

Lista 2, zadania 3, 4, 5

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Zadanie 3

a) $K(s) = \frac{1}{s^2+s}$

Odpowiedź skokowa:

$$\lambda(t) = \mathcal{L}^{-1} \left\{ \frac{1}{s} \cdot K(s) \right\}$$

$$\lambda(t) = \mathcal{L}^{-1} \left\{ \frac{1}{s(s^2+s)} \right\}$$

$$\lambda(t) = \mathcal{L}^{-1} \left\{ \frac{1}{s+1} - \frac{1}{s} + \frac{1}{s^2} \right\}$$

$$\lambda(t) = t - 1 + e^{-t}$$

$$\lambda'(t) = 1 - e^{-t}$$

$$\lambda''(t) = e^{-t}$$

$$\lambda(0) = 0$$

$$\lambda'(0) = 0$$

$$\lambda''(0) = 1$$

Odpowiedź impulsowa:

$$k(t) = \mathcal{L}^{-1} \{K(s)\}$$

$$k(t) = \mathcal{L}^{-1} \left\{ \frac{1}{s^2 + s} \right\}$$

$$k(t) = \mathcal{L}^{-1} \left\{ -\frac{1}{s+1} + \frac{1}{s} \right\}$$

$$k(t) = 1 - e^{-t}$$

$$k'(t) = e^{-t}$$

$$k''(t) = -e^{-t}$$

$$k(0) = 0$$

$$k'(0) = 1$$

$$k''(0) = -1$$

b) $K(s) = \frac{1}{(s+1)(s^2+1)}$

Odpowiedź skokowa:

$$\lambda(t) = \mathcal{L}^{-1} \left\{ \frac{1}{s} \cdot K(s) \right\}$$

$$\lambda(t) = \mathcal{L}^{-1} \left\{ \frac{1}{s} \cdot \frac{1}{(s+1)(s^2+1)} \right\}$$

$$\lambda(t) = \mathcal{L}^{-1} \left\{ -\frac{s+1}{2(s^2+1)} - \frac{1}{2(s+1)} + \frac{1}{s} \right\}$$

$$\lambda(t) = -\frac{\sin(t)}{2} - \frac{\cos(t)}{2} + 1 - \frac{e^{-t}}{2}$$

$$\lambda'(t) = \frac{\sin(t)}{2} - \frac{\cos(t)}{2} + \frac{e^{-t}}{2}$$

$$\lambda''(t) = \frac{\sin(t)}{2} + \frac{\cos(t)}{2} - \frac{e^{-t}}{2}$$

$$\lambda(0) = 0$$

$$\lambda'(0) = 0$$