Assignment 01 Differential Equations Fall 2023 BS-V (CS) Sections B,C,D,E Course Supervisor Adnan Rauf

Solve nonlinear Lorenz Model in Google Collaboratory

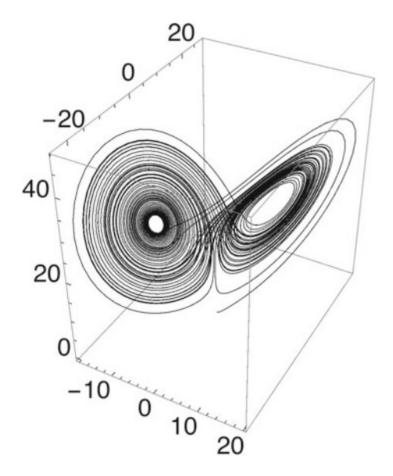
See the following page for details

Note:

- (1) Submit your Assignment as a PDF File with a live link for Google Collaboratory Jupyter Notebook
- (2) Graph of the solution should include a time series plot for each variable x y and z
- (3) A 3D phase portrait plot of x y z variables.
- (4) Elaborate the phenomena of sensitive dependence on initial conditions exhibited by the Lorenz Model
- (5) What is Butterfly Effect

A legendary model is that of meteorologist Edward N. Lorenz (1917–2008), who brought significant insights to the theory of **deterministic chaos**. It is described by the following system of nonlinear differential equations:

$$\begin{vmatrix} \dot{x} = a(y-x) \\ \dot{y} = x(b-z) - y \\ \dot{z} = xy - cz \end{vmatrix}.$$



The figure⁵ shows the associated graph of the numerical solution for parameter values a = 10, b = 28, c = 8/3 with initial values (x(0), y(0), z(0)) = (0, 1, 0).

Using his model, Lorenz discovered that very small changes in the initial conditions can eventually evolve into considerably different solutions. This explains why precise long-range weather forecasting is impossible. But he also found that the solutions all are confined to a narrow region of space, hence a certain structure is maintained. More on this can be found in [1].