

4.)

$$E_F = \frac{1}{2} m_e V_F^2, \quad E_F = \frac{\hbar^2}{2m} \left(\frac{3\pi^2 N}{V} \right)^{2/3}$$

Once E_F is known, can calculate V_F

$$\begin{aligned} \frac{N}{V} &= \frac{0.97 \text{ g}}{1 \text{ cm}^3} \times \frac{1 \text{ mole}}{23 \text{ g}} \times \left(\frac{100 \text{ cm}}{1 \text{ m}} \right)^3 \times \frac{6.023 \times 10^{23} \text{ particles}}{1 \text{ mole}} \\ &= 2.54 \times 10^{28} \frac{\text{electrons}}{\text{m}^3} \end{aligned}$$

$$\begin{aligned} E_F &= \frac{(1.055 \times 10^{-34})^2}{2 \times 9.1 \times 10^{-31}} \left(3\pi^2 \times 2.54 \times 10^{28} \right)^{2/3} \\ &= 5.058 \times 10^{-19} \text{ J} \end{aligned}$$

$$V_F = \sqrt{2E_F/m_e} = 1.05 \times 10^6 \text{ m/s}$$

$$V_F = 1.1 \times 10^6 \text{ m/s}$$