(Show video!)

Project 5: "Schwödinger's double slit"/ double-slit in abox

- · Q: How many has taken a rourse on QM? (not needed)
- Topics: PDEs in \$ 2+7 din - Crank - Dicolson (implicit scheme)
 - Working with complex numbers
 - Some matrix considerations ..
 - Probobility
 - · Schr. eq:

ind 14) = f1/4)

· In position space, for single particle, two dim.

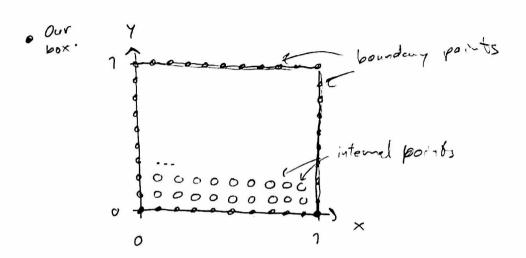
$$\frac{i\hbar \frac{\partial}{\partial t} \Psi(x,y,t)}{\partial t} = -\frac{\hbar^2}{2m} \left[\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right] \Psi(x,y,t) + \frac{1}{2m} \frac{1}{2m} \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \frac{1}{2m} \frac{1}{2$$

o Born vule:

p(r,y;t) = 14(r,y,t) = 4(x,y,t) +(x,y,t)

o Our rase: All dim. less! General form of the diff eq.

$$i\frac{\partial}{\partial t} u = -\frac{\partial^2}{\partial x^2} u - \frac{\partial^2}{\partial y^2} u + V(x,y) u$$
Now a time-indep potential



- · x & (0,1), Y & [0,1]
- · Ax = Ay = h
- o M points in each direction (incl boundar, points)

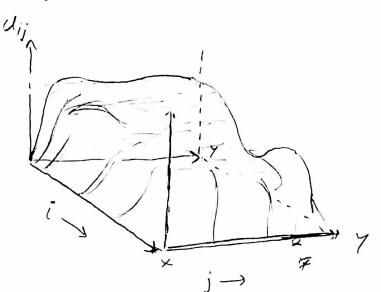
 L3 M-7 steps

 L3 M-7 juteenal points

$$o \quad Y \rightarrow Y_{j} = jh \qquad i,j = 0,1,2,...,M-1$$

· V(x,y) -> Vij

· U, and V; are furtions on the xy plane



- o we'll use conservation of probability as a consistency check.
 - · Vij is fixed in time
 - · But for uij one cative good of values for each timestep -> one matrix per timestop
 - o In this project we will need to swop between matrix and vector representation of our soulution:

