exists z)Q(y,z)))$$