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Automata

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### Homework #6

Create a regular expression that defines the language over  $\{0,1\}^*$  in which all strings contain at most one occurrence of the substring **00**

-  $1^*(01|1)^*00(10|1)^*1^*$

Create regular grammars that generate these languages using the alphabet  $\{0,1\}$ :

- the same language as the regex  **$(001^*01)^*$** 
  - $S \rightarrow 00B \mid \varepsilon$
  - $B \rightarrow 1B \mid 01S$
- all strings that contain at most one occurrence of the substring **00**
  - $S \rightarrow 1S \mid 01S \mid 00A \mid \varepsilon$
  - $A \rightarrow 10A \mid 1A \mid \varepsilon$
- all strings that contain neither substring **00** nor substring **11**
  - $S \rightarrow 0A \mid \varepsilon$
  - $A \rightarrow 1S \mid \varepsilon$
- all strings that contain both substring **00** and substring **11**
  - $S \rightarrow 0S \mid 1S \mid 00A \mid 11B$
  - $A \rightarrow 0A \mid 1A \mid 11C$
  - $B \rightarrow 0B \mid 1B \mid 00C$
  - $C \rightarrow 0C \mid 1C \mid \varepsilon$