

1.

1)

since $(u, v) \in E' \Leftrightarrow \exists x \in V, (u, x) \wedge (x, v) \in E$ and the graph is given in an adjacency list, we could loop through that list and for each vertex go to all its adjacent vertices, and then all the vertices adjacent to those would be made adjacent to the original vertex in G' . pseudo code would look like

```

for each v in vertices
  k = new vertex;
  for each i in v.adjacent
    for each j in i.adjacent
      k.adjacent.add(j);
  vertices_prime.add(k);

```

where $|v.\text{adjacent}| + |i.\text{adjacent}| \leq |E|$ so the max time bound would be $|V| \times |E| = O(mn)$

2)

```

for(var i = 0; i < matrix.length; i++){
  for(var j = 0; j < matrix.length; j++){
    if(matrix[i][j]){
      for(var k = 0; k < matrix.length; k++){
        if(matrix[j][k] && k != i){
          new_matrix[i][k] = 1;
        }
      }
    }
  }
}

```

since $\text{if}(\text{matrix}[i][j])$ is true exactly $|E|$ times the total run time would be $|V|^2 + |E| \times |V|$ because the inner most loop will run $|E|$ times.

2.