# 03.05-Hierarchical-Indexing

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This notebook contains an excerpt from the Python Data Science Handbook by Jake VanderPlas; the content is available on GitHub.

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## 1 Hierarchical Indexing

Up to this point we've been focused primarily on one-dimensional and two-dimensional data, stored in Pandas Series and DataFrame objects, respectively. Often it is useful to go beyond this and store higher-dimensional data—that is, data indexed by more than one or two keys. While Pandas does provide Panel and Panel 4D objects that natively handle three-dimensional and four-dimensional data (see Aside: Panel Data), a far more common pattern in practice is to make use of hierarchical indexing (also known as multi-indexing) to incorporate multiple index levels within a single index. In this way, higher-dimensional data can be compactly represented within the familiar one-dimensional Series and two-dimensional DataFrame objects.

In this section, we'll explore the direct creation of MultiIndex objects, considerations when indexing, slicing, and computing statistics across multiply indexed data, and useful routines for converting between simple and hierarchically indexed representations of your data.

We begin with the standard imports:

```
In [1]: import pandas as pd
    import numpy as np
```

### 1.1 A Multiply Indexed Series

Let's start by considering how we might represent two-dimensional data within a onedimensional Series. For concreteness, we will consider a series of data where each point has a character and numerical key.

### 1.1.1 The bad way

Suppose you would like to track data about states from two different years. Using the Pandas tools we've already covered, you might be tempted to simply use Python tuples as keys:

```
('Texas', 2000), ('Texas', 2010)]
        populations = [33871648, 37253956,
                       18976457, 19378102,
                       20851820, 25145561]
        pop = pd.Series(populations, index=index)
        pop
Out[2]: (California, 2000)
                              33871648
        (California, 2010)
                              37253956
        (New York, 2000)
                              18976457
        (New York, 2010)
                              19378102
        (Texas, 2000)
                              20851820
        (Texas, 2010)
                              25145561
        dtype: int64
```

With this indexing scheme, you can straightforwardly index or slice the series based on this multiple index:

But the convenience ends there. For example, if you need to select all values from 2010, you'll need to do some messy (and potentially slow) munging to make it happen:

This produces the desired result, but is not as clean (or as efficient for large datasets) as the slicing syntax we've grown to love in Pandas.

#### 1.1.2 The Better Way: Pandas MultiIndex

Fortunately, Pandas provides a better way. Our tuple-based indexing is essentially a rudimentary multi-index, and the Pandas MultiIndex type gives us the type of operations we wish to have. We can create a multi-index from the tuples as follows:

Notice that the MultiIndex contains multiple *levels* of indexing—in this case, the state names and the years, as well as multiple *labels* for each data point which encode these levels.

If we re-index our series with this MultiIndex, we see the hierarchical representation of the data:

```
In [6]: pop = pop.reindex(index)
       pop
Out[6]: California 2000
                           33871648
                   2010
                           37253956
       New York
                  2000
                           18976457
                   2010
                          19378102
                   2000
                           20851820
       Texas
                   2010
                           25145561
       dtype: int64
```

Here the first two columns of the Series representation show the multiple index values, while the third column shows the data. Notice that some entries are missing in the first column: in this multi-index representation, any blank entry indicates the same value as the line above it.

Now to access all data for which the second index is 2010, we can simply use the Pandas slicing notation:

The result is a singly indexed array with just the keys we're interested in. This syntax is much more convenient (and the operation is much more efficient!) than the home-spun tuple-based multi-indexing solution that we started with. We'll now further discuss this sort of indexing operation on hieararchically indexed data.

#### 1.1.3 MultiIndex as extra dimension

You might notice something else here: we could easily have stored the same data using a simple <code>DataFrame</code> with index and column labels. In fact, Pandas is built with this equivalence in mind. The <code>unstack()</code> method will quickly convert a multiply indexed <code>Series</code> into a conventionally indexed <code>DataFrame</code>:

Naturally, the stack() method provides the opposite operation:

```
In [9]: pop_df.stack()
Out[9]: California
                     2000
                              33871648
                     2010
                              37253956
        New York
                     2000
                             18976457
                     2010
                             19378102
                     2000
                             20851820
        Texas
                     2010
                              25145561
        dtype: int64
```

Seeing this, you might wonder why would we would bother with hierarchical indexing at all. The reason is simple: just as we were able to use multi-indexing to represent two-dimensional data within a one-dimensional Series, we can also use it to represent data of three or more dimensions in a Series or DataFrame. Each extra level in a multi-index represents an extra dimension of data; taking advantage of this property gives us much more flexibility in the types of data we can represent. Concretely, we might want to add another column of demographic data for each state at each year (say, population under 18); with a MultiIndex this is as easy as adding another column to the DataFrame:

```
In [10]: pop_df = pd.DataFrame({'total': pop,
                                'under18': [9267089, 9284094,
                                            4687374, 4318033,
                                            5906301, 6879014]})
        pop_df
Out[10]:
                            total under18
        California 2000
                         33871648
                                    9267089
                   2010
                         37253956
                                    9284094
                   2000 18976457 4687374
        New York
                   2010 19378102
                                    4318033
         Texas
                   2000
                         20851820
                                    5906301
                   2010
                         25145561
                                    6879014
```

In addition, all the ufuncs and other functionality discussed in Operating on Data in Pandas work with hierarchical indices as well. Here we compute the fraction of people under 18 by year, given the above data:

This allows us to easily and quickly manipulate and explore even high-dimensional data.

### 1.2 Methods of MultiIndex Creation

The most straightforward way to construct a multiply indexed Series or DataFrame is to simply pass a list of two or more index arrays to the constructor. For example:

The work of creating the MultiIndex is done in the background.

Similarly, if you pass a dictionary with appropriate tuples as keys, Pandas will automatically recognize this and use a MultiIndex by default:

```
In [13]: data = {('California', 2000): 33871648,
                 ('California', 2010): 37253956,
                 ('Texas', 2000): 20851820,
                 ('Texas', 2010): 25145561,
                 ('New York', 2000): 18976457,
                 ('New York', 2010): 19378102}
         pd. Series (data)
Out[13]: California 2000
                              33871648
                     2010
                             37253956
         New York
                    2000
                             18976457
                     2010
                             19378102
         Texas
                     2000
                             20851820
                     2010
                             25145561
         dtype: int64
```

Nevertheless, it is sometimes useful to explicitly create a MultiIndex; we'll see a couple of these methods here.

### 1.2.1 Explicit MultiIndex constructors

For more flexibility in how the index is constructed, you can instead use the class method constructors available in the pd.MultiIndex. For example, as we did before, you can construct the MultiIndex from a simple list of arrays giving the index values within each level:

You can construct it from a list of tuples giving the multiple index values of each point:

You can even construct it from a Cartesian product of single indices:

Similarly, you can construct the MultiIndex directly using its internal encoding by passing levels (a list of lists containing available index values for each level) and labels (a list of lists that reference these labels):

Any of these objects can be passed as the index argument when creating a Series or Dataframe, or be passed to the reindex method of an existing Series or DataFrame.

#### 1.2.2 MultiIndex level names

Sometimes it is convenient to name the levels of the MultiIndex. This can be accomplished by passing the names argument to any of the above MultiIndex constructors, or by setting the names attribute of the index after the fact:

```
In [18]: pop.index.names = ['state', 'year']
        pop
Out[18]: state
                    year
        California 2000
                            33871648
                    2010
                            37253956
        New York 2000 18976457
                    2010
                            19378102
        Texas
                    2000
                            20851820
                    2010
                            25145561
        dtype: int64
```

With more involved datasets, this can be a useful way to keep track of the meaning of various index values.

#### 1.2.3 MultiIndex for columns

In a DataFrame, the rows and columns are completely symmetric, and just as the rows can have multiple levels of indices, the columns can have multiple levels as well. Consider the following, which is a mock-up of some (somewhat realistic) medical data:

```
In [19]: # hierarchical indices and columns
         index = pd.MultiIndex.from_product([[2013, 2014], [1, 2]],
                                             names=['year', 'visit'])
         columns = pd.MultiIndex.from_product([['Bob', 'Guido', 'Sue'], ['HR', 'Ter
                                                names=['subject', 'type'])
         # mock some data
         data = np.round(np.random.randn(4, 6), 1)
         data[:, ::2] *= 10
         data += 37
         # create the DataFrame
         health_data = pd.DataFrame(data, index=index, columns=columns)
         health_data
Out[19]: subject
                      Bob
                                 Guido
                                                Sue
         type
                        HR
                            Temp
                                    HR
                                        Temp
                                                 HR
                                                     Temp
         year visit
         2013 1
                      31.0
                            38.7
                                  32.0
                                        36.7
                                               35.0
                                                     37.2
              2
                      44.0
                          37.7
                                  50.0
                                        35.0
                                              29.0
                                                     36.7
         2014 1
                      30.0 37.4
                                  39.0
                                        37.8
                                             61.0
                                                     36.9
                      47.0 37.8
                                  48.0
                                        37.3
                                             51.0
                                                     36.5
              2
```

Here we see where the multi-indexing for both rows and columns can come in *very* handy. This is fundamentally four-dimensional data, where the dimensions are the subject, the measurement type, the year, and the visit number. With this in place we can, for example, index the top-level column by the person's name and get a full DataFrame containing just that person's information:

For complicated records containing multiple labeled measurements across multiple times for many subjects (people, countries, cities, etc.) use of hierarchical rows and columns can be extremely convenient!

### 1.3 Indexing and Slicing a MultiIndex

Indexing and slicing on a MultiIndex is designed to be intuitive, and it helps if you think about the indices as added dimensions. We'll first look at indexing multiply indexed Series, and then multiply-indexed DataFrames.

### 1.3.1 Multiply indexed Series

Consider the multiply indexed Series of state populations we saw earlier:

```
In [21]: pop
Out[21]: state
                    year
        California 2000
                             33871648
                     2010
                            37253956
                    2000
        New York
                            18976457
                    2010
                            19378102
         Texas
                    2000
                            20851820
                     2010
                            25145561
         dtype: int64
```

We can access single elements by indexing with multiple terms:

```
In [22]: pop['California', 2000]
Out[22]: 33871648
```

The MultiIndex also supports *partial indexing*, or indexing just one of the levels in the index. The result is another Series, with the lower-level indices maintained:

Partial slicing is available as well, as long as the MultiIndex is sorted (see discussion in Sorted and Unsorted Indices):

With sorted indices, partial indexing can be performed on lower levels by passing an empty slice in the first index:

Other types of indexing and selection (discussed in Data Indexing and Selection) work as well; for example, selection based on Boolean masks:

Selection based on fancy indexing also works:

### 1.3.2 Multiply indexed DataFrames

A multiply indexed DataFrame behaves in a similar manner. Consider our toy medical DataFrame from before:

```
In [28]: health_data
Out[28]: subject
                                Guido
                      Bob
                                               Sue
         type
                       HR
                          Temp
                                   HR
                                       Temp
                                               HR
                                                    Temp
         year visit
                          38.7 32.0
         2013 1
                     31.0
                                       36.7
                                             35.0
                                                    37.2
              2
                     44.0 37.7
                                 50.0
                                       35.0
                                             29.0
                                                    36.7
         2014 1
                     30.0 37.4 39.0
                                       37.8
                                             61.0
                                                    36.9
                     47.0 37.8 48.0
                                       37.3
                                             51.0
                                                    36.5
```

Remember that columns are primary in a DataFrame, and the syntax used for multiply indexed Series applies to the columns. For example, we can recover Guido's heart rate data with a simple operation:

Also, as with the single-index case, we can use the loc, iloc, and ix indexers introduced in Data Indexing and Selection. For example:

These indexers provide an array-like view of the underlying two-dimensional data, but each individual index in loc or iloc can be passed a tuple of multiple indices. For example:

Working with slices within these index tuples is not especially convenient; trying to create a slice within a tuple will lead to a syntax error:

You could get around this by building the desired slice explicitly using Python's built-in slice() function, but a better way in this context is to use an IndexSlice object, which Pandas provides for precisely this situation. For example:

There are so many ways to interact with data in multiply indexed Series and DataFrames, and as with many tools in this book the best way to become familiar with them is to try them out!

### 1.4 Rearranging Multi-Indices

One of the keys to working with multiply indexed data is knowing how to effectively transform the data. There are a number of operations that will preserve all the information in the dataset, but rearrange it for the purposes of various computations. We saw a brief example of this in the stack() and unstack() methods, but there are many more ways to finely control the rearrangement of data between hierarchical indices and columns, and we'll explore them here.

#### 1.4.1 Sorted and unsorted indices

Earlier, we briefly mentioned a caveat, but we should emphasize it more here. *Many of the MultiIndex slicing operations will fail if the index is not sorted.* Let's take a look at this here.

We'll start by creating some simple multiply indexed data where the indices are *not lexographically sorted*:

```
In [34]: index = pd.MultiIndex.from_product([['a', 'c', 'b'], [1, 2]])
         data = pd.Series(np.random.rand(6), index=index)
         data.index.names = ['char', 'int']
         data
Out[34]: char int
         а
               1
                      0.003001
                      0.164974
               2.
               1
                      0.741650
               2.
                      0.569264
               1
                      0.001693
                      0.526226
         dtype: float64
```

If we try to take a partial slice of this index, it will result in an error:

Although it is not entirely clear from the error message, this is the result of the MultiIndex not being sorted. For various reasons, partial slices and other similar operations require the levels in the MultiIndex to be in sorted (i.e., lexographical) order. Pandas provides a number of convenience routines to perform this type of sorting; examples are the sort\_index() and sortlevel() methods of the DataFrame. We'll use the simplest, sort\_index(), here:

```
Out[36]: char
                int
                        0.003001
          а
                1
                2
                        0.164974
                1
                        0.001693
         b
                2
                        0.526226
                1
                        0.741650
                2
                        0.569264
          dtype: float64
```

With the index sorted in this way, partial slicing will work as expected:

### 1.4.2 Stacking and unstacking indices

As we saw briefly before, it is possible to convert a dataset from a stacked multi-index to a simple two-dimensional representation, optionally specifying the level to use:

```
In [38]: pop.unstack(level=0)
Out[38]: state California New York
                                          Texas
         year
                                       20851820
         2000
                  33871648
                            18976457
         2010
                  37253956
                            19378102
                                       25145561
In [39]: pop.unstack(level=1)
Out[39]: year
                         2000
                                    2010
         state
         California 33871648
                                37253956
         New York
                     18976457
                                19378102
                     20851820
                               25145561
         Texas
```

The opposite of unstack () is stack (), which here can be used to recover the original series:

```
In [40]: pop.unstack().stack()
Out[40]: state
                      year
         California
                      2000
                              33871648
                      2010
                              37253956
                      2000
         New York
                              18976457
                      2010
                              19378102
         Texas
                      2000
                              20851820
                      2010
                              25145561
         dtype: int64
```

### 1.4.3 Index setting and resetting

Another way to rearrange hierarchical data is to turn the index labels into columns; this can be accomplished with the reset\_index method. Calling this on the population dictionary will result in a DataFrame with a *state* and *year* column holding the information that was formerly in the index. For clarity, we can optionally specify the name of the data for the column representation:

```
In [41]: pop_flat = pop.reset_index(name='population')
         pop_flat
Out [41]:
                  state year
                               population
                         2000
         0
            California
                                 33871648
         1
            California 2010
                                 37253956
         2
              New York 2000
                                 18976457
         3
              New York 2010
                                 19378102
         4
                         2000
                                 20851820
                 Texas
         5
                  Texas
                         2010
                                 25145561
```

Often when working with data in the real world, the raw input data looks like this and it's useful to build a MultiIndex from the column values. This can be done with the set\_index method of the DataFrame, which returns a multiply indexed DataFrame:

```
In [42]: pop_flat.set_index(['state', 'year'])
Out [42]:
                            population
         state
                     year
         California 2000
                              33871648
                     2010
                              37253956
         New York
                     2000
                              18976457
                     2010
                              19378102
         Texas
                     2000
                              20851820
                     2010
                              25145561
```

In practice, I find this type of reindexing to be one of the more useful patterns when encountering real-world datasets.

### 1.5 Data Aggregations on Multi-Indices

We've previously seen that Pandas has built-in data aggregation methods, such as mean(), sum(), and max(). For hierarchically indexed data, these can be passed a level parameter that controls which subset of the data the aggregate is computed on.

For example, let's return to our health data:

```
In [43]: health_data
Out [43]: subject
                        Bob
                                    Guido
                                                   Sue
          type
                         HR
                              Temp
                                       HR
                                           Temp
                                                    HR
                                                         Temp
          vear visit
          2013 1
                              38.7
                                     32.0
                                            36.7
                                                  35.0
                                                         37.2
                       31.0
               2
                       44.0
                              37.7
                                     50.0
                                            35.0
                                                  29.0
                                                         36.7
          2014 1
                       30.0
                              37.4
                                     39.0
                                           37.8
                                                  61.0
                                                         36.9
                       47.0 37.8
                                     48.0
                                           37.3
               2
                                                  51.0
                                                         36.5
```

Perhaps we'd like to average-out the measurements in the two visits each year. We can do this by naming the index level we'd like to explore, in this case the year:

```
In [44]: data_mean = health_data.mean(level='year')
         data_mean
Out[44]: subject
                    Bob
                               Guido
                                                Sue
         type
                     HR
                          Temp
                                   HR
                                        Temp
                                                 HR
                                                      Temp
         year
         2013
                   37.5
                          38.2
                                41.0
                                       35.85
                                               32.0
                                                     36.95
                   38.5
                         37.6
                                43.5
                                       37.55
         2.014
                                               56.0
                                                     36.70
```

By further making use of the axis keyword, we can take the mean among levels on the columns as well:

Thus in two lines, we've been able to find the average heart rate and temperature measured among all subjects in all visits each year. This syntax is actually a short cut to the GroupBy functionality, which we will discuss in Aggregation and Grouping. While this is a toy example, many real-world datasets have similar hierarchical structure.

#### 1.6 Aside: Panel Data

Pandas has a few other fundamental data structures that we have not yet discussed, namely the pd.Panel and pd.Panel4D objects. These can be thought of, respectively, as three-dimensional and four-dimensional generalizations of the (one-dimensional) Series and (two-dimensional) DataFrame structures. Once you are familiar with indexing and manipulation of data in a Series and DataFrame, Panel and Panel4D are relatively straightforward to use. In particular, the ix, loc, and iloc indexers discussed in Data Indexing and Selection extend readily to these higher-dimensional structures.

We won't cover these panel structures further in this text, as I've found in the majority of cases that multi-indexing is a more useful and conceptually simpler representation for higher-dimensional data. Additionally, panel data is fundamentally a dense data representation, while multi-indexing is fundamentally a sparse data representation. As the number of dimensions increases, the dense representation can become very inefficient for the majority of real-world datasets. For the occasional specialized application, however, these structures can be useful. If you'd like to read more about the Panel and Panel 4D structures, see the references listed in Further Resources.

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