

### Advanced Encryption Standard (AES)

- Also know as Rijndael (Rain-Dal)
  - Rijndael is the name of the algorithm adopted by NIST in 2001 as the Advanced Encryption Standard
- Rijndael was designed by two Belgian Cryptographers – Vincent Rijmen and Joan Daemen
- AES is a family of three algorithms each having a block size of 128-bits and differing in key size i.e. AES-128, AES-192 and AES-256
  - For AES-n, n is the key size

2

## Advanced Encryption Standard (AES)

- AES is a
  - Symmetric
  - Block cipher
  - Product cipher number of rounds differs based on the key size
- Each round of AES has four transformations
  - SubBytes
  - ShiftRows
  - MixColumns
  - AddRoundKey
- AES operates in finite field of GF(28)
  - Uses  $x^8 + x^4 + x^3 + x + 1$  as its prime polynomial

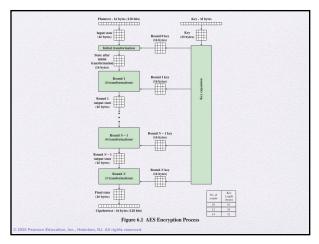
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### Finite Field Arithmetic

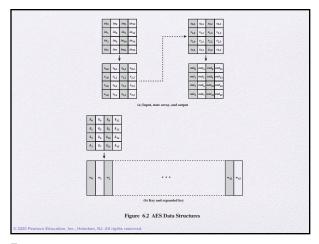
- In the Advanced Encryption Standard (AES) all operations are performed on 8-bit bytes
- The arithmetic operations of addition, multiplication, and division are performed over the finite field GF(2<sup>8</sup>)
- A field is a set in which we can do addition, subtraction, multiplication, and division without leaving the set
- Division is defined with the following rule:
- $a/b = a(b^{-1})$
- \* An example of a finite field (one with a finite number of elements) is the set  $\mathbb{Z}_p$  consisting of all the integers  $\{0,1,\ldots,p-1\}$ , where p is a prime number and in which arithmetic is carried out modulo p

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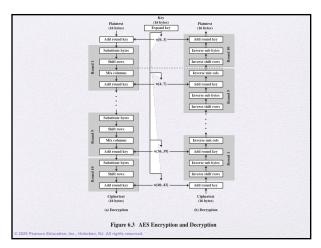
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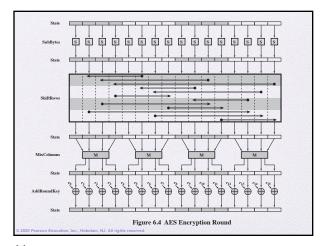
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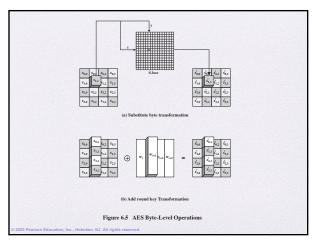


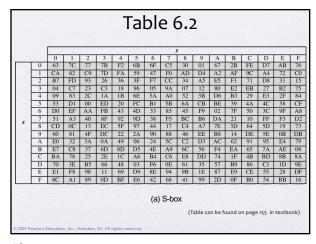
	AES - 128	AES - 192	AES - 256
Key Size (words/bytes/bits)	4/16/128	6/24/192	8/32/256
Plaintext Block Size (words/bytes/bits	4/16/128	4/16/128	4/16/128
Number of Rounds	10	12	14
Round Key Size (words/bytes/bits)	4/16/128	4/16/128	4/16/128
Expanded Key Size (words/bytes)	44/176	52/208	60/240



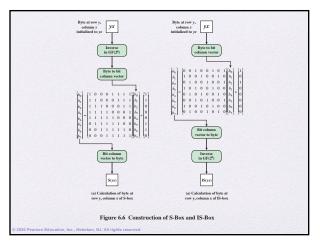
# Processes the entire data block as a single matrix during each round using substitutions and permutation The key that is provided as input is expanded into an array of forty-four 32-bit words, w[i] Four different stages are used: Substitute bytes – uses an S-box to perform a byte-by-byte substitution of the block ShiftRows – a simple permutation MicColumns – a bustitution that makes use of arithmetic over CF(28) AddRoundkey – a simple bitwise XOR of the current block with a portion of the expanded key The cipher begins and ends with an AddRoundKey stage Can view the cipher as alternating operations of XOR encryption (AddRoundKey) of a block, followed by srambling of the block (the other three stages), followed by XOR encryption, and so on Each stage is easily reversible The decryption algorithm makes use of the expanded key in reverse order, however the decryption algorithm is not identical to the encryption algorithm State is the same for both encryption and decryption consists of only three stages







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			y														
	0	52	09	2 6A	3 D5	30	36	6 A5	7	8 BF	9	A A3	9E	C 81	D F3	E D7	F
	0	7C	E3	39	82	9B	2F	FF	87	34	8E	A3	9E 44	C4	DE	E9	СВ
	2	54	7B	94	32	9B A6	C2	23	3D	EE	4C	95	0B	42	FA	C3	4E
433	3	08	2E	Al	66	28	D9	24	B2	76	5B	A2	49	6D	8B	DI	25
7	4	72	F8	F6	64	86	68	98	16	D4	A4	5C	CC	5D	65	B6	92
	5	6C	70	48	50	FD	ED	B9	DA	5E	15	46	57	A7	8D	9D	84
390	6	90	D8	AB	00	8C	BC	D3	0A	F7	E4	58	05	B8	B3	45	06
1/2	7	D0	2C	1E	8F	CA	3F	0F	02	CI	AF	BD	03	01	13	8A	6B
x	8	3A	91	11	41	4F	67	DC	EA	97	F2	CF	CE	FO	B4	E6	73
	9	96	AC	74	22	E7	AD	35	85	E2	F9	37	E8	1C	75	DF	6E
	A	47	F1	1A	71	1D	29	C5	89	6F	В7	62	0E	AA	18	BE	1B
	В	FC	56	3E	4B	C6	D2	79	20	9A	DB	C0	FE	78	CD	5A	F4
	С	1F	DD	A8	33	88	07	C7	31	B1	12	10	59	27	80	EC	5F
	D	60	51	7F	A9	19	B5	4A	0D	2D	E5	7A	9F	93	C9	9C	EF
	Е	A0	E0	3B	4D	AE	2A	F5	B0	C8	EB	BB	3C	83	53	99	61
2	F	17	2B	04	7E	BA	77	D6	26	El	69	14	63	55	21	0C	7D
								(b) In	verse	e S-b	ox						
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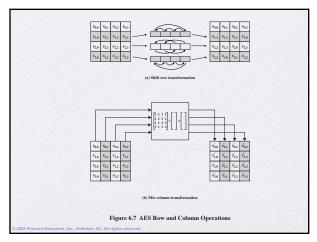


15

### S-Box Rationale

- The S-box is designed to be resistant to known cryptanalytic attacks
- The Rijndael developers sought a design that has a low correlation between input bits and output bits and the property that the output is not a linear mathematical function of the input
- The nonlinearity is due to the use of the multiplicative inverse

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### Shift Row Rationale

- More substantial than it may first appear
- The State, as well as the cipher input and output, is treated as an array of four 4-byte columns
- On encryption, the first 4 bytes of the plaintext are copied to the first column of State, and so on
- The round key is applied to State column by column
  - Thus, a row shift moves an individual byte from one column to another, which is a linear distance of a multiple of 4 bytes
- Transformation ensures that the 4 bytes of one column are spread out to four different columns

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18

### Mix Columns Rationale

- Coefficients of a matrix based on a linear code with maximal distance between code words ensures a good mixing among the bytes of each column
- The mix column transformation combined with the shift row transformation ensures that after a few rounds all output bits depend on all input bits

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### AddRoundKey Transformation

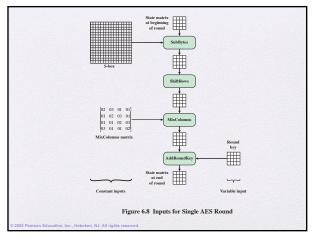
- The 128 bits of State are bitwise XORed with the 128 bits of the round key
- Operation is viewed as a columnwise operation between the 4 bytes of a State column and one word of the round key
  - Can also be viewed as a byte-level operation

# Rationale: Is as simple as possible and affects every bit of State

The complexity of the round key expansion plus the complexity of the other stages of AES ensure security

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20



21

### **AES Key Expansion**

- Takes as input a four-word (16 byte) key and produces a linear array of 44 words (176) bytes
  - This is sufficient to provide a four-word round key for the initial AddRoundKey stage and each of the 10 rounds of the cipher
- Key is copied into the first four words of the expanded key
  - The remainder of the expanded key is filled in four words at a time
- Each added word w[i] depends on the immediately preceding word, w[i 1], and the word four positions back, w[i 4]
  - In three out of four cases a simple XOR is used
  - For a word whose position in the warray is a multiple of 4, a more complex function is used

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### **AES Key Expansion**

• The key expansion algorithm is as follows:

If  $i \mod 4 = 0$  then

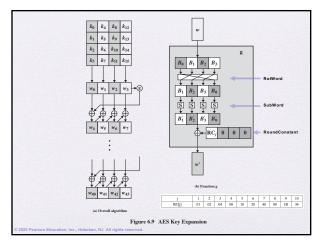
 $w[i] = g(w[i-1]) \oplus w[i-4]$ 

else  $w[i] = w[i-1] \oplus w[i-4]$ 

- The **g** function consists of three rounds of transformation
  - RotWord Circular byte shiftSubWord S-Box substitution

  - RoundConstant –Bitwise XOR with the round

23



24

AES Key Expanded Key Calculation									
	#Rounds*	Words per Round	Size of Expanded Key Array (Words)	Size of Initial Key (Words)	Expanded Key Values Derived from Initial Key	Expanded Key Values Calculated			
AES-128	10 + 1	4	44	4	w[o-3]	w[4-43]			
AES-192	12 + 1	4	52	6	w[o-5]	w[6-51]			
AES-256	14 + 1	4	60	8	w[0-7]	w[8-59]			
* The extra added round is for the initial transformation									

### Key Expansion Rationale

- The Rijndael developers designed the expansion key algorithm to be resistant to known cryptanalytic attacks
- Inclusion of a rounddependent round constant eliminates the symmetry between the ways in which round keys are generated in different

- Knowledge of a part of the cipher key or round key does not enable calculation of many other round-key bits
- An invertible transformation
- Speed on a wide range of processors

- Usage of round constants to eliminate symmetries
   Diffusion of cipher key differences into the round keys
   Enough nonlinearity to prohibit the full determination of round key differences for the property of the from cipher key differences only
  • Simplicity of description

26

Table 6.3	Example Round	Key	Calculation

Description	Value
i (decimal)	36
temp = w[i - 1]	7F8D292F
RotWord (temp)	8D292F7F
SubWord (RotWord (temp))	5DA515D2
Rcon (9)	1B000000
SubWord (RotWord (temp)) ⊕ Rcon (9)	46A515D2
w[i - 4]	EAD27321
$w[i] = w[i - 4] \oplus SubWord (RotWord (temp)) \oplus Rcon (9)$	AC7766F3

27

Table	6.4

Key Expansion

AES Example

w7 = w6 ⊕ w3 = 38 81 15 a7	y2 ⊕ Rcon(2)= 0e 59 5c 07 = z2
w8 = w4 ⊕ 22 = d2 c9 6b b7	RotMord(w11)= ff d3 c6 e6 = x3
w9 = w8 ⊕ w5 = 49 80 b4 5e	SubMord(x2)= 16 66 b4 8e = y3
w10 = w9 ⊕ w6 = de 7e c6 61	Rcon(3)= 04 00 00 00
w11 = w10 ⊕ w7 = e6 ff d3 c6	y3 ⊕ Rcon(3)= 12 66 b4 8e = z3
w12 = w8 @ 23 = c0 af df 39	RotMord(W15)= ae 7e c0 51 = x4
w13 = w12 @ w9 = 89 2f 6b 67	SubMord(X3)= e4 f3 ba c8 = y4
w14 = w13 @ w10 = 57 51 ad 06	Rcon(4)= 08 00 00 00
w15 = w14 @ w11 = b1 ae 7e c0	y4 ⊕ Rcon(4)= ec f3 ba c8 = 4
w16 = w12 @ z4 = 2c 5c 65 f1	RotMord(u19)= 8c dd 50 43 = x5
w17 = w16 @ w13 = a5 73 0e 96	SubMord(x4)= 64 c1 53 1a = y5
w18 = w17 @ w14 = f2 22 a3 90	Reon(5)= 10 00 00 00
w19 = w18 @ w15 = 43 8c dd 50	y5 ⊕ Reon(5)= 74 c1 53 1a = z5
w20 = w16 ⊕ z5 = 58 9d 36 eb	RotMord(WZ3)= 40 46 bd 4c = x6
w21 = w20 ⊕ w17 = fd ee 38 7d	SubMord(X5)= 09 5a 7a 29 = y6
w22 = w21 ⊕ w18 = 0f cc 9b ed	Reon(6)= 20 00 00 00
w23 = w22 ⊕ w19 = 4c 40 46 bd	y6 ⊕ Reon(6)= 29 5a 7a 29 = z6
w24 = w20 ⊕ z6 = 71 c7 4c c2	RotMord(w27)= a5 a9 ef cf = x7
w25 = w24 ⊕ w21 = 8c 29 74 bf	SubMord(x6)= 06 d3 df 8a = y7
w26 = w25 ⊕ w22 = 83 e5 ef 52	Rcon(7)= 40 00 00 00
w27 = w26 ⊕ w23 = cf a5 a9 ef	y7 ⊕ Rcon(7)= 46 d3 df 8a = z7
w28 = w24 ⊕ x7 = 37 14 93 48	RotMord(w31) - 7d a1 4a f7 - x8
w29 = w28 ⊕ w25 = bb 3d e7 f7	SubMord(x7) - ff 32 d6 68 - y8
w30 = w29 ⊕ w26 = 38 d8 08 a5	Rcon(8) - 80 00 00 00
w31 = w30 ⊕ w27 = f7 7d a1 4a	y8 ⊕ Rcon(8) - 7f 32 d6 68 - z8
w32 = w28 ⊕ z8 = 48 26 45 20	RotMord(x3)= be 0b 38 3c = x9
w33 = w32 ⊕ w29 = f3 1b a2 d7	SubMord(x8)= ae 2b 07 eb = y9
w34 = w33 ⊕ w30 = cb c3 aa 72	Rcon(9)= 1B 00 00 00
w35 = w34 ⊕ w32 = 3c be 0b 38	y9 ⊕ Rcon(9)= b5 2b 07 eb = z9
w36 = w32 ⊕ x9 = fd 0d 42 cb	Rotword(w39)= 6b 41 56 19 = x10
w37 = w36 ⊕ w33 = 0e 16 e0 1c	SubMord(x9)= 7f 83 b1 99 = y10
w38 = w37 ⊕ w34 = c5 d5 4a 6e	Rcon(10)= 36 00 00 00
w39 = w38 ⊕ w35 = f9 6b 41 56	y10 ⊕ Rcon(10)= 49 83 b1 99 = z10
w40 = w36 ⊕ z10 = b4 8e f3 52 w41 = w40 ⊕ w37 = ba 98 13 4e w42 = w41 ⊕ w38 = 7f 4d 59 20 w43 = w42 ⊕ w39 = 86 26 18 76	

	Table 6.4 AES	Example			
	Start of Round	After SubBytes	After ShiftRows	After MixColumns	Round Key
	01 89 fe 76 23 ab de 54 45 ed ba 32				0f 47 0c af 15 d9 b7 7f 71 e8 ad 67
	67 ef 98 10				c9 59 d6 98
	0e ce f2 d9 36 72 6b 2b	ab 8b 89 35 05 40 7f f1	ab 8b 89 35 40 7f fl 05	b9 94 57 75 e4 8e 16 51	dc 9b 97 38 90 49 fe 81
	36 72 65 25 34 25 17 55	18 3f f0 fc	f0 fc 18 3f	47 20 9a 3f	90 49 fe 81 37 df 72 15
	ae b6 4e 88	e4 4e 2f c4	c4 e4 4e 2f	o5 d6 f5 3b	b0 e9 3f a7
	65 Of c0 4d	4d 76 ba e3	4d 76 ba e3	8e 22 db 12	d2 49 de e6
	74 c7 e8 d0	92 c6 9b 70	c6 9b 70 92	b2 f2 de 92	c9 80 7e ff
T-blac 4	70 ff e8 2a 75 3f ca 9c	51 16 9b e5 9d 75 74 de	9b e5 51 16 de 9d 75 74	df 80 f7 c1 2d c5 le 52	6b b4 c6 d3 b7 5e 61 c6
Table 6.4	5c 6b 05 f4	4a 7f 6b bf	4a 7f 6b bf	b1 c1 0b cc	c0 89 57 b1
Table 0.4	7b 72 a2 6d	21 40 3a 3c	40 3a 3c 21	ba f3 8b 07	af 2f 51 ae
	b4 34 31 12	8d 18 c7 c9	c7 c9 8d 18	f9 1f 6a c3	df 6b ad 7e
	9a 9b 7f 94	b8 14 d2 22	22 b8 14 d2	1d 19 24 5c	39 67 06 c0
	71 48 5c 7d	a3 52 4a ff	a3 52 4a ff	d4 11 fe Of	2c a5 f2 43
	15 dc da a9 26 74 c7 bd	59 86 57 d3 £7 92 c6 7a	86 57 d3 59 c6 7a f7 92	3b 44 06 73 cb ab 62 37	5c 73 22 8c 65 0e a3 dd
	24 7e 22 9c	36 f3 93 de	de 36 f3 93	19 b7 07 ec	f1 96 90 50
	f8 b4 0c 4c	41 8d fe 29	41 8d fe 29	2a 47 c4 48	58 fd 0f 4c
	67 37 24 ff	85 9a 36 16	9a 36 16 85	83 e8 18 ba	9d ee cc 40
	ae a5 c1 ea	e4 06 78 87	78 87 e4 06	84 18 27 23	36 38 9b 46
AFC	e8 21 97 bc 72 ba cb 04	9b fd 88 65 40 f4 1f f2	65 9b fd 88 40 f4 1f f2	eb 10 0a f3 7b 05 42 4a	eb 7d ed bd 71 8c 83 cf
AES	72 ba cb 04 1e 06 d4 fa	72 6f 48 2d	6f 48 2d 72	75 05 42 4a 1e d0 20 40	71 8c 83 cf c7 29 e5 a5
/ \LJ	b2 20 bc 65	37 b7 65 4d	65 4d 37 b7	94 83 18 52	4c 74 ef a9
	00 6d e7 4e	63 3c 94 2f	2f 63 3c 94	94 c4 43 fb	c2 bf 52 ef
	Oa 89 cl 85	67 a7 78 97	67 a7 78 97	ec 1a c0 80	37 bb 38 f7
EVALADIE	d9 f9 c5 e5	35 99 a6 d9	99 a6 d9 35	0c 50 53 c7	14 3d d8 7d
FXAMPLE	d8 f7 f7 fb 56 7b 11 14	61 68 68 Of bl 21 82 fa	68 Of 61 68 fa b1 21 82	3b d7 00 ef b7 22 72 e0	93 e7 08 a1 48 f7 a5 4a
L/V\\IVII LL	db al f8 77	b9 32 41 f5	b9 32 41 f5	b1 1a 44 17	48 f3 cb 3c
	18 6d 8b ba	ad 30 3d f4	3c 3d f4 ad	3d 2f ec b6	26 1b c3 be
	a8 30 08 4e	d2 04 30 2f	30 2f c2 04	Oa 6b 2f 42	45 a2 aa 0b
	ff d5 d7 aa	16 03 0e ac	ac 16 03 0e	9f 68 f3 b1	20 d7 72 38
	f9 e9 8f 2b	99 le 73 fl	99 le 73 fl	31 30 3a c2	fd 0e c5 f9
	1b 34 2f 08 4f c9 85 49	af 18 15 30 84 dd 97 3b	18 15 30 af 97 3b 84 dd	ac 71 8c c4 46 65 48 eb	0d 16 d5 6b
	bf bf 81 89	08 08 0c a7	a7 08 08 0c	46 65 48 eD 6a 1c 31 62	d2 e0 4a 41 cb 1c 6e 56
	cc 3e ff 3b	4b b2 16 e2	4b b2 16 e2		b4 ba 7f 86
	a1 67 59 af	32 85 cb 79	85 cb 79 32		8e 98 4d 26
	04 85 02 aa	f2 97 77 ac	77 ac f2 97		f3 13 59 18
	al 00 5f 34	32 63 of 18	18 32 63 of		52 4e 20 76
	ff 08 69 64 0b 53 34 14				
	84 bf ab 8f				
	4a 7c 43 b9				
		055276334075025		CXC 10 10 25 40 45 11 57 11 50 50 50 50 50 50 50 50 50 50 50 50 50	
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T.I.I. 6 -	Round	anche Effect in AES: Change in Plaintext	Number of Bits that Differ
Table 6.5		0123456789abcdeffedcba9876543210 0023456789abcdeffedcba9876543210	1
	0	0e3634aece7225b6f26b174ed92b5588 0f3634aece7225b6f26b174ed92b5588	1
	1	657470750fc7ff3fc0e8e8ca4dd02a9c c4a9ad090fc7ff3fc0e8e8ca4dd02a9c	20
Avalanche	2	5c7bb49a6b72349b05a2317ff46d1294 fe2ae569f7ee8bb8c1f5a2bb37ef53d5	58
Effect	3	7115262448dc747e5cdac7227da9bd9c ec093dfb7c45343d689017507d485e62	59
LITCCC	4	f867aee8b437a5210c24c1974cffeabc 43efdb697244df808e8d9364ee0ae6f5	61
in AES:	5	721eb200ba06206dcbd4bce704fa654e 7b28a5d5ed643287e006c099bb375302	68
Classical	6	0ad9d85689f9f77bclc5f71185e5fb14 3bc2d8b6798d8ac4fe36a1d891ac181a	64
Change	7	db18a8ffa16d30d5f88b08d777ba4eaa 9fb8b5452023c70280e5c4bb9e555a4b	67
in Plaintext	8	f91b4fbfe934c9bf8f2f85812b084989 20264e1126b219aef7feb3f9b2d6de40	65
IIII Idilitext	9	cca104a13e678500ff59025f3bafaa34 b56a0341b2290ba7dfdfbddcd8578205	61
	10	ff0b844a0853bf7c6934ab4364148fb9 612b89398d0600cde116227ce72433f0	58

	Round		Number of Bits that Differ
Table 6.7		0123456789abcdeffedcba9876543210 0123456789abcdeffedcba9876543210	0
Table 0.7	0	0e3634aece7225b6f26b174ed92b5588 0f3634aece7225b6f26b174ed92b5588	1
	1	657470750fc7ff3fc0e8e8ca4dd02a9c c5a9ad090ec7ff3fc1e8e8ca4cd02a9c	22
Avalanche	2	5c7bb49a6b72349b05a2317ff46d1294 90905fa9563356d15f3760f3b8259985	58
Effect	3	7115262448dc747e5cdac7227da9bd9c 18aeb7aa794b3b66629448d575c7cebf	67
in	4	f867aee8b437a5210c24c1974cffeabc f81015f993c978a876ae017cb49e7eec	63
AES:	5	721eb200ba06206dcbd4bce704fa654e 5955c91b4e769f3cb4a94768e98d5267	81
Change in	6	0ad9d85689f9f77bc1c5f71185e5fb14 dc60a24d137662181e45b8d3726b2920	70
Key	7	db18a8ffa16d30d5f88b08d777ba4eaa fe8343b8f88bef66cab7e977d005a03c	74
	8	f91b4fbfe934c9bf8f2f85812b084989 da7dad581d1725c5b72fa0f9d9d1366a	67
	9	ccal04al3e678500ff59025f3bafaa34 0ccb4c66bbfd912f4b511d72996345e0	59
	10	ff0b844a0853bf7c6934ab4364148fb9 fc8923ee501a7d207ab670686839996b	53

### Implementation Aspects

- AES can be implemented very efficiently on an 8bit processor
- AddRoundKey is a bytewise XOR operation
- ShiftRows is a simple byte-shifting operation
- SubBytes operates at the byte level and only requires a table of 256 bytes
- MixColumns requires matrix multiplication in the field GF(28), which means that all operations are carried out on bytes

32

### **Implementation Aspects**

- Can efficiently implement on a 32-bit processor
  - Redefine steps to use 32-bit words
  - Can precompute 4 tables of 256-words
  - Then each column in each round can be computed using 4 table lookups + 4 XORs
  - At a cost of 4Kb to store tables
- Designers believe this very efficient implementation was a key factor in its selection as the AES cipher

33

### Summary

- Present an overview of the general structure of the Advanced **Encryption Standard** (AES)

- Understand the four transformations used in AES
- Understand the use of polynomials with coefficients in GF(28)

Explain the AES key

expansion algorithm