

Summary of symmetry calculations

October 26, 2021

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Chapter 1

DBH_model

Run 11_43PM_26_October-2021

Degree in tangential ansätze: 1.
The system of ODEs is given by:

$$\begin{aligned}\frac{dw_1}{dt} &= -w_1w_2 - w_1w_3 + w_2w_3, \\ \frac{dw_2}{dt} &= -w_1w_2 + w_1w_3 - w_2w_3, \\ \frac{dw_3}{dt} &= w_1w_2 - w_1w_3 - w_2w_3.\end{aligned}$$

The calculated generators are:

$$X_1 = (-1 + t) \partial t + (w_1) \partial w_1 + (w_2) \partial w_2 + (w_3) \partial w_3,$$

$$X_2 = (1) \partial t,$$

$$\begin{aligned}X_3 &= (t + 2) \partial t + (1 - 2tw_1) \partial w_1 + (1 - 2tw_2) \partial w_2 \\ &\quad + (1 - 2tw_3) \partial w_3\end{aligned}$$

The execution time of the script was:

0 hours 0 minutes 25 seconds.

Run 11_44PM_26_October-2021

Degree in tangential ansätze: 1.
The system of ODEs is given by:

$$\begin{aligned}\frac{dw_1}{dt} &= -w_1w_2 - w_1w_3 + w_2w_3, \\ \frac{dw_2}{dt} &= -w_1w_2 + w_1w_3 - w_2w_3, \\ \frac{dw_3}{dt} &= w_1w_2 - w_1w_3 - w_2w_3.\end{aligned}$$

The calculated generators are:

$$X_1 = (1) \partial t,$$

$$X_2 = (-1 + t) \partial t + (w_1) \partial w_1 + (w_2) \partial w_2 + (w_3) \partial w_3,$$

$$\begin{aligned}X_3 &= (t + 2) \partial t + (1 - 2tw_1) \partial w_1 + (1 - 2tw_2) \partial w_2 \\ &\quad + (1 - 2tw_3) \partial w_3\end{aligned}$$

The execution time of the script was:

0 hours 0 minutes 25 seconds.

Run 11_44PM_26_October-2021

Degree in tangential ansätze: 1.

The system of ODEs is given by:

$$\begin{aligned}\frac{dw_1}{dt} &= -w_1w_2 - w_1w_3 + w_2w_3, \\ \frac{dw_2}{dt} &= -w_1w_2 + w_1w_3 - w_2w_3, \\ \frac{dw_3}{dt} &= w_1w_2 - w_1w_3 - w_2w_3.\end{aligned}$$

The calculated generators are:

$$\begin{aligned}X_1 &= (t + 2) \partial t + (1 - 2tw_1) \partial w_1 + (1 - 2tw_2) \partial w_2 \\ &\quad + (1 - 2tw_3) \partial w_3\end{aligned}$$

$$X_2 = (-1 + t) \partial t + (w_1) \partial w_1 + (w_2) \partial w_2 + (w_3) \partial w_3,$$

$$X_3 = (1) \partial t.$$

The execution time of the script was:

0 hours 0 minutes 25 seconds.

Run 11_45PM_26_October-2021

Degree in tangential ansätze: 1.

The system of ODEs is given by:

$$\begin{aligned}\frac{dw_1}{dt} &= -w_1w_2 - w_1w_3 + w_2w_3, \\ \frac{dw_2}{dt} &= -w_1w_2 + w_1w_3 - w_2w_3, \\ \frac{dw_3}{dt} &= w_1w_2 - w_1w_3 - w_2w_3.\end{aligned}$$

The calculated generators are:

$$\begin{aligned}X_1 &= (t+2) \partial t + (1-2tw_1) \partial w_1 + (1-2tw_2) \partial w_2 \\ &\quad + (1-2tw_3) \partial w_3\end{aligned}$$

$$X_2 = (-1+t) \partial t + (w_1) \partial w_1 + (w_2) \partial w_2 + (w_3) \partial w_3,$$

$$X_3 = (1) \partial t.$$

The execution time of the script was:

0 hours 0 minutes 25 seconds.

Run 11_48PM_26_October-2021

Degree in tangential ansätze: 2.

The system of ODEs is given by:

$$\begin{aligned}\frac{dw_1}{dt} &= -w_1w_2 - w_1w_3 + w_2w_3, \\ \frac{dw_2}{dt} &= -w_1w_2 + w_1w_3 - w_2w_3, \\ \frac{dw_3}{dt} &= w_1w_2 - w_1w_3 - w_2w_3.\end{aligned}$$

The calculated generators are:

$$X_1 = (-1+t) \partial t + (w_1) \partial w_1 + (w_2) \partial w_2 + (w_3) \partial w_3,$$

$$X_2 = (1) \partial t,$$

$$X_3 = (-1) \partial t,$$

$$X_4 = (t+2) \partial t + (1-2tw_1) \partial w_1 + (1-2tw_2) \partial w_2 \\ + (1-2tw_3) \partial w_3$$

$$X_5 = (t) \partial t + (w_2 w_3 f_1(t) - w_1 w_2 f_1(t) - w_1 w_3 f_1(t)) \partial w_1 + (w_1 w_3 f_1(t) - w_1 w_2 f_1(t) \\ + -w_2 w_3 f_1(t)) \partial w_2 + (w_1 w_2 f_1(t) - w_1 w_3 f_1(t) - w_2 w_3 f_1(t)) \partial w_3$$

Some of the generators might contain the following arbitrary functions:

$$f_1$$

The execution time of the script was:

0 hours 3 minutes 28 seconds.

Run 11_52PM_26_October-2021

Degree in tangential ansätze: 2.

The system of ODEs is given by:

$$\frac{dw_1}{dt} = -w_1 w_2 - w_1 w_3 + w_2 w_3, \\ \frac{dw_2}{dt} = -w_1 w_2 + w_1 w_3 - w_2 w_3, \\ \frac{dw_3}{dt} = w_1 w_2 - w_1 w_3 - w_2 w_3.$$

The calculated generators are:

$$X_1 = (-1+t) \partial t + (w_1) \partial w_1 + (w_2) \partial w_2 + (w_3) \partial w_3,$$

$$X_2 = (-1) \partial t,$$

$$X_3 = (t+2) \partial t + (1-2tw_1) \partial w_1 + (1-2tw_2) \partial w_2 \\ + (1-2tw_3) \partial w_3$$

$$X_4 = (1) \partial t,$$

$$X_5 = (t) \partial t + (w_2 w_3 f_1(t) - w_1 w_2 f_1(t) - w_1 w_3 f_1(t)) \partial w_1 + (w_1 w_3 f_1(t) - w_1 w_2 f_1(t) \\ + -w_2 w_3 f_1(t)) \partial w_2 + (w_1 w_2 f_1(t) - w_1 w_3 f_1(t) - w_2 w_3 f_1(t)) \partial w_3$$

Some of the generators might contain the following arbitrary functions:

$$f_1$$

The execution time of the script was:

0 hours 3 minutes 29 seconds.

Run 11_55PM_26_October-2021

Degree in tangential ansätze: 2.

The system of ODEs is given by:

$$\begin{aligned} \frac{dw_1}{dt} &= -w_1 w_2 - w_1 w_3 + w_2 w_3, \\ \frac{dw_2}{dt} &= -w_1 w_2 + w_1 w_3 - w_2 w_3, \\ \frac{dw_3}{dt} &= w_1 w_2 - w_1 w_3 - w_2 w_3. \end{aligned}$$

The calculated generators are:

$$X_1 = (1) \partial t,$$

$$X_2 = (t + 2) \partial t + (1 - 2t w_1) \partial w_1 + (1 - 2t w_2) \partial w_2 \\ + (1 - 2t w_3) \partial w_3$$

$$X_3 = (-1 + t) \partial t + (w_1) \partial w_1 + (w_2) \partial w_2 + (w_3) \partial w_3,$$

$$X_4 = (-1) \partial t,$$

$$X_5 = (t) \partial t + (w_2 w_3 f_1(t) - w_1 w_2 f_1(t) - w_1 w_3 f_1(t)) \partial w_1 + (w_1 w_3 f_1(t) - w_1 w_2 f_1(t) + w_2 w_3 f_1(t)) \partial w_2 + (w_1 w_2 f_1(t) - w_1 w_3 f_1(t) - w_2 w_3 f_1(t)) \partial w_3$$

Some of the generators might contain the following arbitrary functions:

$$f_1$$

The execution time of the script was:

0 hours 3 minutes 35 seconds.

Run 11_59PM_26_October-2021

Degree in tangential ansätze: 2.

The system of ODEs is given by:

$$\begin{aligned} \frac{dw_1}{dt} &= -w_1 w_2 - w_1 w_3 + w_2 w_3, \\ \frac{dw_2}{dt} &= -w_1 w_2 + w_1 w_3 - w_2 w_3, \\ \frac{dw_3}{dt} &= w_1 w_2 - w_1 w_3 - w_2 w_3. \end{aligned}$$

The calculated generators are:

$$X_1 = (t + 2) \partial t + (1 - 2t w_1) \partial w_1 + (1 - 2t w_2) \partial w_2 + (1 - 2t w_3) \partial w_3$$

$$X_2 = (-1 + t) \partial t + (w_1) \partial w_1 + (w_2) \partial w_2 + (w_3) \partial w_3,$$

$$X_3 = (1) \partial t,$$

$$X_4 = (-1) \partial t,$$

$$X_5 = (t) \partial t + (w_2 w_3 f_1(t) - w_1 w_2 f_1(t) - w_1 w_3 f_1(t)) \partial w_1 + (w_1 w_3 f_1(t) - w_1 w_2 f_1(t) + w_2 w_3 f_1(t)) \partial w_2 + (w_1 w_2 f_1(t) - w_1 w_3 f_1(t) - w_2 w_3 f_1(t)) \partial w_3$$

Some of the generators might contain the following arbitrary functions:

$$f_1$$

The execution time of the script was:

0 hours 3 minutes 33 seconds.

Chapter 2

hydons_model

Run 11_29PM_26_October-2021

Degree in tangential ansätze: 1.
The system of ODEs is given by:

$$\begin{aligned}\frac{dy_1}{dt} &= \frac{ty_1 + y_2^2}{-t^2 + y_1y_2}, \\ \frac{dy_2}{dt} &= \frac{ty_2 + y_1^2}{-t^2 + y_1y_2}.\end{aligned}$$

The calculated generators are:

$$X_1 = (t) \partial t + (y_1) \partial y_1 + (y_2) \partial y_2.$$

The execution time of the script was:

0 hours 0 minutes 5 seconds.

Run 11_29PM_26_October-2021

Degree in tangential ansätze: 1.
The system of ODEs is given by:

$$\begin{aligned}\frac{dy_1}{dt} &= \frac{ty_1 + y_2^2}{-t^2 + y_1y_2}, \\ \frac{dy_2}{dt} &= \frac{ty_2 + y_1^2}{-t^2 + y_1y_2}.\end{aligned}$$

The calculated generators are:

$$X_1 = (t) \partial t + (y_1) \partial y_1 + (y_2) \partial y_2.$$

The execution time of the script was:

0 hours 0 minutes 5 seconds.

Run 11_29PM_26_October-2021

Degree in tangential ansätze: 1.

The system of ODEs is given by:

$$\begin{aligned}\frac{dy_1}{dt} &= \frac{ty_1 + y_2^2}{-t^2 + y_1y_2}, \\ \frac{dy_2}{dt} &= \frac{ty_2 + y_1^2}{-t^2 + y_1y_2}.\end{aligned}$$

The calculated generators are:

$$X_1 = (t) \partial t + (y_1) \partial y_1 + (y_2) \partial y_2.$$

The execution time of the script was:

0 hours 0 minutes 5 seconds.

Run 11_30PM_26_October-2021

Degree in tangential ansätze: 1.

The system of ODEs is given by:

$$\begin{aligned}\frac{dy_1}{dt} &= \frac{ty_1 + y_2^2}{-t^2 + y_1y_2}, \\ \frac{dy_2}{dt} &= \frac{ty_2 + y_1^2}{-t^2 + y_1y_2}.\end{aligned}$$

The calculated generators are:

$$X_1 = (t) \partial t + (y_1) \partial y_1 + (y_2) \partial y_2.$$

The execution time of the script was:

0 hours 0 minutes 5 seconds.

Run 11_30PM_26_October-2021

Degree in tangential ansätze: 2.

The system of ODEs is given by:

$$\begin{aligned}\frac{dy_1}{dt} &= \frac{ty_1 + y_2^2}{-t^2 + y_1y_2}, \\ \frac{dy_2}{dt} &= \frac{ty_2 + y_1^2}{-t^2 + y_1y_2}.\end{aligned}$$

The calculated generators are:

$$X_1 = (t) \partial t + (y_1) \partial y_1 + (y_2) \partial y_2,$$

$$X_2 = (-t^2 f_1(t) + y_1 y_2 f_1(t)) \partial t + (y_2^2 f_1(t) + t y_1 f_1(t)) \partial y_1 + (y_1^2 f_1(t) + t y_2 f_1(t)) \partial y_2$$

Some of the generators might contain the following arbitrary functions:

$$f_1$$

The execution time of the script was:

0 hours 0 minutes 23 seconds.

Run 11_30PM_26_October-2021

Degree in tangential ansätze: 2.

The system of ODEs is given by:

$$\begin{aligned} \frac{dy_1}{dt} &= \frac{t y_1 + y_2^2}{-t^2 + y_1 y_2}, \\ \frac{dy_2}{dt} &= \frac{t y_2 + y_1^2}{-t^2 + y_1 y_2}. \end{aligned}$$

The calculated generators are:

$$X_1 = (t) \partial t + (y_1) \partial y_1 + (y_2) \partial y_2,$$

$$X_2 = (-t^2 f_1(t) + y_1 y_2 f_1(t)) \partial t + (y_2^2 f_1(t) + t y_1 f_1(t)) \partial y_1 + (y_1^2 f_1(t) + t y_2 f_1(t)) \partial y_2$$

Some of the generators might contain the following arbitrary functions:

$$f_1$$

The execution time of the script was:

0 hours 0 minutes 24 seconds.

Run 11_31PM_26_October-2021

Degree in tangential ansätze: 2.

The system of ODEs is given by:

$$\begin{aligned}\frac{dy_1}{dt} &= \frac{ty_1 + y_2^2}{-t^2 + y_1y_2}, \\ \frac{dy_2}{dt} &= \frac{ty_2 + y_1^2}{-t^2 + y_1y_2}.\end{aligned}$$

The calculated generators are:

$$X_1 = (t) \partial t + (y_1) \partial y_1 + (y_2) \partial y_2,$$

$$X_2 = (-t^2 f_1(t) + y_1 y_2 f_1(t)) \partial t + (y_2^2 f_1(t) + t y_1 f_1(t)) \partial y_1 + (y_1^2 f_1(t) + t y_2 f_1(t)) \partial y_2$$

Some of the generators might contain the following arbitrary functions:

$$f_1$$

The execution time of the script was:

0 hours 0 minutes 23 seconds.

Chapter 3

linear_model

Run 11_31PM_26_October-2021

Degree in tangential ansätze: 1.
The system of ODEs is given by:

$$\begin{aligned}\frac{du}{dt} &= u + v, \\ \frac{dv}{dt} &= u + v.\end{aligned}$$

The calculated generators are:

$$\begin{aligned}X_1 &= \left(\frac{u}{2} - \frac{v}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t \\ X_2 &= \left(\frac{v}{2} - \frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t \\ X_3 &= \left(-\frac{e^{2t}}{4} + \frac{e^{-2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} - \frac{ve^{2t}}{2} \right) \partial u \\ &\quad + \left(\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v \\ X_4 &= \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v \\ X_5 &= (1) \partial t,\end{aligned}$$

$$\begin{aligned}X_6 &= \left(-\frac{1}{2} - \frac{e^{-2t}}{4} - \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right. \\ &\quad \left. + -\frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v\end{aligned}$$

$$X_7 = \left(-\frac{1}{2} + \frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} + \frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_8 = \left(-\frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ve^{2t}}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right) \partial u + \left(\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_9 = \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_{10} = (t) \partial t + (u f_1(t) + v f_1(t)) \partial u + (u f_1(t) + v f_1(t)) \partial v$$

Some of the generators might contain the following arbitrary functions:

$$f_1$$

The execution time of the script was:

0 hours 0 minutes 12 seconds.

Run 11_32PM_26_October-2021

Degree in tangential ansätze: 1.

The system of ODEs is given by:

$$\begin{aligned} \frac{du}{dt} &= u + v, \\ \frac{dv}{dt} &= u + v. \end{aligned}$$

The calculated generators are:

$$X_1 = \left(-\frac{1}{2} + \frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} + \frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_2 = \left(-\frac{e^{2t}}{4} + \frac{e^{-2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} - \frac{ve^{2t}}{2} \right) \partial u + \left(\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v$$

$$X_3 = \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_4 = \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_5 = (1) \partial t,$$

$$X_6 = \left(\frac{v}{2} - \frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$X_7 = \left(\frac{u}{2} - \frac{v}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$X_8 = \left(-\frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ve^{2t}}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right) \partial u \\ + \left(\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_9 = \left(-\frac{1}{2} - \frac{e^{-2t}}{4} - \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right. \\ \left. + -\frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v$$

$$X_{10} = (t) \partial t + (u f_1(t) + v f_1(t)) \partial u + (u f_1(t) + v f_1(t)) \partial v$$

Some of the generators might contain the following arbitrary functions:

$$f_1$$

The execution time of the script was:

0 hours 0 minutes 12 seconds.

Run 11_32PM_26_October-2021

Degree in tangential ansätze: 1.

The system of ODEs is given by:

$$\frac{du}{dt} = u + v, \\ \frac{dv}{dt} = u + v.$$

The calculated generators are:

$$X_1 = \left(-\frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ve^{2t}}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right) \partial u \\ + \left(\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_2 = \left(-\frac{e^{2t}}{4} + \frac{e^{-2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} - \frac{ve^{2t}}{2} \right) \partial u \\ + \left(\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v$$

$$X_3 = \left(-\frac{1}{2} - \frac{e^{-2t}}{4} - \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right. \\ \left. + -\frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v$$

$$X_4 = \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_5 = (1) \partial t,$$

$$X_6 = \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_7 = \left(\frac{u}{2} - \frac{v}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$X_8 = \left(-\frac{1}{2} + \frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right. \\ \left. + \frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_9 = \left(\frac{v}{2} - \frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$X_{10} = (t) \partial t + (u f_1(t) + v f_1(t)) \partial u + (u f_1(t) + v f_1(t)) \partial v$$

Some of the generators might contain the following arbitrary functions:

$$f_1$$

The execution time of the script was:

0 hours 0 minutes 11 seconds.

Run 11_32PM_26_October-2021

Degree in tangential ansätze: 1.

The system of ODEs is given by:

$$\begin{aligned}\frac{du}{dt} &= u + v, \\ \frac{dv}{dt} &= u + v.\end{aligned}$$

The calculated generators are:

$$\begin{aligned}X_1 &= \left(-\frac{1}{2} - \frac{e^{-2t}}{4} - \frac{e^{2t}}{4}\right) \partial t + \left(-\frac{u}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right. \\ &\quad \left. + -\frac{ve^{2t}}{2}\right) \partial u + \left(-\frac{v}{2} - \frac{ve^{2t}}{2}\right) \partial v\end{aligned}$$

$$\begin{aligned}X_2 &= \left(-\frac{1}{2} + \frac{e^{-2t}}{4} + \frac{e^{2t}}{4}\right) \partial t + \left(-\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right. \\ &\quad \left. + \frac{ve^{2t}}{2}\right) \partial u + \left(-\frac{v}{2} + \frac{ve^{2t}}{2}\right) \partial v\end{aligned}$$

$$X_3 = \left(-\frac{1}{2} + \frac{e^{2t}}{2}\right) \partial u + \left(\frac{1}{2} + \frac{e^{2t}}{2}\right) \partial v$$

$$X_4 = \left(\frac{u}{2} - \frac{v}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2}\right) \partial t$$

$$X_5 = (1) \partial t,$$

$$X_6 = \left(\frac{1}{2} + \frac{e^{2t}}{2}\right) \partial u + \left(-\frac{1}{2} + \frac{e^{2t}}{2}\right) \partial v$$

$$X_7 = \left(\frac{v}{2} - \frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2}\right) \partial t$$

$$\begin{aligned}X_8 &= \left(-\frac{e^{2t}}{4} + \frac{e^{-2t}}{4}\right) \partial t + \left(\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} - \frac{ve^{2t}}{2}\right) \partial u \\ &\quad + \left(\frac{v}{2} - \frac{ve^{2t}}{2}\right) \partial v\end{aligned}$$

$$\begin{aligned}X_9 &= \left(-\frac{e^{-2t}}{4} + \frac{e^{2t}}{4}\right) \partial t + \left(\frac{u}{2} + \frac{ve^{2t}}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2}\right) \partial u \\ &\quad + \left(\frac{v}{2} + \frac{ve^{2t}}{2}\right) \partial v\end{aligned}$$

$$X_{10} = (t) \partial t + (u f_1(t) + v f_1(t)) \partial u + (u f_1(t) + v f_1(t)) \partial v$$

Some of the generators might contain the following arbitrary functions:

$$f_1$$

The execution time of the script was:

0 hours 0 minutes 13 seconds.

Run 11_35PM_26_October-2021

Degree in tangential ansätze: 2.

The system of ODEs is given by:

$$\begin{aligned} \frac{du}{dt} &= u + v, \\ \frac{dv}{dt} &= u + v. \end{aligned}$$

The calculated generators are:

$$\begin{aligned} X_1 = & \left(-\frac{e^{2t}}{4} + \frac{e^{-2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} - \frac{ve^{2t}}{2} \right) \partial u \\ & + \left(\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v \end{aligned}$$

$$X_2 = \left(\frac{v}{2} - \frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$X_3 = \left(-\frac{u^2}{4} - \frac{v^2}{4} + \frac{uv}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t$$

$$\begin{aligned} X_4 = & \left(-\frac{u}{8} - \frac{v}{8} - \frac{3ve^{-2t}}{8} - \frac{ue^{2t}}{8} + \frac{ue^{-4t}}{8} + \frac{ue^{-2t}}{8} \right. \\ & \left. + \frac{ve^{-4t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} + \frac{u^2e^{-2t}}{2} + \frac{v^2e^{2t}}{2} \right. \\ & \left. + \frac{uv}{2} - \frac{v^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} \right. \\ & \left. + \frac{v^2e^{2t}}{2} \right) \partial v \end{aligned}$$

$$\begin{aligned}
X_5 = & \left(-\frac{3v}{8} + \frac{u}{8} - \frac{3ve^{2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{-2t}}{8} - \frac{ve^{-4t}}{8} \right. \\
& \left. + \frac{ve^{-2t}}{8} + \frac{ue^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} - \frac{uv}{2} - \frac{v^2e^{2t}}{2} \right. \\
& \left. + \frac{u^2e^{-4t}}{4} - \frac{v^2e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} - \frac{v^2e^{2t}}{2} \right) \partial v
\end{aligned}$$

$$\begin{aligned}
X_6 = & \left(\frac{u^2}{4} + \frac{v^2}{4} + \frac{u^2e^{-2t}}{2} - \frac{uv}{2} - \frac{v^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} \right. \\
& \left. + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t
\end{aligned}$$

$$\begin{aligned}
X_7 = & \left(-\frac{3u}{8} + \frac{5v}{8} - \frac{3ue^{-2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{2t}}{8} - \frac{ve^{-4t}}{8} \right. \\
& \left. + \frac{ve^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} + \frac{v^2e^{-2t}}{2} \right. \\
& \left. + \frac{v^2e^{2t}}{2} - \frac{u^2e^{-2t}}{2} - \frac{u^2e^{-4t}}{4} - \frac{v^2e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} \right. \\
& \left. + \frac{v^2e^{2t}}{2} \right) \partial v
\end{aligned}$$

$$X_8 = \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$\begin{aligned}
X_9 = & \left(-\frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ve^{2t}}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right) \partial u \\
& + \left(\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v
\end{aligned}$$

$$X_{10} = (1) \partial t,$$

$$X_{11} = \left(\frac{u}{2} - \frac{v}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$\begin{aligned}
X_{12} = & \left(-\frac{5v}{8} + \frac{3u}{8} - \frac{3ue^{-2t}}{8} - \frac{ue^{2t}}{8} + \frac{ue^{-4t}}{8} + \frac{ve^{-4t}}{8} \right. \\
& \left. + \frac{ve^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} + \frac{v^2e^{-2t}}{2} + \frac{v^2e^{2t}}{2} \right. \\
& \left. + \frac{uv}{2} - \frac{u^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} \right. \\
& \left. + \frac{v^2e^{2t}}{2} \right) \partial v
\end{aligned}$$

$$X_{13} = \left(-\frac{u}{8} + \frac{3v}{8} - \frac{3ve^{2t}}{8} - \frac{ue^{-2t}}{8} - \frac{ve^{-2t}}{8} + \frac{ue^{-4t}}{8} + \frac{ue^{2t}}{8} + \frac{ve^{-4t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} - \frac{v^2e^{2t}}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} - \frac{v^2e^{2t}}{2} \right) \partial v$$

$$X_{14} = \left(\frac{u^2}{4} + \frac{v^2}{4} + \frac{v^2e^{-2t}}{2} - \frac{uv}{2} - \frac{u^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t$$

$$X_{15} = \left(-\frac{1}{2} - \frac{e^{-2t}}{4} - \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} + \frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v$$

$$X_{16} = \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_{17} = \left(\frac{u}{8} + \frac{v}{8} - \frac{3ve^{-2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{2t}}{8} - \frac{ve^{-4t}}{8} + \frac{ue^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} + \frac{u^2e^{-2t}}{2} + \frac{v^2e^{2t}}{2} - \frac{v^2e^{-2t}}{2} - \frac{u^2e^{-4t}}{4} - \frac{v^2e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} + \frac{v^2e^{2t}}{2} \right) \partial v$$

$$X_{18} = \left(-\frac{1}{2} + \frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} + \frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_{19} = (u f_2(t) + v f_1(t) - v f_2(t) + f_3(t)) \partial t + (u f_3(t) + v f_3(t) + u^2 f_2(t) + v^2 f_1(t) - v^2 f_2(t) + uv f_1(t)) \partial u + (u f_3(t) + v f_3(t) + u^2 f_2(t) + v^2 f_1(t) - v^2 f_2(t) + uv f_1(t)) \partial v$$

Some of the generators might contain the following arbitrary functions:

f_1
 f_2
 f_3

The execution time of the script was:

0 hours 3 minutes 19 seconds.

Run 11_37PM_26_October-2021

Degree in tangential ansätze: 2.

The system of ODEs is given by:

$$\begin{aligned}\frac{du}{dt} &= u + v, \\ \frac{dv}{dt} &= u + v.\end{aligned}$$

The calculated generators are:

$$\begin{aligned}X_1 = & \left(-\frac{3v}{8} + \frac{u}{8} - \frac{3ve^{2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{-2t}}{8} - \frac{ve^{-4t}}{8} \right. \\ & \left. + \frac{ve^{-2t}}{8} + \frac{ue^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} - \frac{uv}{2} - \frac{v^2e^{2t}}{2} \right. \\ & \left. + \frac{u^2e^{-4t}}{4} - \frac{v^2e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} - \frac{v^2e^{2t}}{2} \right) \partial v\end{aligned}$$

$$\begin{aligned}X_2 = & \left(-\frac{u}{8} + \frac{3v}{8} - \frac{3ve^{2t}}{8} - \frac{ue^{-2t}}{8} - \frac{ve^{-2t}}{8} + \frac{ue^{-4t}}{8} \right. \\ & \left. + \frac{ue^{2t}}{8} + \frac{ve^{-4t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} - \frac{v^2e^{2t}}{2} \right. \\ & \left. + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} - \frac{v^2e^{2t}}{2} \right) \partial v\end{aligned}$$

$$\begin{aligned}X_3 = & \left(\frac{u}{8} + \frac{v}{8} - \frac{3ve^{-2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{2t}}{8} - \frac{ve^{-4t}}{8} \right. \\ & \left. + \frac{ue^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} + \frac{u^2e^{-2t}}{2} \right. \\ & \left. + \frac{v^2e^{2t}}{2} - \frac{v^2e^{-2t}}{2} - \frac{u^2e^{-4t}}{4} - \frac{v^2e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} \right. \\ & \left. + \frac{v^2e^{2t}}{2} \right) \partial v\end{aligned}$$

$$\begin{aligned}X_4 = & \left(-\frac{1}{2} - \frac{e^{-2t}}{4} - \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right. \\ & \left. + \frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v\end{aligned}$$

$$\begin{aligned}X_5 = & \left(-\frac{e^{2t}}{4} + \frac{e^{-2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} - \frac{ve^{2t}}{2} \right) \partial u \\ & + \left(\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v\end{aligned}$$

$$X_6 = \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_7 = \left(\frac{v}{2} - \frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$X_8 = (1) \partial t,$$

$$X_9 = \left(-\frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ve^{2t}}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right) \partial u \\ + \left(\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_{10} = \left(\frac{u^2}{4} + \frac{v^2}{4} + \frac{u^2e^{-2t}}{2} - \frac{uv}{2} - \frac{v^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} \right. \\ \left. + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t$$

$$X_{11} = \left(-\frac{5v}{8} + \frac{3u}{8} - \frac{3ue^{-2t}}{8} - \frac{ue^{2t}}{8} + \frac{ue^{-4t}}{8} + \frac{ve^{-4t}}{8} \right. \\ \left. + \frac{ve^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} + \frac{v^2e^{-2t}}{2} + \frac{v^2e^{2t}}{2} \right. \\ \left. + \frac{uv}{2} - \frac{u^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} \right. \\ \left. + \frac{v^2e^{2t}}{2} \right) \partial v$$

$$X_{12} = \left(-\frac{u}{8} - \frac{v}{8} - \frac{3ve^{-2t}}{8} - \frac{ue^{2t}}{8} + \frac{ue^{-4t}}{8} + \frac{ue^{-2t}}{8} \right. \\ \left. + \frac{ve^{-4t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} + \frac{u^2e^{-2t}}{2} + \frac{v^2e^{2t}}{2} \right. \\ \left. + \frac{uv}{2} - \frac{v^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} \right. \\ \left. + \frac{v^2e^{2t}}{2} \right) \partial v$$

$$X_{13} = \left(-\frac{3u}{8} + \frac{5v}{8} - \frac{3ue^{-2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{2t}}{8} - \frac{ve^{-4t}}{8} \right. \\ \left. + \frac{ve^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} + \frac{v^2e^{-2t}}{2} \right. \\ \left. + \frac{v^2e^{2t}}{2} - \frac{u^2e^{-2t}}{2} - \frac{u^2e^{-4t}}{4} - \frac{v^2e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} \right. \\ \left. + \frac{v^2e^{2t}}{2} \right) \partial v$$

$$X_{14} = \left(\frac{u}{2} - \frac{v}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$X_{15} = \left(\frac{u^2}{4} + \frac{v^2}{4} + \frac{v^2 e^{-2t}}{2} - \frac{uv}{2} - \frac{u^2 e^{-2t}}{2} + \frac{u^2 e^{-4t}}{4} + \frac{v^2 e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t$$

$$X_{16} = \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_{17} = \left(-\frac{1}{2} + \frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} + \frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_{18} = \left(-\frac{u^2}{4} - \frac{v^2}{4} + \frac{uv}{2} + \frac{u^2 e^{-4t}}{4} + \frac{v^2 e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t$$

$$\begin{aligned} X_{19} = & (u f_2(t) + v f_1(t) - v f_2(t) + f_3(t)) \partial t + (u f_3(t) + v f_3(t) \\ & + u^2 f_2(t) + v^2 f_1(t) - v^2 f_2(t) + uv f_1(t)) \partial u + (u f_3(t) + v f_3(t) \\ & + u^2 f_2(t) + v^2 f_1(t) - v^2 f_2(t) + uv f_1(t)) \partial v \end{aligned}$$

Some of the generators might contain the following arbitrary functions:

$$\begin{aligned} & f_1 \\ & f_2 \\ & f_3 \end{aligned}$$

The execution time of the script was:

0 hours 2 minutes 6 seconds.

Run 11_40PM_26_October-2021

Degree in tangential ansätze: 2.

The system of ODEs is given by:

$$\begin{aligned} \frac{du}{dt} &= u + v, \\ \frac{dv}{dt} &= u + v. \end{aligned}$$

The calculated generators are:

$$X_1 = \left(-\frac{1}{2} - \frac{e^{-2t}}{4} - \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right. \\ \left. + -\frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v$$

$$X_2 = \left(-\frac{e^{2t}}{4} + \frac{e^{-2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} - \frac{ve^{2t}}{2} \right) \partial u \\ + \left(\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v$$

$$X_3 = \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_4 = \left(-\frac{5v}{8} + \frac{3u}{8} - \frac{3ue^{-2t}}{8} - \frac{ue^{2t}}{8} + \frac{ue^{-4t}}{8} + \frac{ve^{-4t}}{8} \right. \\ \left. + \frac{ve^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} + \frac{v^2e^{-2t}}{2} + \frac{v^2e^{2t}}{2} \right. \\ \left. + -\frac{uv}{2} - \frac{u^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} \right. \\ \left. + \frac{v^2e^{2t}}{2} \right) \partial v$$

$$X_5 = \left(\frac{u}{2} - \frac{v}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$X_6 = \left(-\frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ve^{2t}}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right) \partial u \\ + \left(\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_7 = \left(-\frac{u}{8} + \frac{3v}{8} - \frac{3ve^{2t}}{8} - \frac{ue^{-2t}}{8} - \frac{ve^{-2t}}{8} + \frac{ue^{-4t}}{8} \right. \\ \left. + \frac{ue^{2t}}{8} + \frac{ve^{-4t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} - \frac{v^2e^{2t}}{2} \right. \\ \left. + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} - \frac{v^2e^{2t}}{2} \right) \partial v$$

$$X_8 = \left(-\frac{3u}{8} + \frac{5v}{8} - \frac{3ue^{-2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{2t}}{8} - \frac{ve^{-4t}}{8} \right. \\ \left. + \frac{ve^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} + \frac{v^2e^{-2t}}{2} \right. \\ \left. + \frac{v^2e^{2t}}{2} - \frac{u^2e^{-2t}}{2} - \frac{u^2e^{-4t}}{4} - \frac{v^2e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} \right. \\ \left. + \frac{v^2e^{2t}}{2} \right) \partial v$$

$$X_9 = \left(\frac{u^2}{4} + \frac{v^2}{4} + \frac{v^2 e^{-2t}}{2} - \frac{uv}{2} - \frac{u^2 e^{-2t}}{2} + \frac{u^2 e^{-4t}}{4} + \frac{v^2 e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t$$

$$X_{10} = \left(-\frac{u^2}{4} - \frac{v^2}{4} + \frac{uv}{2} + \frac{u^2 e^{-4t}}{4} + \frac{v^2 e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t$$

$$X_{11} = \left(-\frac{3v}{8} + \frac{u}{8} - \frac{3ve^{2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{-2t}}{8} - \frac{ve^{-4t}}{8} + \frac{ve^{-2t}}{8} + \frac{ue^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} - \frac{uv}{2} - \frac{v^2 e^{2t}}{2} + \frac{u^2 e^{-4t}}{4} - \frac{v^2 e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} - \frac{v^2 e^{2t}}{2} \right) \partial v$$

$$X_{12} = \left(\frac{u^2}{4} + \frac{v^2}{4} + \frac{u^2 e^{-2t}}{2} - \frac{uv}{2} - \frac{v^2 e^{-2t}}{2} + \frac{u^2 e^{-4t}}{4} + \frac{v^2 e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t$$

$$X_{13} = \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_{14} = \left(-\frac{u}{8} - \frac{v}{8} - \frac{3ve^{-2t}}{8} - \frac{ue^{2t}}{8} + \frac{ue^{-4t}}{8} + \frac{ue^{-2t}}{8} + \frac{ve^{-4t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} + \frac{u^2 e^{-2t}}{2} + \frac{v^2 e^{2t}}{2} + \frac{uv}{2} - \frac{v^2 e^{-2t}}{2} + \frac{u^2 e^{-4t}}{4} + \frac{v^2 e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} + \frac{v^2 e^{2t}}{2} \right) \partial v$$

$$X_{15} = \left(\frac{u}{8} + \frac{v}{8} - \frac{3ve^{-2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{2t}}{8} - \frac{ve^{-4t}}{8} + \frac{ue^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} + \frac{u^2 e^{-2t}}{2} + \frac{v^2 e^{2t}}{2} - \frac{v^2 e^{-2t}}{2} - \frac{u^2 e^{-4t}}{4} - \frac{v^2 e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} + \frac{v^2 e^{2t}}{2} \right) \partial v$$

$$X_{16} = (1) \partial t,$$

$$X_{17} = \left(-\frac{1}{2} + \frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} + \frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_{18} = \left(\frac{v}{2} - \frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$\begin{aligned} X_{19} = & (u f_2(t) + v f_1(t) - v f_2(t) + f_3(t)) \partial t + (u f_3(t) + v f_3(t) \\ & + u^2 f_2(t) + v^2 f_1(t) - v^2 f_2(t) + uv f_1(t)) \partial u + (u f_3(t) + v f_3(t) \\ & + u^2 f_2(t) + v^2 f_1(t) - v^2 f_2(t) + uv f_1(t)) \partial v \end{aligned}$$

Some of the generators might contain the following arbitrary functions:

$$\begin{aligned} & f_1 \\ & f_2 \\ & f_3 \end{aligned}$$

The execution time of the script was:

0 hours 2 minutes 42 seconds.

Run 11_43PM_26_October-2021

Degree in tangential ansätze: 2.

The system of ODEs is given by:

$$\begin{aligned} \frac{du}{dt} &= u + v, \\ \frac{dv}{dt} &= u + v. \end{aligned}$$

The calculated generators are:

$$X_1 = \left(\frac{v}{2} - \frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$\begin{aligned} X_2 = & \left(-\frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ve^{2t}}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} \right) \partial u \\ & + \left(\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v \end{aligned}$$

$$X_3 = (1) \partial t,$$

$$\begin{aligned} X_4 = & \left(-\frac{5v}{8} + \frac{3u}{8} - \frac{3ue^{-2t}}{8} - \frac{ue^{2t}}{8} + \frac{ue^{-4t}}{8} + \frac{ve^{-4t}}{8} \right. \\ & \left. + \frac{ve^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} + \frac{v^2e^{-2t}}{2} + \frac{v^2e^{2t}}{2} \right. \\ & \left. + \frac{uv}{2} - \frac{u^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} \right. \\ & \left. + \frac{v^2e^{2t}}{2} \right) \partial v \end{aligned}$$

$$\begin{aligned} X_5 = & \left(-\frac{u}{8} - \frac{v}{8} - \frac{3ve^{-2t}}{8} - \frac{ue^{2t}}{8} + \frac{ue^{-4t}}{8} + \frac{ue^{-2t}}{8} \right. \\ & \left. + \frac{ve^{-4t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} + \frac{u^2e^{-2t}}{2} + \frac{v^2e^{2t}}{2} \right. \\ & \left. + \frac{uv}{2} - \frac{v^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} \right. \\ & \left. + \frac{v^2e^{2t}}{2} \right) \partial v \end{aligned}$$

$$\begin{aligned} X_6 = & \left(-\frac{e^{2t}}{4} + \frac{e^{-2t}}{4} \right) \partial t + \left(\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} - \frac{ve^{2t}}{2} \right) \partial u \\ & + \left(\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v \end{aligned}$$

$$\begin{aligned} X_7 = & \left(\frac{u}{8} + \frac{v}{8} - \frac{3ve^{-2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{2t}}{8} - \frac{ve^{-4t}}{8} \right. \\ & \left. + \frac{ue^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} + \frac{u^2e^{-2t}}{2} \right. \\ & \left. + \frac{v^2e^{2t}}{2} - \frac{v^2e^{-2t}}{2} - \frac{u^2e^{-4t}}{4} - \frac{v^2e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} \right. \\ & \left. + \frac{v^2e^{2t}}{2} \right) \partial v \end{aligned}$$

$$\begin{aligned} X_8 = & \left(\frac{u^2}{4} + \frac{v^2}{4} + \frac{u^2e^{-2t}}{2} - \frac{uv}{2} - \frac{v^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} \right. \\ & \left. + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t \end{aligned}$$

$$X_9 = \left(-\frac{u^2}{4} - \frac{v^2}{4} + \frac{uv}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t$$

$$X_{10} = \left(-\frac{1}{2} - \frac{e^{-2t}}{4} - \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} - \frac{ue^{-2t}}{2} - \frac{ve^{-2t}}{2} + \frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} - \frac{ve^{2t}}{2} \right) \partial v$$

$$X_{11} = \left(\frac{u}{2} - \frac{v}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} \right) \partial t$$

$$X_{12} = \left(-\frac{3v}{8} + \frac{u}{8} - \frac{3ve^{2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{-2t}}{8} - \frac{ve^{-4t}}{8} + \frac{ve^{-2t}}{8} + \frac{ue^{2t}}{8} \right) \partial t + \left(-\frac{v^2}{4} + \frac{u^2}{4} - \frac{uv}{2} - \frac{v^2e^{2t}}{2} + \frac{u^2e^{-4t}}{4} - \frac{v^2e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(-\frac{v^2}{2} - \frac{v^2e^{2t}}{2} \right) \partial v$$

$$X_{13} = \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_{14} = \left(\frac{u^2}{4} + \frac{v^2}{4} + \frac{v^2e^{-2t}}{2} - \frac{uv}{2} - \frac{u^2e^{-2t}}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial t$$

$$X_{15} = \left(-\frac{u}{8} + \frac{3v}{8} - \frac{3ve^{2t}}{8} - \frac{ue^{-2t}}{8} - \frac{ve^{-2t}}{8} + \frac{ue^{-4t}}{8} + \frac{ue^{2t}}{8} + \frac{ve^{-4t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} - \frac{v^2e^{2t}}{2} + \frac{u^2e^{-4t}}{4} + \frac{v^2e^{-4t}}{4} + \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} - \frac{v^2e^{2t}}{2} \right) \partial v$$

$$X_{16} = \left(-\frac{3u}{8} + \frac{5v}{8} - \frac{3ue^{-2t}}{8} - \frac{ue^{-4t}}{8} - \frac{ue^{2t}}{8} - \frac{ve^{-4t}}{8} + \frac{ve^{-2t}}{8} + \frac{3ve^{2t}}{8} \right) \partial t + \left(-\frac{u^2}{4} + \frac{v^2}{4} + \frac{uv}{2} + \frac{v^2e^{-2t}}{2} + \frac{v^2e^{2t}}{2} - \frac{u^2e^{-2t}}{2} - \frac{u^2e^{-4t}}{4} - \frac{v^2e^{-4t}}{4} - \frac{uve^{-4t}}{2} \right) \partial u + \left(\frac{v^2}{2} + \frac{v^2e^{2t}}{2} \right) \partial v$$

$$X_{17} = \left(\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial u + \left(-\frac{1}{2} + \frac{e^{2t}}{2} \right) \partial v$$

$$X_{18} = \left(-\frac{1}{2} + \frac{e^{-2t}}{4} + \frac{e^{2t}}{4} \right) \partial t + \left(-\frac{u}{2} + \frac{ue^{-2t}}{2} + \frac{ve^{-2t}}{2} + \frac{ve^{2t}}{2} \right) \partial u + \left(-\frac{v}{2} + \frac{ve^{2t}}{2} \right) \partial v$$

$$X_{19} = (u f_2(t) + v f_1(t) - v f_2(t) + f_3(t)) \partial t + (u f_3(t) + v f_3(t) + u^2 f_2(t) + v^2 f_1(t) - v^2 f_2(t) + uv f_1(t)) \partial u + (u f_3(t) + v f_3(t) + u^2 f_2(t) + v^2 f_1(t) - v^2 f_2(t) + uv f_1(t)) \partial v$$

Some of the generators might contain the following arbitrary functions:

$$\begin{aligned} &f_1 \\ &f_2 \\ &f_3 \end{aligned}$$

The execution time of the script was:

0 hours 2 minutes 45 seconds.