### Asset selection with Local Search

#### Enrico Schumann

December 8, 2011

#### **Abstract**

A brief tutorial on using Local Search for the selection of assets.

#### 1 Introduction

We provide a code example for a simple asset selection problem. The purpose of this vignette is to provide the code in a convenient way; for more details, please see Gilli et~al. [2011]. We start by attaching the package.

```
> require("NMOF")
> set.seed(112233)
```

# 2 The problem

We wish to select between  $K_{inf}$  and  $K_{sup}$  out of  $n_A$  assets such that an equally-weighted portfolio of these assets has the lowest-possible variance. The formal model is:

$$\min_{w} w' \Sigma w \tag{1}$$

subject to the constraints

$$w_j = 1/K$$
 for  $j \in J$ ,  
 $K_{\text{inf}} \le K \le K_{\text{sup}}$ .

Thw weights are stored in the vector w; the symbol J stands for the set of assets in the portfolio; and  $K = \#\{J\}$  is the cardinality of this set, ie, the number of assets in the portfolio.

# 3 Setting up the algorithm

We start by attaching the package and creating random data. We simulate 500 assets: each gets a random volatility between 20% and 40%, and all pairwise correlations are set to 0.6.

... or even simpler:

The neighbourhood function.

```
> neighbour <- function(xc, data) {
+      xn <- xc
+      p <- sample.int(data$na, data$nn, replace = FALSE)
+      xn[p] <- abs(xn[p] - 1L)
+      ## reject infeasible solution
+      if((sum(xn) > data$Ksup) || (sum(xn) < data$Kinf))
+      xc else xn
+ }</pre>
```

We collect all necessary information in the list data: the variance—corvariance matrix Sigma, the cardinality limits Kinf and Ksup, the total number of assets na (ie, the cardinality of the asset universe), and the parameter nn. This parameter controls the neighbourhood: it gives the number of assets that are to be changed when a new solution is computed.

# 4 Solving the model

[1,] 0.1629979

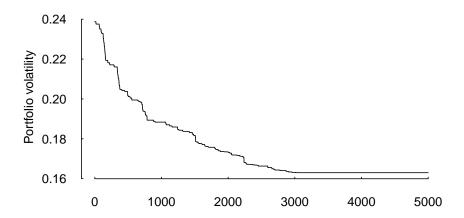
As an initial solution we use a random portfolio.

```
> card0 <- sample(data$Kinf:data$Ksup, 1L, replace = FALSE)
> assets <- sample.int(na, card0, replace = FALSE)
> x0 <- numeric(na)
> x0[assets] <- 1L</pre>
```

With this implementation we need assume that data\$Ksup > data\$Kinf. (If data\$Ksup == data\$Kinf, then sample returns a draw 1:data\$Kinf.)

We collect all settings in the list algo.

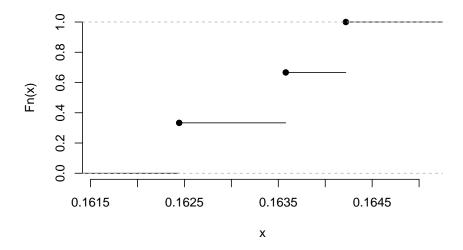
```
> par(ylog = TRUE, bty = "n", las = 1, tck = 0.01)
> plot(sqrt(sol1$Fmat[,2L]),
+ type = "l", xlab = "", ylab = "Portfolio volatility")
```



(Recall that the simulated data had volatilities between 20 and 40%.) We can also run the search repeatedly with the same starting value.

```
> trials <- 3L
> allRes <- restartOpt(LSopt, n = trials, OF, algo = algo, data = data)
> allResOF <- numeric(trials)
> for (i in seq_len(trials))
+         allResOF[i] <- sqrt(allRes[[i]]$OFvalue)
> par(bty = "n")
> plot(ecdf(allResOF), main = "Portfolio volatility")
```

#### Portfolio volatility



(We run LSopt only three times, to keep the build time for the vignette acceptable. To get more meaningful results, we should run more trials.)

# References

Manfred Gilli, Dietmar Maringer, and Enrico Schumann. *Numerical Methods and Optimization in Finance*. Elsevier, 2011.