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Automata  
3/17/20

### Homework 13

Use the pumping lemma to prove that these languages are **not** context-free.

- $L_1 = \{ 0^i 1^j 2^k \mid i < j < k \}$ 
  - Given that pumping lemma are required to at most pump 2 strings in parallel, and this grammar by nature of its relationship between all 3 counts of 0, 1, and 2, would require there to be NO pumping lemma which will succeed for this grammar, Hence, this is not a Context-free language.
- $L_2$  is the set of all strings in  $\{0,1,2\}^*$  where the number of 0's is equal to the *higher of* the number of 1's or 2's [so in string  $w$ ,  $\#0(w) = \max(\#1(w), \#2(w))$  ]
  - Again, this language would require keeping track of 0s as well as 1's and 2's in order to figure out which one has a higher number. This is not allowed.

Convert this grammar to Chomsky normal form.

$S \rightarrow AAA \mid B$

$A \rightarrow 1A \mid B$

$B \rightarrow \epsilon$

-  $S \rightarrow AB$

-  $A \rightarrow XA$

-  $B \rightarrow AA$

-  $X \rightarrow 1$