## EE24BTECH11032 - John Bobby

**Question:**Calculate the area under the curve  $y = 2\sqrt{x}$  included with the lines x = 1 and x = 0.

**Solution:** For a line  $\mathbf{x} = \mathbf{h} + k\mathbf{m}$ , the intersection of the line with a conic with parameters  $\mathbf{V}$ ,  $\mathbf{u}$ ,  $\mathbf{h}$ ,  $\mathbf{m}$  and  $\mathbf{h}$  is given by  $\mathbf{x} = \mathbf{h} + k_i \mathbf{m}$ 

 $L_1 : x = 0$  $L_2 : x = 1$ 

$$k_{i} = \frac{1}{\mathbf{m}^{\top} \mathbf{V} \mathbf{m}} \left( -\mathbf{m}^{\top} \left( \mathbf{V} \mathbf{h} + \mathbf{u} \right) + \sqrt{\left[ \mathbf{m}^{\top} \left( \mathbf{V} \mathbf{h} + \mathbf{u} \right) \right]^{2} - g \left( \mathbf{h} \right) \left( \mathbf{m}^{\top} \mathbf{V} \mathbf{m} \right)} \right)$$
(0.1)

on solving for  $L_1$  and  $L_2$ 

$$k_1 = 0, k_2 = 2 \tag{0.2}$$

$$\mathbf{A} = \mathbf{h_1} + k_1 \mathbf{m_1} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} + 0 \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \tag{0.3}$$

$$\mathbf{B} = \mathbf{h_2} + k_2 \mathbf{m_2} = \begin{pmatrix} 1 \\ 0 \end{pmatrix} + 2 \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 2 \end{pmatrix} \tag{0.4}$$

Thus the area under the curve included with the lines x = 1 and x = 0 is given by

$$\int_0^1 2\sqrt{x} \, dx = \left(\frac{4}{3}x^{\frac{3}{2}}\right)_0^1 = \frac{4}{3} \tag{0.5}$$

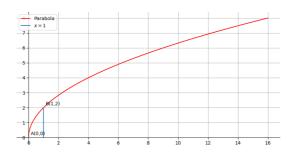


Fig. 0.1: Plot of Parabola

Variable	Description	Value
$\mathbf{m_1}$	direction vector of $L_1$	$\begin{pmatrix} 0 \\ 1 \end{pmatrix}$
m <sub>2</sub>	direction vector of $L_2$	$\begin{pmatrix} 0 \\ 1 \end{pmatrix}$
h <sub>1</sub>	vector passing through $L_1$	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$
h <sub>2</sub>	vector passing through $L_2$	$\begin{pmatrix} 1 \\ 0 \end{pmatrix}$
V	Conic parameter	$\begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}$
u	Conic parameter	$\begin{pmatrix} -2 \\ 0 \end{pmatrix}$
f	Conic parameter	0

TABLE 0: Input Parameters