# Survival Analysis Methodology

**Last Updated:** 2025-10-24

**Framework Version:** 1.0

This document describes the theoretical foundations and implementation approach for the survival analysis framework. It is maintained alongside code changes to ensure consistency between theory and implementation.

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## Introduction

### Purpose

This framework implements survival analysis for predicting customer churn/termination events. Unlike binary classification (will churn: yes/no) or time-series forecasting, survival analysis jointly models:

1. **Whether** an event will occur (termination)
2. **When** the event will occur (survival time)
3. **Censored observations** where the event has not yet occurred

### Key Advantages

* Handles right-censored data (customers still active at observation end)
* Provides time-dependent risk predictions
* Estimates expected survival time for each customer
* Quantifies uncertainty through survival probabilities

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## Survival Analysis Fundamentals

### Core Concepts

**Survival Function S(t)**

The survival function represents the probability that an individual survives beyond time t:

S(t) = P(T > t)

Where:

* T is the random variable representing survival time
* S(t) is monotonically decreasing: S(0) = 1, lim(t→∞) S(t) = 0
* In our context: probability that a customer remains active beyond t months

**Hazard Function h(t)**

The hazard function represents the instantaneous risk of the event occurring at time t, given survival up to t:

h(t) = lim(Δt→0) P(t ≤ T < t + Δt | T ≥ t) / Δt

Properties:

* h(t) ≥ 0 for all t
* Higher hazard = higher instantaneous risk
* Relationship to survival: S(t) = exp(-∫₀ᵗ h(u)du)

**Cumulative Hazard Function H(t)**

H(t) = ∫₀ᵗ h(u)du = -log(S(t))

**Censoring**

**Right Censoring** occurs when the event has not been observed by the end of the study period:

* **Event indicator**: δ = 1 if event observed, δ = 0 if censored
* **Observed time**: T\_obs = min(T\_event, T\_censoring)
* Censored observations provide partial information: "survived at least until T\_obs"

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## Model Implementations

### 1. Cox Proportional Hazards (Cox PH)

**Theory**

The Cox PH model assumes the hazard function can be written as:

h(t|X) = h₀(t) · exp(β'X)

Where:

* h₀(t) is the baseline hazard (unspecified, non-parametric)
* β is the vector of coefficients
* X is the covariate vector
* exp(β'X) is the risk score (hazard ratio)

**Proportional Hazards Assumption**: The ratio of hazards for two individuals is constant over time.

**Implementation Details**

**Module**: `CoxPHWrapper` in `models.py`

* Uses `CoxPHSurvivalAnalysis` from scikit-survival
* **L2 Regularization** (Ridge): α = 1.0 by default to prevent numerical instability
* Optimization: Newton-Raphson with 200 iterations, tolerance 1e-9
* Input validation: checks for finite values, minimum sample size, non-zero variance

**Why L2 Regularization?**

* Prevents LAPACK errors from multicollinearity
* Stabilizes coefficient estimates with high-dimensional data
* Default α=1.0 balances stability and model flexibility

### 2. Elastic Net Cox (Coxnet)

**Theory**

Extends Cox PH with elastic net penalty (L1 + L2 regularization):

minimize: -log-likelihood + λ[(1-α)/2 ||β||₂² + α||β||₁]

Where:

* λ controls overall regularization strength
* α ∈ [0,1] controls L1/L2 mix
* α=1: Lasso (feature selection)
* α=0: Ridge (shrinkage only)
* 0<α<1: Elastic net (both)

**Implementation Details**

**Module**: `CoxnetWrapper` in `models.py`

* Uses `CoxnetSurvivalAnalysis` from scikit-survival
* Default: l1\_ratio=0.5 (balanced L1/L2)
* Automatic regularization path selection via cross-validation
* Feature selection through L1 penalty

### 3. Weibull Accelerated Failure Time (AFT)

**Theory**

AFT models assume covariates act multiplicatively on survival time:

log(T) = β'X + σε

Where:

* ε follows a specified distribution (Weibull in our case)
* σ is a scale parameter
* exp(β'X) is the acceleration factor

Weibull distribution:

S(t|X) = exp(-(λt)ᵖ) where λ = exp(-β'X/σ)

* p > 1: increasing hazard (aging)
* p < 1: decreasing hazard
* p = 1: constant hazard (exponential)

**Implementation Details**

**Module**: `WeibullAFTWrapper` in `models.py`

* Uses `WeibullAFTFitter` from lifelines
* Parametric model with interpretable acceleration factors
* Requires DataFrame input with 'time' and 'event' columns
* Directly models survival time distribution

### 4. Gradient Boosting Survival Analysis (GBSA)

**Theory**

Ensemble method that builds an additive model:

h(t|X) = h₀(t) · exp(∑ᵢ fᵢ(X))

Where each fᵢ is a regression tree fitted to negative gradients of the partial likelihood loss.

**Advantages**:

* Captures non-linear relationships
* Handles interactions automatically
* Robust to irrelevant features
* No proportional hazards assumption

**Implementation Details**

**Module**: `GBSAWrapper` in `models.py`

* Uses `GradientBoostingSurvivalAnalysis` from scikit-survival
* Tree-based ensemble with boosting
* Flexible non-parametric approach
* Often achieves best predictive performance

### 5. Random Survival Forest (RSF)

**Theory**

Extension of random forests to survival data:

1. Bootstrap sample from training data
2. At each node, randomly select subset of features
3. Split node to maximize survival difference (log-rank test)
4. Aggregate predictions across trees

**Cumulative Hazard Estimate**:

Ĥ(t|X) = average over trees of cumulative hazard in terminal node

**Implementation Details**

**Module**: `RSFWrapper` in `models.py`

* Uses `RandomSurvivalForest` from scikit-survival
* Ensemble of survival trees
* Handles non-linear patterns and interactions
* Provides feature importance measures

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## Data Preprocessing Pipeline

### Pipeline Architecture

The preprocessing pipeline (`make\_pipeline()` in `data.py`) consists of three stages:

Input Data → Preprocessing → Variance Filtering → Survival Model

### Stage 1: Column Transformation

**Numeric Features**:

Pipeline([  
 SimpleImputer(strategy='median', add\_indicator=True),  
 StandardScaler()  
])

* **Imputation**: Missing values replaced with median
* **Missing indicators**: Binary flags for missingness (preserves information)
* **Scaling**: Zero mean, unit variance (required for Cox models)

**Categorical Features**:

Pipeline([  
 SimpleImputer(strategy='most\_frequent', add\_indicator=True),  
 OneHotEncoder(drop='first', handle\_unknown='ignore')  
])

* **Imputation**: Missing values replaced with mode
* **Missing indicators**: Binary flags for missingness
* **One-hot encoding**: drop='first' to avoid multicollinearity
* **Unknown handling**: Assigns all-zero vector for new categories

### Stage 2: Variance Threshold

VarianceThreshold(threshold=1e-12)

**Purpose**: Remove effectively constant features that cause:

* Singular covariance matrices
* LAPACK numerical errors
* Unstable coefficient estimates

**Rationale**: Features with variance < 1e-12 provide no discriminative information and destabilize matrix operations in Cox models.

### Stage 3: Survival Model

The fitted model from Stage 1-2 is passed to the survival estimator.

### Why This Design?

1. **Missing value handling**: Prevents NaN propagation while preserving missingness as a signal
2. **Numerical stability**: Scaling + variance filtering prevent matrix singularity
3. **Regularization compatibility**: Scaled features enable fair L1/L2 penalties
4. **Censoring-aware**: All stages preserve sample indices for proper y alignment

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## Evaluation Metrics

### 1. Concordance Index (C-index)

**Definition**

Measures the proportion of all comparable pairs where predictions and outcomes are concordant:

C-index = P(risk\_i > risk\_j | time\_i < time\_j, event\_i = 1)

**Interpretation**:

* 0.5: Random predictions
* 1.0: Perfect discrimination
* >0.7: Generally considered good
* Analogous to AUC-ROC for survival data

**Implementation**

* Uses Harrell's C-index with IPCW (inverse probability of censoring weighting)
* Handles censored observations appropriately
* Primary metric for model comparison

### 2. Integrated Brier Score (IBS)

**Definition**

Measures prediction accuracy across time by averaging Brier scores:

BS(t) = (1/n) ∑ᵢ [S(t|Xᵢ) - I(Tᵢ > t)]² · W(Tᵢ, δᵢ, t)  
IBS = ∫ BS(t) dt / (t\_max - t\_min)

Where W is the IPCW weight accounting for censoring.

**Interpretation**:

* 0: Perfect calibration
* Lower is better
* Measures both discrimination and calibration
* Time-dependent metric

**Implementation**

* Evaluated at time horizons: 3, 6, 12, 18, 24 months
* Uses IPCW to handle censoring
* Secondary metric for model selection

### 3. Time-Dependent AUC

**Definition**

Extension of ROC AUC for time-varying predictions:

AUC(t) = P(risk\_i > risk\_j | Tᵢ = t, Tⱼ > t)

**Interpretation**:

* Discrimination at specific time point t
* 0.5: Random classifier
* 1.0: Perfect discrimination
* Evaluated at multiple time horizons

**Implementation**

* Uses cumulative/dynamic AUC definition
* Evaluated at CV time horizons
* Provides time-specific performance insights

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## Cross-Validation Strategy

### Event-Balanced Stratified K-Fold

**Motivation**

Standard K-fold can create folds with:

* Imbalanced event rates (e.g., 5% vs 15%)
* Insufficient events for model fitting
* Biased performance estimates

**Implementation**

**Function**: `event\_balanced\_splitter()` in `validation.py`

StratifiedKFold(n\_splits=5, shuffle=True, random\_state=42)

**Stratification variable**: Event indicator (δ)

**Ensures**:

* Each fold has approximately equal proportion of events
* Both censored and event samples in train/test
* Representative folds for unbiased evaluation

### Fold-Aware Time Grid Constraints

**Problem**: Survival metrics require time points within the test set's observed range.

**Solution**: `default\_time\_grid()` with test set constraints:

t\_min = max(train\_5th\_percentile, test\_min + 0.1)  
t\_max = min(train\_95th\_percentile, test\_max - 0.1)

**Benefits**:

* Prevents extrapolation errors
* Avoids "all times must be within follow-up" errors
* Ensures valid metric computation

### Cross-Validation Workflow

For each model:

1. Create 5 event-balanced folds
2. For each fold:

* Fit preprocessing + model on training data
* Generate fold-aware time grid
* Predict on test fold
* Compute C-index, IBS, time-dependent AUC
* Save predictions to `artifacts/<model>/<model>\_fold{i}\_\*.npy`

1. Aggregate metrics across folds
2. Rank models by mean C-index (primary), IBS (secondary)

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## Prediction Methodology

### Model Selection

**Criterion**: Highest mean C-index from cross-validation

**Process**:

1. Read `artifacts/model\_summary.csv`
2. Select top-ranked model (sorted by rank\_cindex, rank\_ibs)
3. Load most recent saved model from `models/`

### Survival Probability Predictions

**Point Estimates at Fixed Horizons**:

Given feature vector X and time point t:

Ŝ(t|X) = model.predict\_survival\_function(X, times=[t])

**Current horizons**: 3, 6, 12, 18, 24, 36 months

**Interpretation**:

* P(customer remains active beyond t months | features X)
* Higher probability = lower churn risk
* Used for threshold-based interventions (e.g., contact if Ŝ(12) < 0.7)

### Expected Survival Time

**Restricted Mean Survival Time (RMST)**:

E[T|X] = ∫₀ᵗᵐᵃˣ Ŝ(u|X) du

**Implementation**:

def calculate\_expected\_survival\_time(pipeline, X):  
 times = np.linspace(0, t\_max, 200)  
 surv\_probs = pipeline.predict\_survival\_function(X, times)  
 expected\_time = trapezoid(surv\_probs, times) # area under curve

**Where**:

* t\_max = maximum observed time in training data (auto-detected)
* 200 points for numerical integration (trapezoidal rule)

**Properties**:

* **Intuitive interpretation**: Average months until termination
* **Single summary metric**: Easier for business stakeholders than probability curves
* **Restricted**: Lower bound if survival curve doesn't reach 0
* **Higher value = lower risk**: Directly ranks customers by expected retention

**Use Cases**:

* Customer lifetime value estimation
* Prioritizing retention interventions
* Segmentation by risk level

### Output Format

Each prediction CSV contains per-account:

| Column | Description | Range |

| `account\_entities\_key` | Account identifier | - |

| `model\_name` | Best model used | - |

| `expected\_survival\_months` | RMST | [0, t\_max] |

| `survival\_prob\_3m` | P(survive > 3 months) | [0, 1] |

| `survival\_prob\_6m` | P(survive > 6 months) | [0, 1] |

| `survival\_prob\_12m` | P(survive > 12 months) | [0, 1] |

| `survival\_prob\_18m` | P(survive > 18 months) | [0, 1] |

| `survival\_prob\_24m` | P(survive > 24 months) | [0, 1] |

| `survival\_prob\_36m` | P(survive > 36 months) | [0, 1] |

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## Implementation Architecture

### Module Structure

survival\_framework/  
├── data.py # Data loading, preprocessing pipelines  
├── models.py # Survival model wrappers  
├── validation.py # Cross-validation, evaluation  
├── metrics.py # Survival-specific metrics  
├── predict.py # Prediction generation  
├── train.py # Training orchestration  
├── tracking.py # MLflow experiment tracking  
└── utils.py # Helper utilities

### Design Principles

1. **Unified Interface**: All models inherit from `BaseSurvivalModel` with standard `fit()`, `predict\_survival\_function()`, `score()` methods
2. **Pipeline Composition**: sklearn Pipeline pattern for reproducible preprocessing + modeling
3. **Separation of Concerns**:

* `data.py`: Feature engineering
* `models.py`: Algorithmic logic
* `validation.py`: Evaluation protocol
* `train.py`: Workflow orchestration

1. **Type Safety**: Type hints on all function signatures
2. **Comprehensive Docstrings**: Google-style docstrings with Args, Returns, Examples
3. **Experiment Tracking**: MLflow integration for reproducibility

### Key Abstractions

**Structured Array for Survival Data**

y = np.array(  
 [(event\_1, time\_1), (event\_2, time\_2), ...],  
 dtype=[('event', bool), ('time', float)]  
)

**Rationale**:

* scikit-survival standard format
* Type-safe event/time pairing
* Prevents index misalignment

**Model Wrapper Pattern**

class BaseSurvivalModel:  
 def fit(self, X, y) -> self  
 def predict\_survival\_function(self, X, times) -> np.ndarray  
 def score(self, X, y) -> float

**Benefits**:

* Consistent API across libraries (scikit-survival, lifelines)
* Easy to add new models
* Enables pipeline composition

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## Input/Output Organization

### Run Type System

The framework distinguishes between two run types to enable safe parallel development and production workflows:

RunType = Literal["sample", "production"]

**Sample Runs** (`run\_type="sample"`):

* Purpose: Development, testing, rapid iteration
* Data: Small representative subset (~2,000 records)
* Format: CSV for human readability
* Location: `data/inputs/sample/`
* Use case: Algorithm development, parameter tuning, validation

**Production Runs** (`run\_type="production"`):

* Purpose: Final models, actual predictions, deployment
* Data: Full population dataset
* Format: Pickle (recommended for >10MB) or CSV
* Location: `data/inputs/production/`
* Use case: Generating predictions for all customers

### Directory Structure

data/  
├── inputs/  
│ ├── sample/ # Development datasets  
│ │ ├── survival\_inputs\_sample2000.csv  
│ │ └── README.md  
│ └── production/ # Full population datasets  
│ ├── survival\_inputs\_complete.pkl  
│ └── README.md  
└── outputs/  
 ├── sample/ # Sample run outputs  
 │ ├── predictions/ # Prediction CSVs  
 │ │ └── survival\_predictions\_sample\_YYYYMMDD\_HHMMSS.csv  
 │ ├── artifacts/ # Training metrics, PH flags  
 │ │ ├── model\_metrics.csv  
 │ │ ├── model\_summary.csv  
 │ │ ├── ph\_flags.csv  
 │ │ └── <model>/ # Per-fold predictions  
 │ ├── models/ # Saved model pipelines  
 │ │ └── sample\_<model>.joblib\_YYYYMMDD\_HHMMSS  
 │ └── mlruns/ # MLflow experiment tracking  
 └── production/ # Production run outputs  
 ├── predictions/  
 │ └── survival\_predictions\_production\_YYYYMMDD\_HHMMSS.csv  
 ├── artifacts/  
 ├── models/  
 │ └── production\_<model>.joblib\_YYYYMMDD\_HHMMSS  
 └── mlruns/

### File Format Support

**Input Formats**:

| Format | Extension | Use Case | Performance |

| CSV | `.csv` | Human-readable, small datasets (<10MB) | Slower I/O |

| Pickle | `.pkl`, `.pickle` | Large datasets (>10MB), production | Fast I/O |

**Auto-detection**: Format determined by file extension

**Validation**: Schema checked on load (required columns, types)

**Output Formats**:

* **Predictions**: Always CSV for portability
* **Models**: Joblib (sklearn standard)
* **Artifacts**: CSV for metrics, NumPy arrays for predictions

### File Naming Conventions

All generated files include `run\_type` prefix for clear identification:

**Models**:

sample\_cox\_ph.joblib\_20251024\_143052  
production\_rsf.joblib\_20251024\_143052

**Predictions**:

survival\_predictions\_sample\_20251024\_143052.csv  
survival\_predictions\_production\_20251024\_143052.csv

**Benefits**:

* No file conflicts between sample and production runs
* Easy identification of run provenance
* Clear separation for testing vs deployment
* Reproducible experiments with timestamped artifacts

### Usage Examples

**Command-Line Interface**:

# Sample run with CSV (default)  
python src/main.py  
  
# Sample run (explicit)  
python src/main.py \  
 --input data/inputs/sample/survival\_inputs\_sample2000.csv \  
 --run-type sample  
  
# Production run with pickle  
python src/main.py \  
 --input data/inputs/production/survival\_inputs\_complete.pkl \  
 --run-type production  
  
# Prediction only (skip training)  
python src/main.py \  
 --input data/inputs/sample/data.csv \  
 --run-type sample \  
 --predict-only  
  
# Training only (skip prediction)  
python src/main.py \  
 --input data/inputs/production/data.pkl \  
 --run-type production \  
 --train-only

**Programmatic API**:

from main import run\_pipeline  
  
# Sample run  
run\_pipeline(  
 input\_file="data/inputs/sample/survival\_inputs\_sample2000.csv",  
 run\_type="sample"  
)  
  
# Production run  
run\_pipeline(  
 input\_file="data/inputs/production/survival\_inputs\_complete.pkl",  
 run\_type="production",  
 predict\_only=False,  
 train\_only=False  
)

### Data Schema Requirements

All input files (CSV or pickle) must contain:

**Required Columns**:

* `account\_entities\_key` (str/int): Unique customer identifier
* `survival\_months` (float): Time to event or censoring
* `is\_terminated` (bool/int): Event indicator (1 = terminated, 0 = censored)

**Numeric Features** (9):

* `debit\_exp\_smooth`: Exponentially smoothed debit amounts
* `credit\_exp\_smooth`: Exponentially smoothed credit amounts
* `balance\_exp\_smooth`: Exponentially smoothed account balance
* `past\_due\_balance\_exp\_smooth`: Exponentially smoothed past due balance
* `oldest\_past\_due\_exp\_smooth`: Exponentially smoothed oldest past due days
* `waobd\_exp\_smooth`: Exponentially smoothed weighted average outstanding balance days
* `total\_settlements`: Total number of settlement agreements
* `active\_settlements`: Number of active settlements
* `defaulted\_settlements`: Number of defaulted settlements

**Categorical Features** (2):

* `typeoftariff\_coarse`: Coarse tariff type category
* `risk\_level\_coarse`: Coarse risk level category

### Prediction Output Schema

Generated predictions CSV contains:

| Column | Type | Description |

| `account\_entities\_key` | str/int | Customer identifier |

| `model\_name` | str | Best model used (e.g., "gbsa", "rsf") |

| `expected\_survival\_months` | float | RMST - expected survival time |

| `survival\_prob\_3m` | float | P(survival > 3 months) |

| `survival\_prob\_6m` | float | P(survival > 6 months) |

| `survival\_prob\_12m` | float | P(survival > 12 months) |

| `survival\_prob\_18m` | float | P(survival > 18 months) |

| `survival\_prob\_24m` | float | P(survival > 24 months) |

| `survival\_prob\_36m` | float | P(survival > 36 months) |

**Interpretation**:

* Higher survival probability = lower churn risk
* Expected survival months = area under survival curve (RMST)
* All probabilities in [0, 1]

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## Changelog

### 2025-10-24 - I/O Organization Update

* Added comprehensive Input/Output Organization section
* Documented run\_type system (sample vs production)
* Described directory structure with separate outputs for each run type
* Explained file format support (CSV and pickle with auto-detection)
* Documented file naming conventions with run\_type prefix
* Provided CLI and programmatic API usage examples
* Detailed data schema requirements for input and output

### 2025-10-23 - Initial Version

* Documented survival analysis theory and fundamentals
* Described all five model implementations (Cox PH, Coxnet, Weibull AFT, GBSA, RSF)
* Detailed preprocessing pipeline with L2 regularization and variance filtering
* Explained evaluation metrics (C-index, IBS, time-dependent AUC)
* Documented event-balanced cross-validation strategy
* Added prediction methodology including RMST calculation
* Outlined implementation architecture and design principles

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**Maintenance Note**: This document should be updated whenever:

* New models are added to the framework
* Preprocessing steps are modified
* Evaluation metrics are changed
* Prediction outputs are altered
* Theoretical assumptions are revised