



# Identification of normal modes in underwater acoustic propagation using convolutional neural networks

Costas Smaragdakis, **Ioannis Maris**, Michael Taroudakis



*University of Crete and Foundation for Research and Technology-Hellas  
Greece*



**FORTH**  
INSTITUTE OF APPLIED & COMPUTATIONAL MATHEMATICS

## Motivation

- Introduce a student into applications of Acoustical Oceanography
- **Background** : Mathematical Modeling, Acoustics, Inverse Problems
- **Problem** : Of practical interest

## Given Problem

- **Concept** Use of modal dispersion as the characteristic feature of an acoustic signal to be exploited for inversions
- **Question** : How we can identify the dispersion characteristics of a measured signal in order for them to be used for inversion purposes

## Objectives

- Suggest a scheme for an automatic identification of the dispersion characteristics (dispersion curves) for a limited number of modes.
- Test the scheme with synthetic data.

# Theory

- Short time Fourier Transform

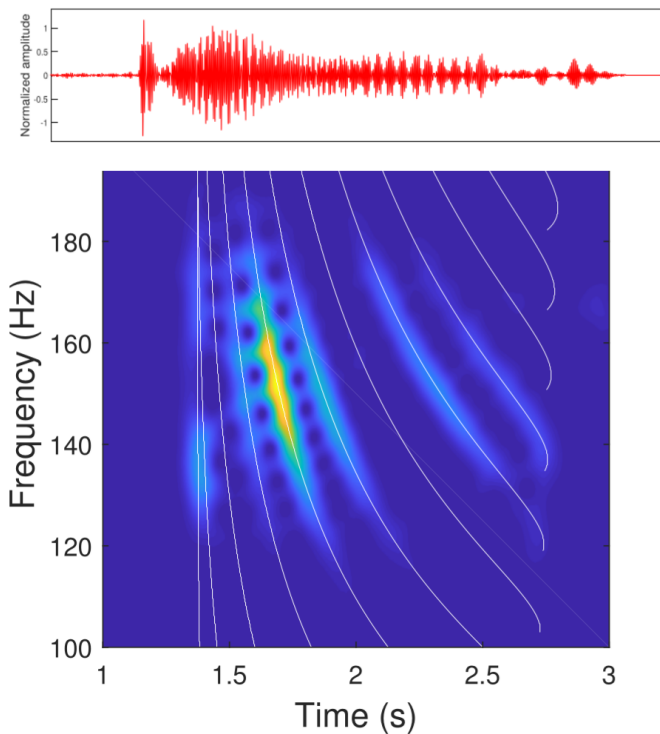
$$\text{STFT}_h(s; \tau, f) = \int_{-\infty}^{\infty} s(t) h(t - \tau) e^{-i2\pi ft} dt$$

- Spectrogram

$$\text{SP}_h(s; \tau, f) = |\text{STFT}_h(\tau, f)|^2$$

- Dispersion curves :

$$t_n(f) = \frac{r}{v_{g,n}(f)}, \quad v_{g,n}(f) = \left. \frac{\partial \omega}{\partial k_n} \right|_{\omega=2\pi f}$$



## Solution

- Use Convolutional Neural Networks for the dispersion identification.
- Model the dispersion curves with an appropriate function.
- Train the CNN with a set of synthetic signals. (Training set)
- Evaluate the model with an independent set of signals. (Testing set)

## Modelling the dispersion curves

- Polynomial of 5<sup>th</sup> order

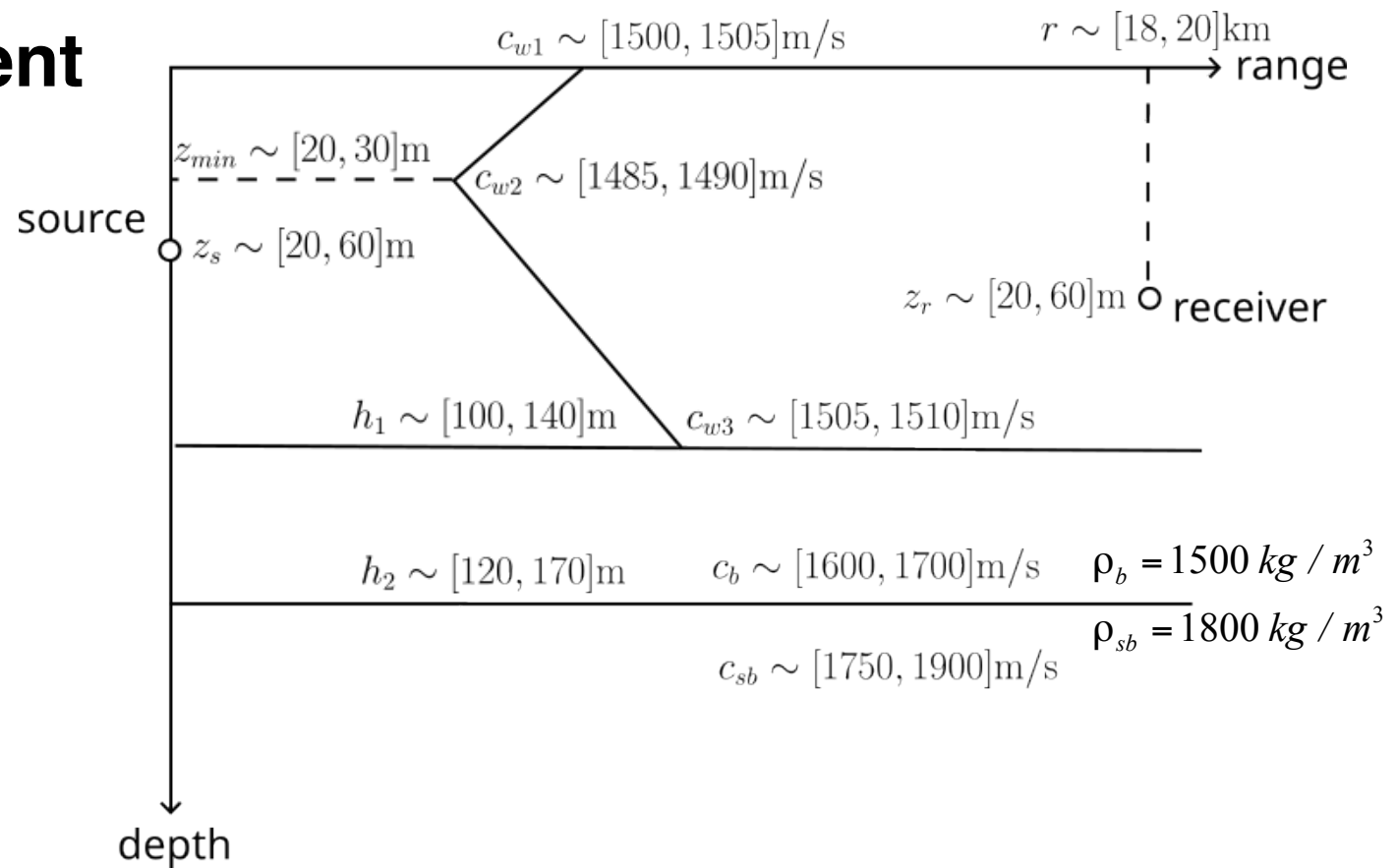
$$\hat{t}_n(f) = a_5^{(n)} f^5 + a_4^{(n)} f^4 + a_3^{(n)} f^3 + a_2^{(n)} f^2 + a_1^{(n)} f + a_0^{(n)}$$

$$\hat{t}_n(f) = a_5^{(n)} f^5 + a_4^{(n)} f^4 + a_3^{(n)} f^3 + a_2^{(n)} f^2 + a_1^{(n)} f + \varepsilon a_0^{(n)}, \quad \varepsilon = 0.1$$

- The Neural Network should estimate the vector of the polynomial parameters for the three first orders of modes.

$$\mathbf{a}^{(n)} = \left( a_0^{(n)}, a_1^{(n)}, a_2^{(n)}, a_3^{(n)}, a_4^{(n)}, a_5^{(n)} \right)$$

# A simple environment

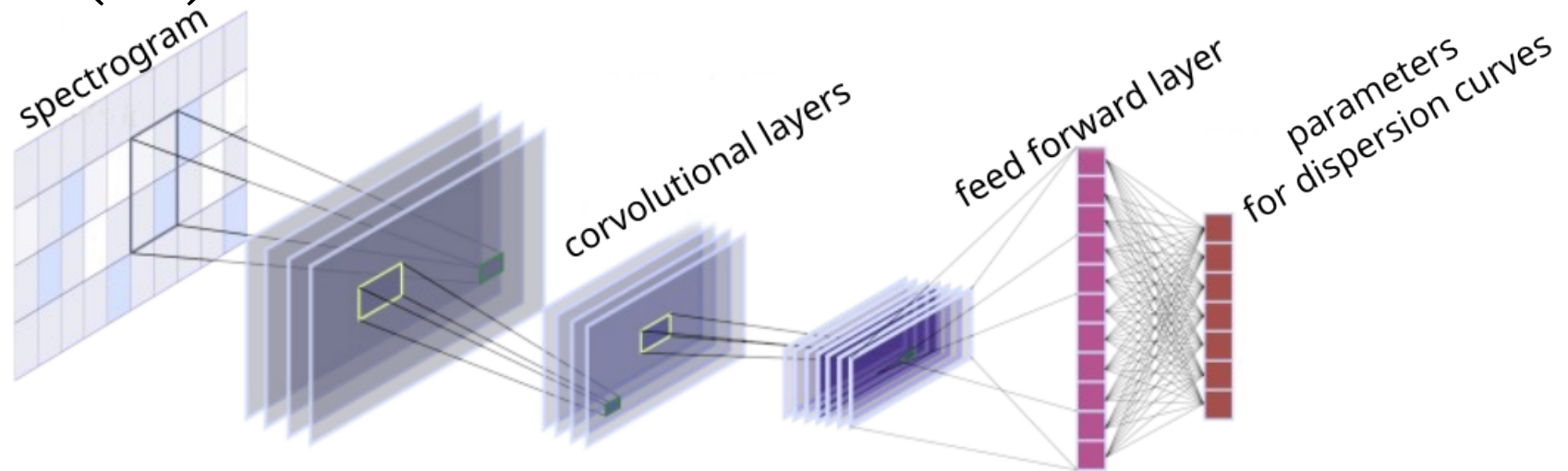




# The convolutional neural network

Input :  $\log(SP + 1)$

Output :  $(a_i^{(n)})$ ,  $i = 1, \dots, 6$   $n = 1, 2, 3$

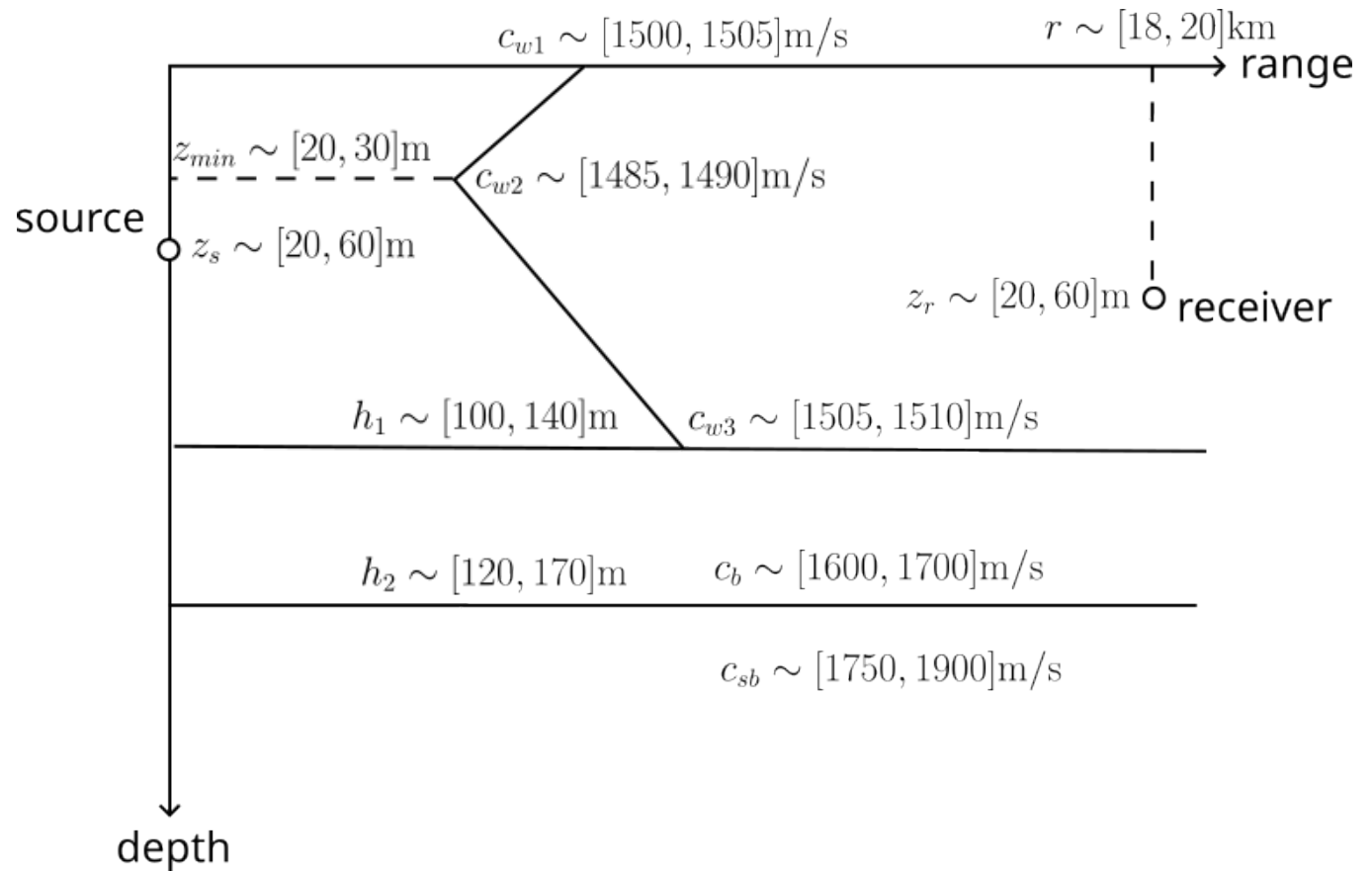


# Implementation

4096 random samples

80% training set

20% testing set

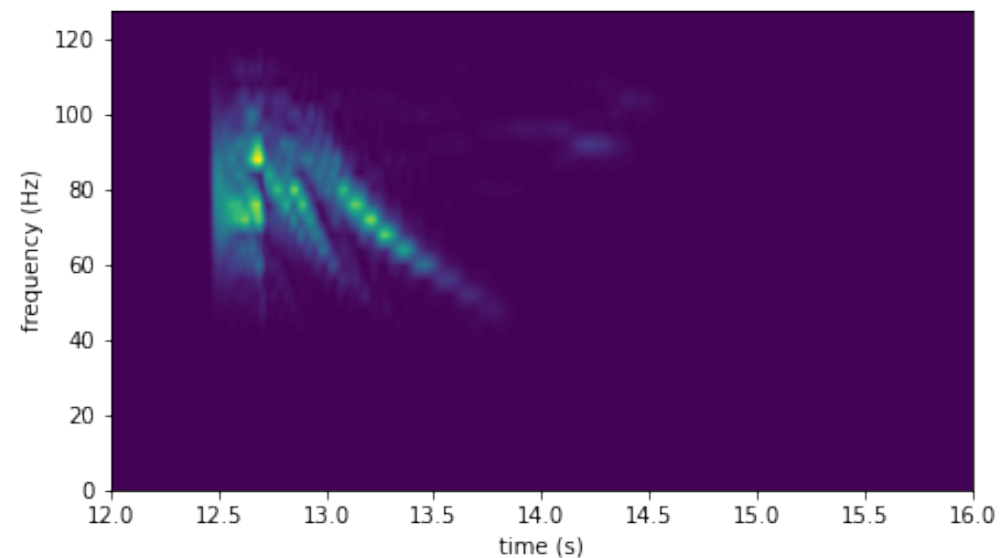
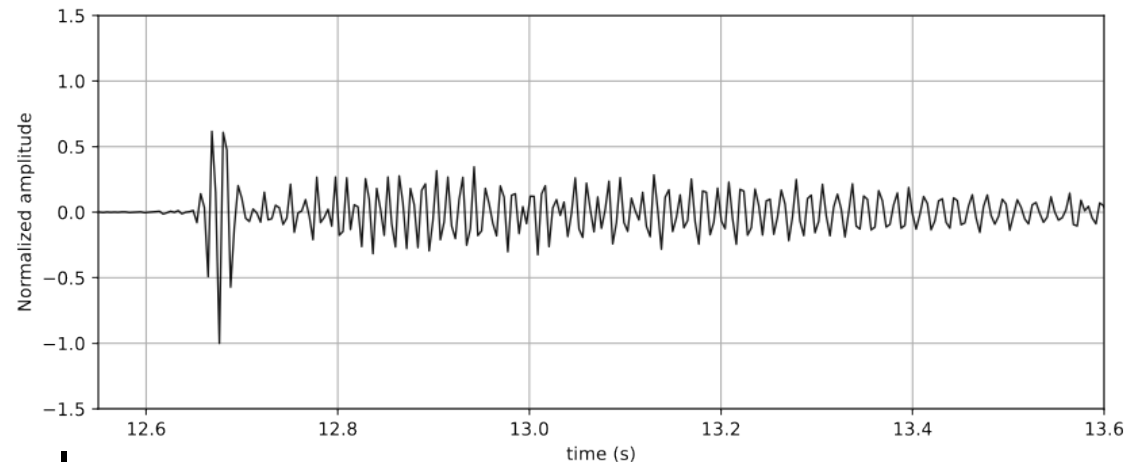


## Implementation

A signal is chosen among the testing set to be used as the reference (measured) signal

No noise is added

Its spectrogram



# Implementation

The spectrogram is given in discrete sets of time and frequency

Determination of the CNN output

$$a_*^{(n)} = \arg \min \sum_i \left( \hat{t}^{(n)}(f_i) - t^{(n)}(f_i) \right)^2$$

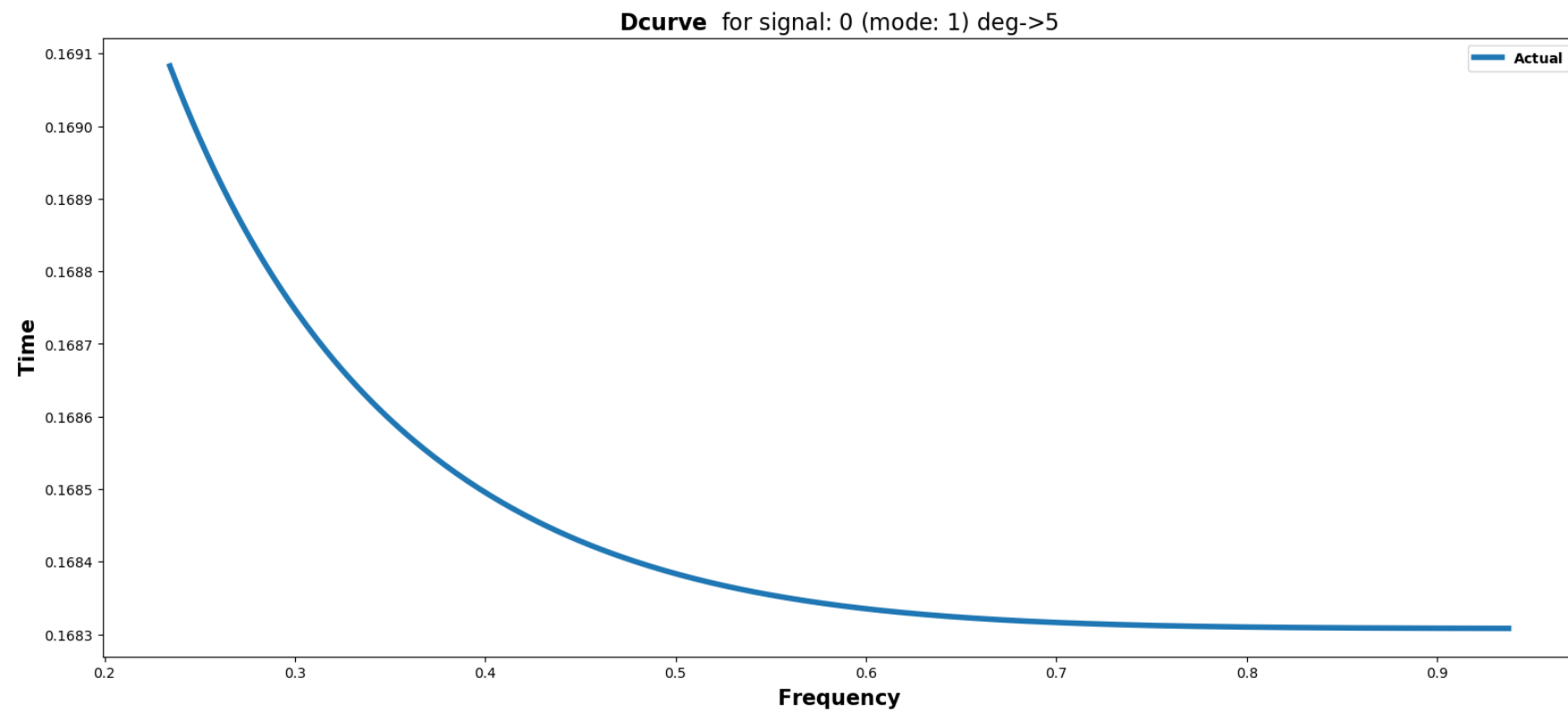
## Results

Mode	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$
1	0.1925,	-0.0279,	0.0731,	-0.1039,	0.0727,	-0.0201
2	0.3702,	-1.1324,	3.1526,	-4.5516,	3.3233,	-0.9606
3	0.3857,	-0.8043,	1.6648,	-1.9313,	1.1617,	-0.2713
1	0.1725,	-0.0277,	0.0753,	-0.1055,	0.0752,	-0.0215
2	0.3739,	-1.3339,	3.7522,	-5.4873,	4.0550,	-1.1950
3	0.4067,	-1.1110,	2.5854,	-3.3142,	2.2223,	-0.6082

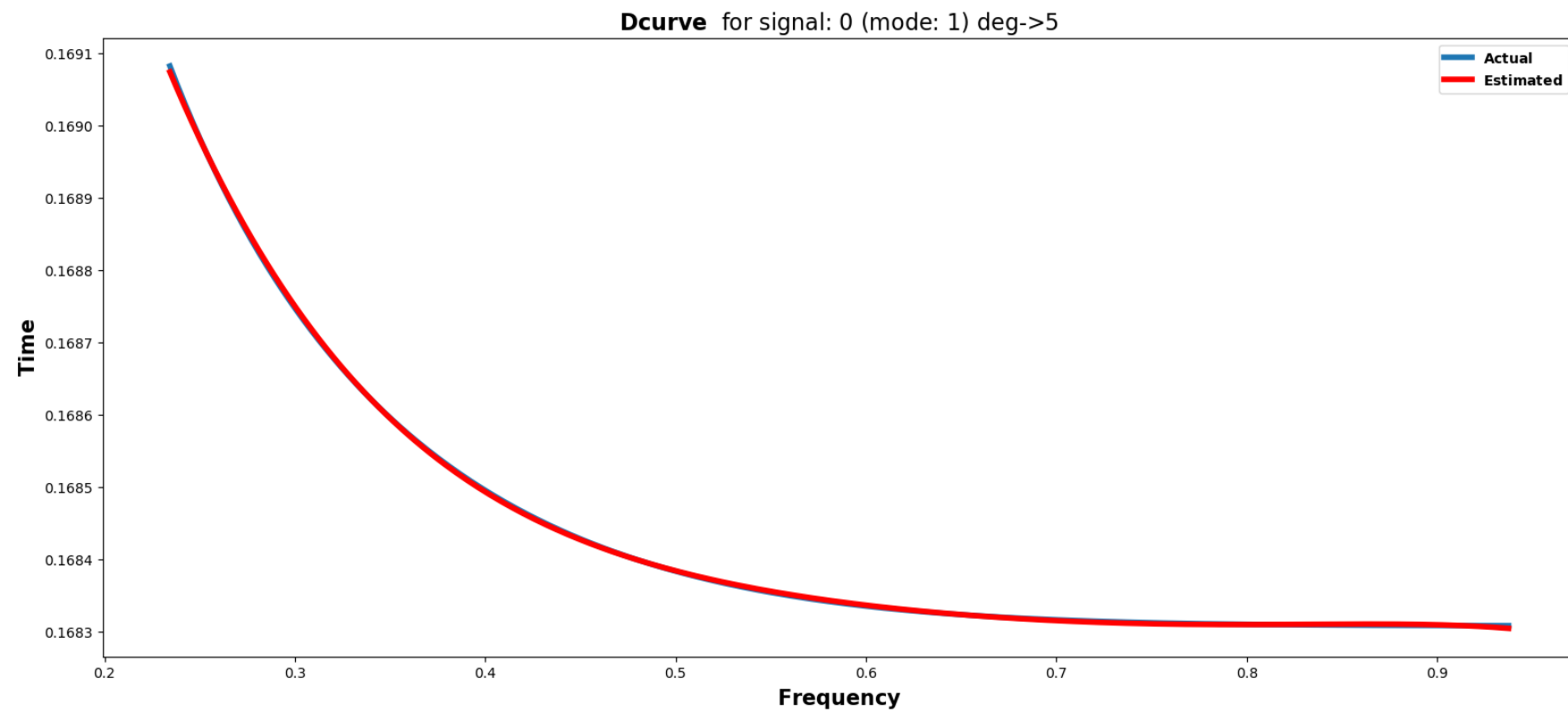
“Measured”

“Estimated”

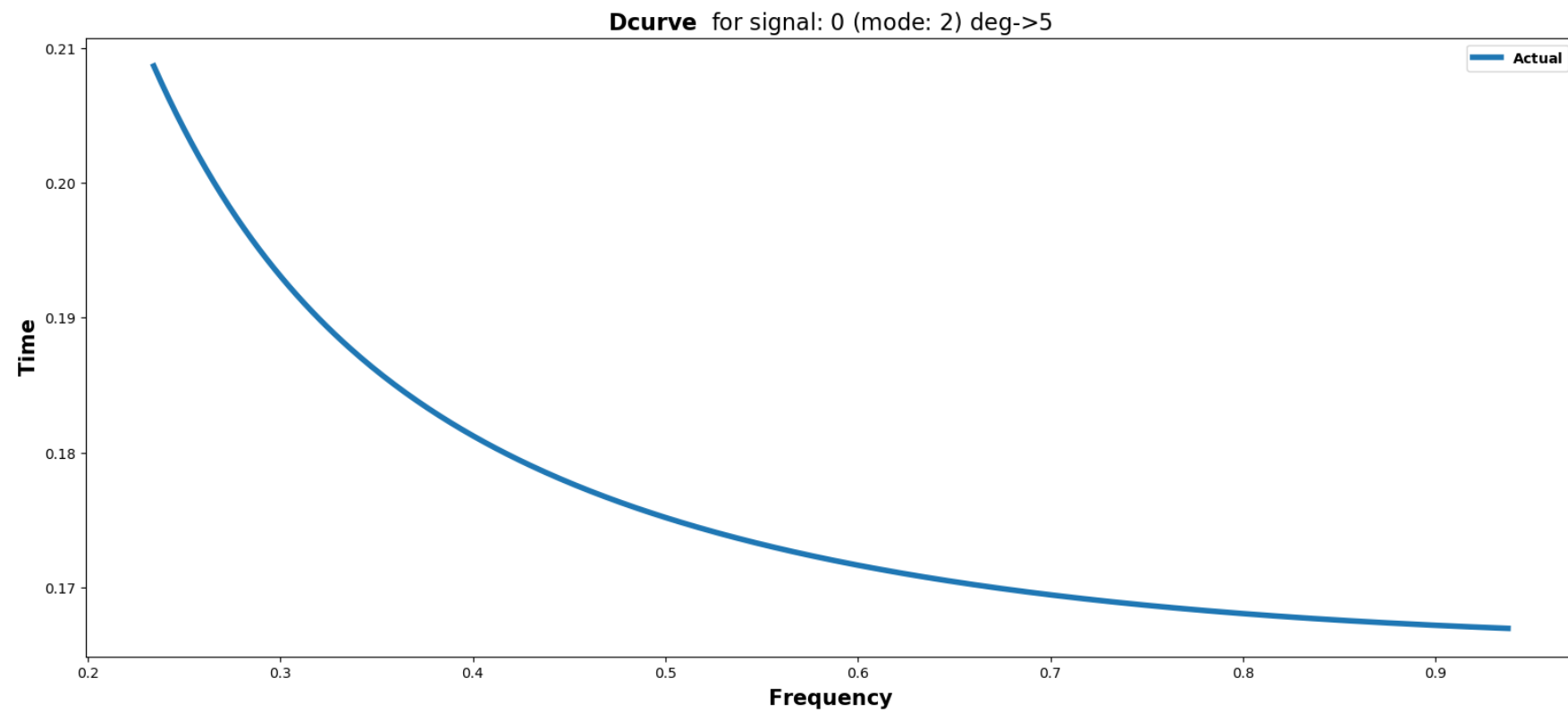
## Mode 1



## Mode 1

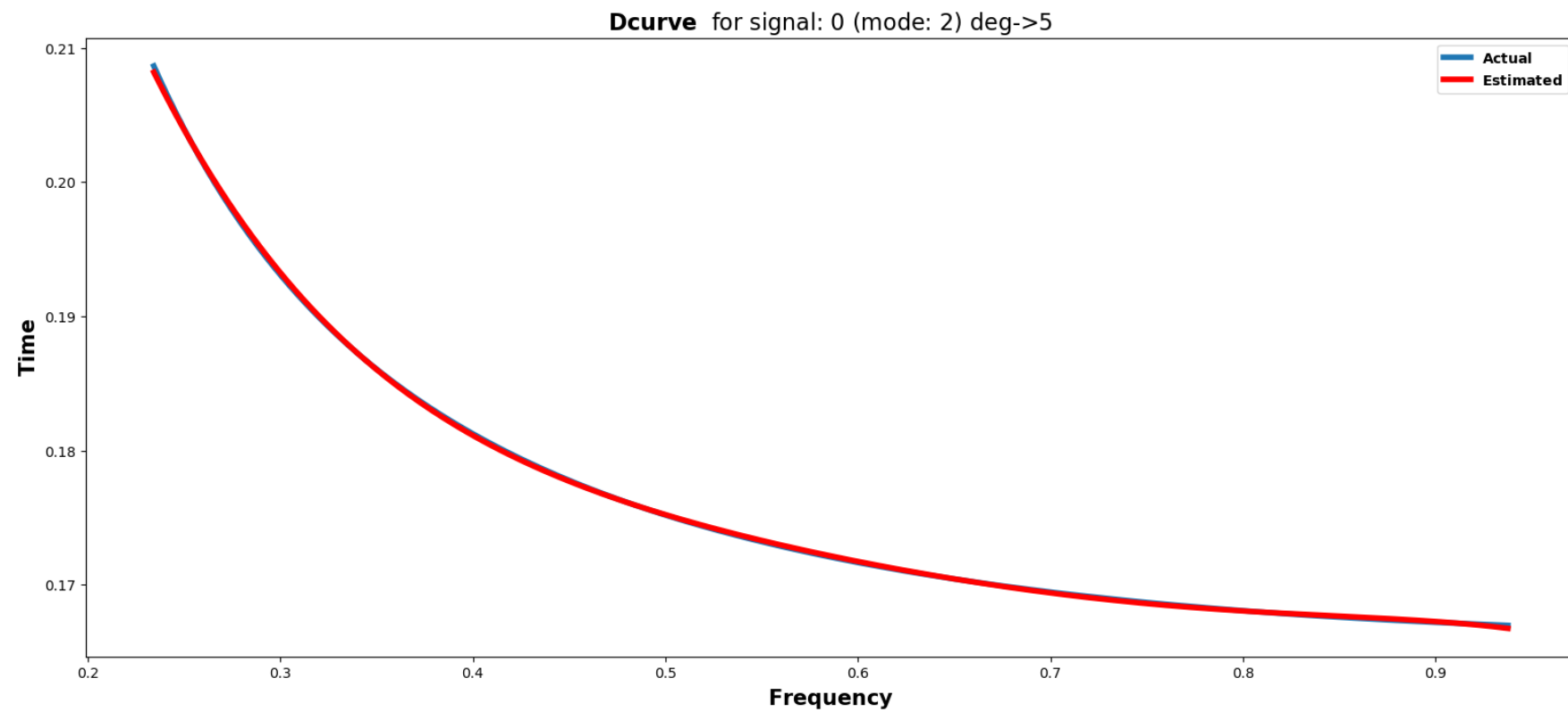


## Mode 2

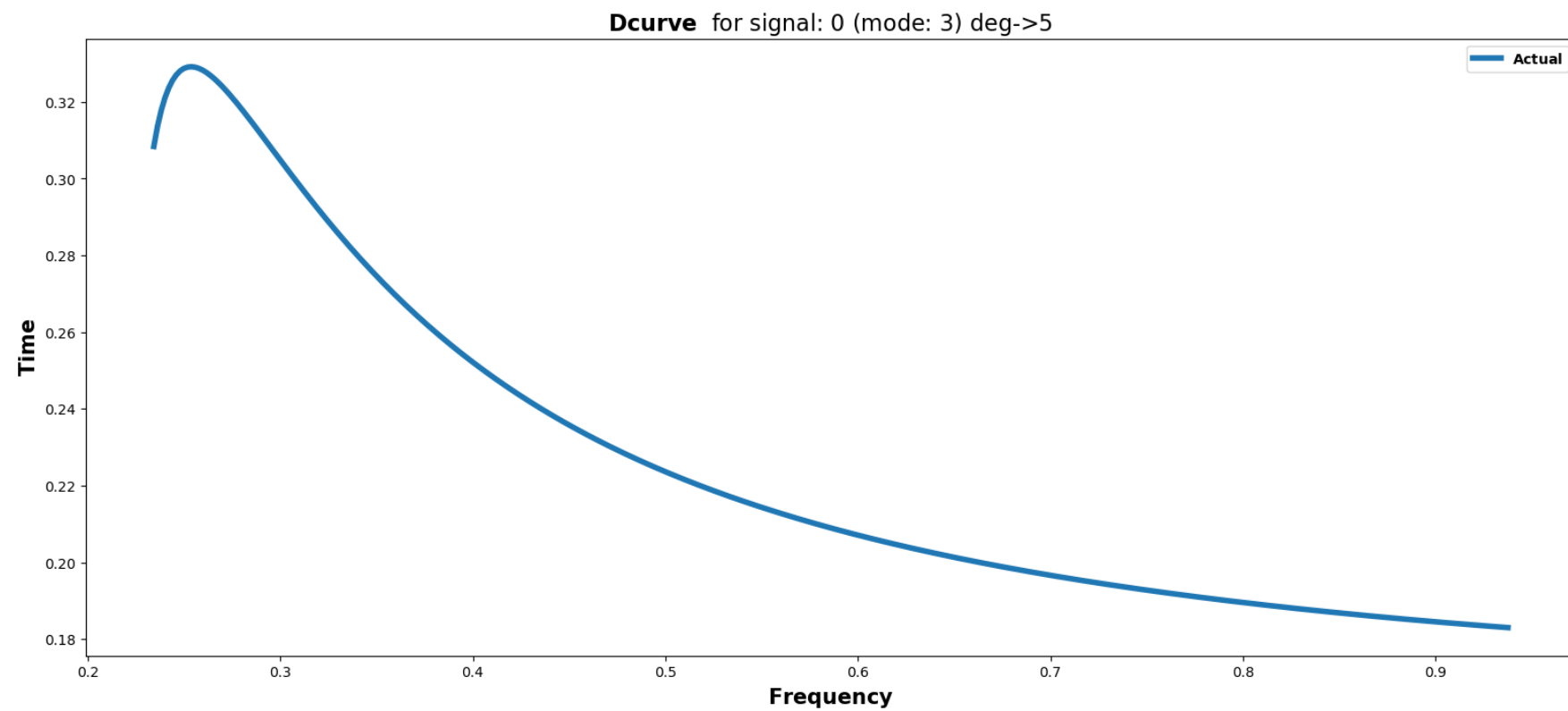




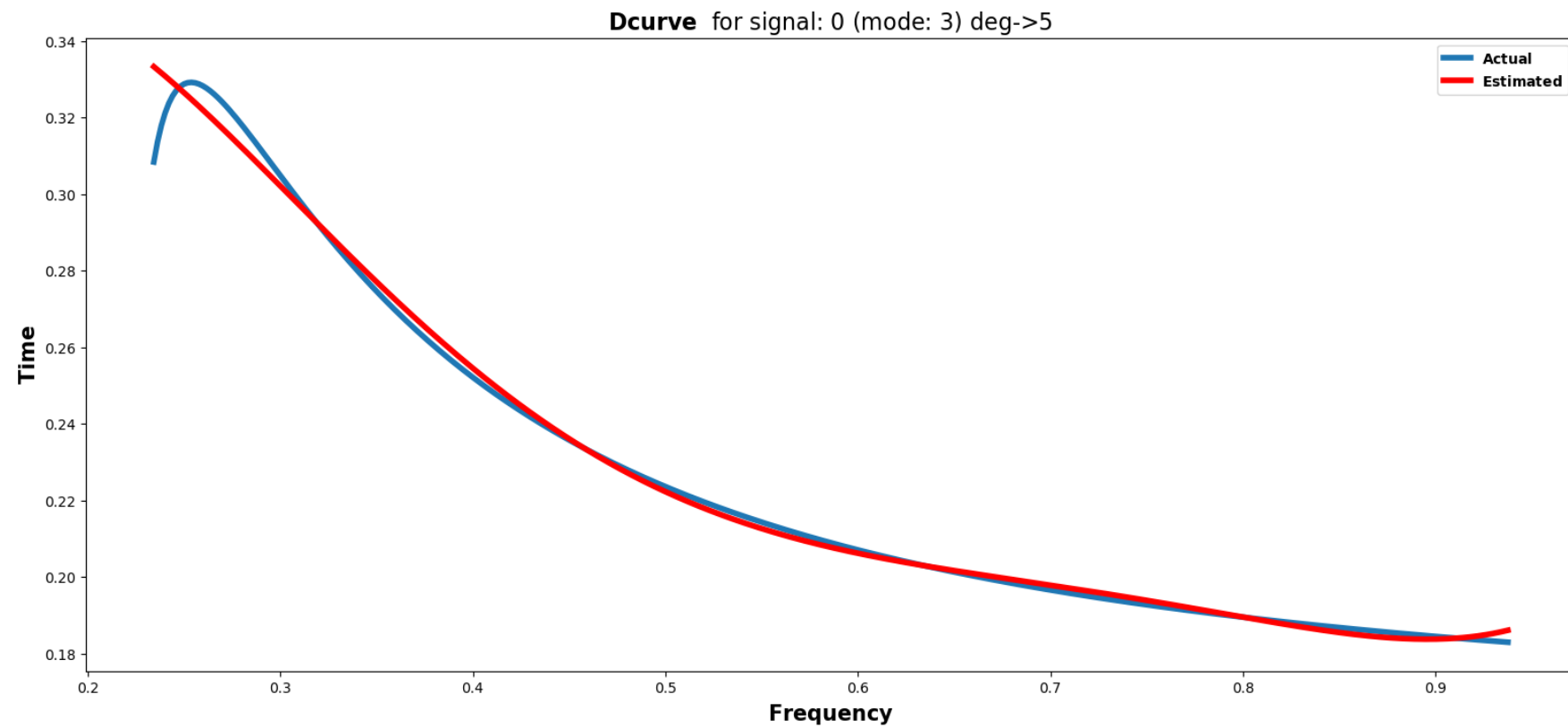
## Mode 2



## Mode 3



## Mode 3

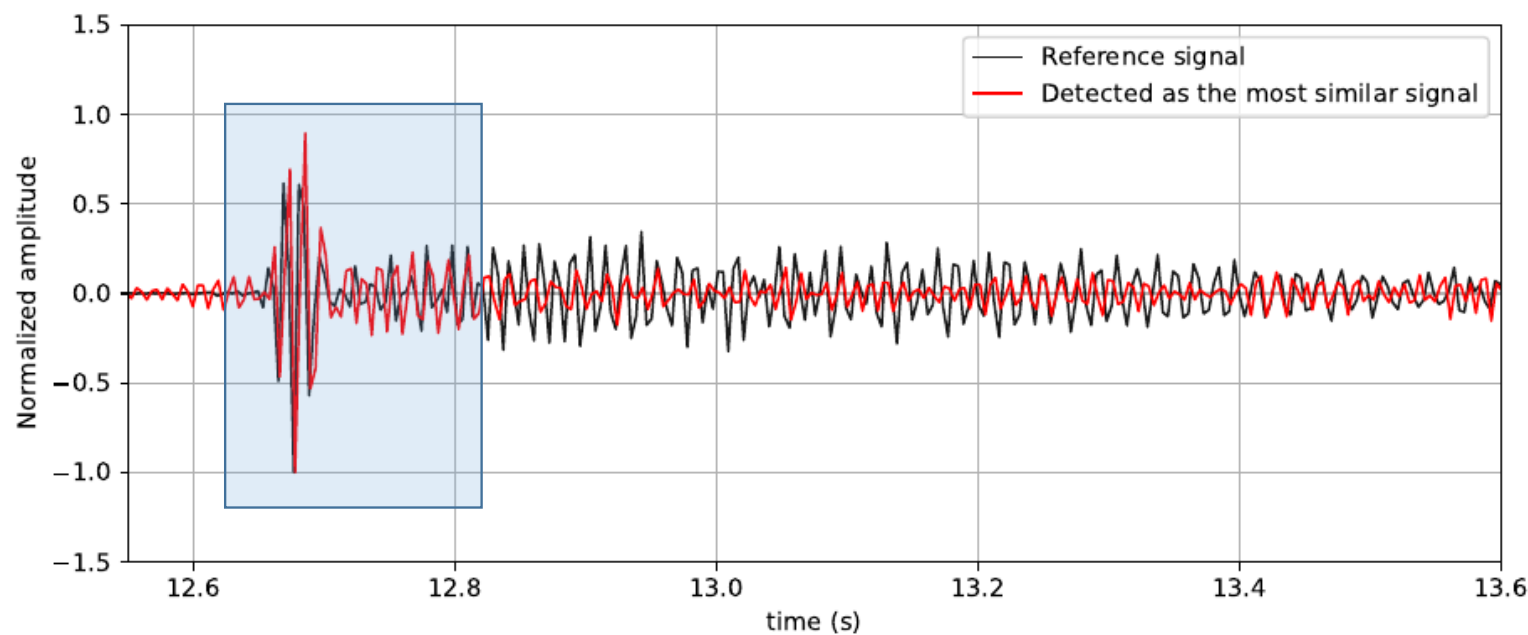


## **An attempt to use the estimated dispersion curves for environmental parameters estimation**

Discretize the curves and compare them with those associated with the signals of the data sets.

Use a simple least square norm of their distance to determine the closest (most similar) signal.

# Signal associated with estimated dispersion curves



Among signals of  
the NN sets

Naive inversion

# Comparison between the environmental/operational parameters associated with the “measured” signal and the “closest” signal

Reference

Closest signal

$r \text{ (km)}$	18.834	18.994
$c_{w1} \text{ (m/s)}$	1500	1503
$c_{w2} \text{ (m/s)}$	1485	1488
$c_{w3} \text{ (m/s)}$	1506	1505
$z_{min} \text{ (m)}$	23	24
$h_1 \text{ (m)}$	112	105
$h_2 \text{ (m)}$	133	126
$z_s \text{ (m)}$	48	43
$z_r \text{ (m)}$	20	31
$c_b \text{ (m/s)}$	1653	1659
$c_{sb} \text{ (m/s)}$	1812	1780

## Conclusions

- The students under appropriate supervision can produce interesting results to be used as the basis of further research.
- The identification of the modal packets of an underwater acoustic signal in the time-frequency domain using Artificial Neural Network seems feasible.

## Future projects

- For realistic applications there is a need to increase the training set.
- Application in inverse problems of ocean acoustic tomography or geoacoustic inversion, based on the identification of the dispersion characteristics of the propagating modes.
- We need to identify higher order modal packets.
- Try splines instead of polynomials



*Thank you for your attention*

Ευχαριστώ για την προσοχή σας

관심을 가져주셔서 감사합니다.