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Automata

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Homework 8

1. $L1 = \{ 0^a 1^b 0^c \mid a+b > c \}$

a. Let's suppose $L1$ is accepted by some FA. choosing some string $x = 0^a 1^b 0^c$ such that $x \in L1$. Then, by pumping lemma, $x = uvw$ such that, $|uv| \leq n$, $|v| > 0$ and $\forall i \geq 0, uv^i w \in L1$. So all the symbols in u and v are 0's. So we know that $v = 0^k$ for some $k > 0$. By the pumping lemma, $uvvw \in L1$ as well. This would make a string y with $0^{a+k} 1^b 0^c$. Since this string $y \in L1$, because $a+b+k > c$ is still true, we can be confident that $L1$ is a regular language.

2. $L2 = \{ 0^a 1^b 0^c \mid a+b+c > 3 \}$

a. Let's suppose $L2$ is accepted by some FA. choosing some string $x = 0^a 1^b 0^c$ such that $x \in L2$. Then, by pumping lemma, $x = uvw$ such that, $|uv| \leq n$, $|v| > 0$ and $\forall i \geq 0, uv^i w \in L2$. So all the symbols in u and v are 0's. So we know that $v = 0^k$ for some $k > 0$. By the pumping lemma, $uvvw \in L2$ as well. This would make a string y with $0^{a+k} 1^b 0^c$. Since this string $y \in L2$, because if $a+b+c > 3$ is true, then $a+b+k+c > 3$, we can be confident that $L2$ is a regular language.

3. $L3 = \{ ww^R \mid w \in \{0,1\}^* \}$

a. Let's suppose $L3$ is accepted by some FA. choosing some string $x = ww^R$ such that $x \in L3$. Then, by pumping lemma, $x = uvw$ such that, $|uv| \leq n$, $|v| > 0$ and $\forall i \geq 0, uv^i w \in L3$. So $u = w$ and v is some non-zero amount of ws . So we know that $v = w^k$ for some $k > 0$. By the pumping lemma, $uvvw \in L3$ as well. This would make a string y with ww^{2k} . Since this string $y \in L3$, because $ww^R \mid w \in \{0,1\}^*$, where $r = 2k$ is true. We can be confident that $L3$ is a regular language.

4. $L_4 = \{ w \mid w \in X, wR \in Y \}$, given any two regular languages X and Y (that share an alphabet)
- Since R is not actually used in the string which is being defined in the string, it should hold no relevance in the definition of L_4 . Thus a more concise statement of it is $L_4 = \{ w \mid w \in X \}$ and we can assume this is a regular language given that X is already defined as a regular language.