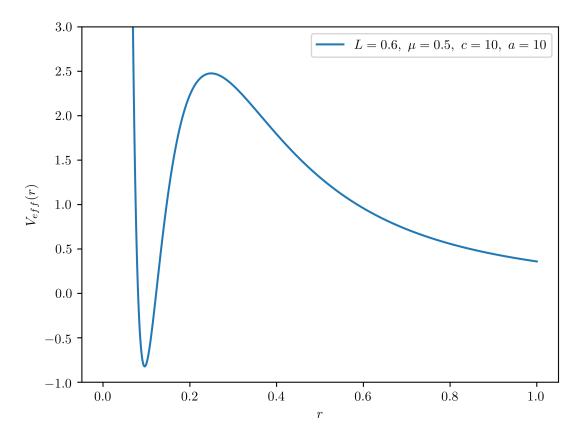
Classical Assignment #6

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October 13, 2021

1. (a) The effective potential is simply:

$$V_{\text{eff}}(r) = \frac{L^2}{2\mu r^2} - C\frac{e^{-\alpha r}}{r}$$



- (b) There are 3 distinct ranges of energies: The first range of energies are those above the "hump" where the particle will simply be scattered. Below this the particle will either, depending on the initial value of r, scatter of the hump, or "orbit" around the central force while oscillating between two different values of r. The third range is simply the bottom of the well, the lowest allowed energy, where the particle will cleanly orbit the central force.
- (a) Since the particle is scattering off of a sphere, $r_{\min} = a_0$, and since the origin is at the center of the sphere $\Psi = \arcsin\left(\frac{s}{a_0}\right)$. Using the relation $\Theta = \pi 2\Psi$ we get

 $\Theta = \pi - 2\arcsin\left(\frac{s}{a_0}\right)$. Rearranging this equation in terms of s:

$$s = \sin\left(\frac{\pi - \Theta}{2}\right) = \cos\left(\frac{\Theta}{2}\right)$$
$$\frac{ds}{d\Theta} = -\frac{1}{2}\sin\left(\frac{\Theta}{2}\right)$$