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Automata Theory

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### Homework # 16

(1) Create an unrestricted grammar to describe the language  $L = \{ 0^a 1^b 2^{ab} \mid a, b \geq 1 \}$

For strings in this language, the number of 2's is equal to the product of the number of 0's and the number of 1's.

UG

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S A B C X L T J

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0 1 2

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S

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S,AS

S,X

X,BX

X,T

AB,BAC

CA,AC

CB,BC

CT,T2

BT,BL

BL,L1

AL,AJ

AJ,J0

J,e

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This unrestricted grammar produces all strings in form  $\{ 0a1b2ab \mid a,b \geq 1 \}$

(2) Create an unrestricted grammar to describe the language  $L = \{ w \in \{1\}^* \mid |w| = 2k, k \geq 0 \}$

UG

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S A

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1

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S

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S,A

A,11A

A,e

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This unrestricted grammar produces all strings in form{  $w \in \{1\}^* \mid |w| = 2k, k \geq 0$  }