

```
> require(fBasics)
```

```
Loading required package: fBasics
```

```
Loading required package: timeDate
```

```
Loading required package: timeSeries
```

Rmetrics Package fBasics

Analysing Markets and calculating Basic Statistics

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Educational Software for Financial Engineering and Computational Science

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<https://www.rmetrics.org> --- Mail to: info@rmetrics.org

```
>
```

```
> #-----
```

```
> ### Part 1 ###
```

```
> da <- read.table("m-ge3dx8113.txt",header=T)
```

```
> head(da)
```

```
  PERMNO  date    ge  vwretd  ewretd  sprtrn
1 12060 19810130 0.000000 -0.040085 0.005615 -0.045742
2 12060 19810227 0.089796 0.015521 0.002150 0.013277
3 12060 19810331 0.014981 0.046184 0.072674 0.036033
4 12060 19810430 -0.020522 -0.011268 0.027885 -0.023456
5 12060 19810529 0.001905 0.013551 0.027187 -0.001657
6 12060 19810630 -0.046768 -0.010242 -0.013194 -0.010408
```

```
> # a) basic stats of raw data
```

```
> basicStats(da$ge)
```

```
      X..da.ge
nobs    396.000000
NAs      0.000000
Minimum  -0.272877
Maximum   0.251236
1. Quartile -0.025779
3. Quartile  0.053870
Mean       0.012900
Median     0.008022
Sum        5.108405
SE Mean    0.003572
LCL Mean   0.005878
UCL Mean   0.019922
Variance   0.005051
Stdev      0.071073
Skewness   -0.226160
Kurtosis    1.373376
```

```
> basicStats(da$vwretd)
```

```
      X..da.vwretd
nobs      396.000000
NAs        0.000000
Minimum    -0.225363
Maximum     0.128496
1. Quartile -0.016682
3. Quartile  0.039373
Mean        0.009698
Median      0.014381
Sum         3.840419
SE Mean     0.002263
LCL Mean    0.005249
UCL Mean    0.014147
Variance    0.002028
Stdev       0.045036
Skewness    -0.780736
Kurtosis    2.526277
> basicStats(da$ewretd)
```

```
      X..da.ewretd
nobs      396.000000
NAs        0.000000
Minimum    -0.272248
Maximum     0.225012
1. Quartile -0.019678
3. Quartile  0.039903
Mean        0.011022
Median      0.015401
Sum         4.364730
SE Mean     0.002686
LCL Mean    0.005740
UCL Mean    0.016304
Variance    0.002858
Stdev       0.053461
Skewness    -0.499120
Kurtosis    3.259182
> basicStats(da$sprtrn)
```

```
      X..da.sprtrn
nobs      396.000000
NAs        0.000000
Minimum    -0.217630
Maximum     0.131767
1. Quartile -0.017593
3. Quartile  0.035838
Mean        0.007594
```

```

Median      0.011063
Sum         3.007062
SE Mean     0.002207
LCL Mean    0.003254
UCL Mean    0.011933
Variance    0.001929
Stdev       0.043921
Skewness    -0.658830
Kurtosis    2.204877

```

> # b) Log returns of the raw data

> basicStats(exp(da\$ge)-1)

```

      X..exp.da.ge..1
nobs      396.000000
NAs        0.000000
Minimum    -0.238814
Maximum     0.285613
1. Quartile -0.025450
3. Quartile  0.055348
Mean        0.015527
Median      0.008055
Sum         6.148507
SE Mean     0.003609
LCL Mean    0.008431
UCL Mean    0.022622
Variance    0.005158
Stdev       0.071822
Skewness    0.113377
Kurtosis    1.049145

```

> basicStats(exp(da\$vwretd)-1)

```

      X..exp.da.vwretd..1
nobs      396.000000
NAs        0.000000
Minimum    -0.201774
Maximum     0.137117
1. Quartile -0.016544
3. Quartile  0.040159
Mean        0.010756
Median      0.014485
Sum         4.259201
SE Mean     0.002251
LCL Mean    0.006330
UCL Mean    0.015181
Variance    0.002007
Stdev       0.044799

```

```

Skewness      -0.530368
Kurtosis       1.728979
> basicStats(exp(da$ewretd)-1)
      X..exp.da.ewretd..1
nobs      396.000000
NAs        0.000000
Minimum     -0.238335
Maximum      0.252338
1. Quartile  -0.019485
3. Quartile   0.040710
Mean         0.012513
Median       0.015520
Sum          4.955338
SE Mean      0.002693
LCL Mean     0.007220
UCL Mean     0.017807
Variance     0.002871
Stdev        0.053581
Skewness     -0.111537
Kurtosis     2.686021
> basicStats(exp(da$sprtrn)-1)
      X..exp.da.sprtrn..1
nobs      396.000000
NAs        0.000000
Minimum     -0.195577
Maximum      0.140842
1. Quartile  -0.017439
3. Quartile   0.036487
Mean         0.008583
Median       0.011124
Sum          3.398995
SE Mean      0.002197
LCL Mean     0.004264
UCL Mean     0.012903
Variance     0.001912
Stdev        0.043724
Skewness     -0.422155
Kurtosis     1.550534
> # c) Test the Null Hypothesis
> t.test(da$ge)

```

One Sample t-test

data: da\$ge

t = 3.6119, df = 395, p-value = 0.0003432
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
0.005878371 0.019921654
sample estimates:
mean of x
0.01290001

```
> # e) obtain emperical density plot
> d1=density(da$ge)
> d2=density(da$sprtrn)
> par(mfcol=c(1,2))
> plot(d1$x,d1$y,xlab='returns',ylab='density',main= "GE",type='l')
> plot(d2$x,d2$y,xlab='returns', ylab='density', main='SP', type='l')
>
> #-----
> ### Part 2 ###
> ge=da$ge
> lr <- (exp(da$ge)-1)
> lr
[1] 0.0000000000 0.0939510949 0.0150937777 -0.0203128569 0.0019068157 -
0.0456912285
[7] -0.0140414857 -0.0805834547 -0.0035726030 -0.0113253795 0.1195233339 -
0.0357830907
[13] 0.0934359653 0.0060180361 0.0208912293 0.0119042988 -0.0344795533
0.0429153368
[19] 0.0339630082 0.1554466741 0.0046618327 0.1604745311 0.0909457712
0.0260084679
[25] 0.0951693403 0.0494948992 -0.0241281476 0.0676671130 -0.0731634033
0.0760285555
[31] -0.0889723218 0.0253797174 0.0419312893 -0.0187784461 0.1202221345
0.0266057786
[37] -0.0699296030 -0.0427378537 0.0670565820 0.0114551130 -0.0418903018 -
0.0023502339
[43] 0.0000000000 0.0817401560 -0.0066011163 0.0318878617 -0.0270192683
0.0228296980
[49] 0.1365927827 0.0047080482 -0.0682837841 0.0000000000 0.0352800812
0.0208330401
[55] 0.0370332579 -0.0475646040 -0.0472102321 0.0021763649 0.1489276166
0.1245804132
[61] -0.0254437112 0.1070048113 0.0129866029 -0.0047656083 0.0210178277
0.0232123079
[67] -0.0940444174 0.0801014803 -0.0754739027 0.0627607463 0.0925615663
0.0447054713
```

[73] 0.1802166225 0.0316629347 0.0208187486 -0.0130254252 0.0048426881
0.0533957568
[79] 0.0937968587 0.0563842582 -0.0106627456 -0.2052081321 -0.1001624213
0.0508065372
[85] 0.0229217568 0.0083446239 -0.0996259582 0.0000000000 0.0410689273
0.0544043391
[91] -0.0253150613 -0.0540409515 0.0865113858 0.0057806438 0.0320209838
0.0035623301
[97] 0.0843774028 -0.0528179826 -0.0181934638 0.1033102731 0.1248469703 -
0.0463075128
[103] 0.1424464822 -0.0148456997 -0.0123313382 -0.0197150654 0.1270898987
0.0490688907
[109] -0.0342825670 -0.0004818839 0.0413167312 -0.0038834399 0.0871026088
0.0054598510
[115] 0.0348908891 -0.1257422165 -0.1071949223 -0.0448357846 0.0543083927
0.0589310967
[121] 0.1223985972 0.0730113056 0.0241848214 0.0162892464 0.1041557326 -
0.0411982968
[127] -0.0100838140 0.0224318946 -0.0644718099 -0.0053904193 -0.0597354433
0.2092024378
[133] -0.0162072264 0.0458709675 -0.0291380560 0.0116179704 -0.0032576822
0.0255253317
[139] -0.0159484548 -0.0321517785 0.0675913113 -0.0189864431 0.0883807051
0.0352003677
[145] 0.0073367833 -0.0229544444 0.0692142148 0.0169724223 0.0237250657
0.0399129420
[151] 0.0291374251 -0.0025347820 -0.0176042031 0.0118031134 0.0142759417
0.0761533821
[157] 0.0277932211 -0.0218008502 -0.0432144516 -0.0463895269 0.0456293992 -
0.0540617624
[163] 0.0837518975 -0.0123303505 -0.0251064564 0.0157060638 -0.0571272999
0.1248042269
[169] 0.0098522167 0.0651408032 -0.0061907578 0.0377314162 0.0363594053 -
0.0207301147
[175] 0.0476640798 -0.0021167565 0.0939182769 -0.0078123239 0.0631806197
0.0827228221
[181] 0.0681968072 -0.0161550840 0.0382639090 -0.0079938777 0.0737927422
0.0495253349
[187] -0.0455032111 0.0106947847 0.1054704600 0.0652260179 0.0778140907 -
0.0433129954
[193] 0.0478872560 -0.0060208019 -0.0297310715 0.1256807908 0.0918112343
0.0796155440
[199] 0.0863744940 -0.1022314650 0.0964393774 -0.0492508251 0.1538832579 -
0.0027033394

[205] 0.0578282652 0.0032312091 0.1189368574 -0.0115359448 -0.0210522415
0.0941250470
[211] -0.0124389882 -0.1001444243 -0.0017175234 0.1049101285 0.0334027521
0.1416824411
[217] 0.0285869838 -0.0425712756 0.1121476880 -0.0463494744 -0.0343887901
0.1176720552
[223] -0.0317848945 0.0308564896 0.0605259878 0.1535648301 -0.0388915258
0.2121455849
[229] -0.1276032762 -0.0093113781 0.1957038407 0.0104967079 0.0051803720
0.0059486232
[235] -0.0265443379 0.1513647755 -0.0146033219 -0.0486155125 -0.0913370085 -
0.0291264056
[241] -0.0400115252 0.0113731885 -0.0918484418 0.1727377821 0.0097320514 -
0.0050890069
[247] -0.0991441292 -0.0562849385 -0.0845467672 -0.0210130828 0.0590814756
0.0467749905
[253] -0.0704958434 0.0420438240 -0.0269044498 -0.1457599195 -0.0129109295 -
0.0594928237
[259] 0.1145313470 -0.0616807162 -0.1617601481 0.0246396604 0.0768703390 -
0.0907480041
[265] -0.0484775517 0.0486850017 0.0621455859 0.1675435362 -0.0251454514
0.0059405756
[271] -0.0083330857 0.0405329148 0.0146482493 -0.0264800877 -0.0116515883
0.0914946549
[277] 0.0893040434 -0.0266961851 -0.0596479946 -0.0185026841 0.0398380709
0.0487070244
[283] 0.0265821669 -0.0137397362 0.0306524002 0.0162109952 0.0370104434
0.0392112376
[289] -0.0100857938 -0.0194591777 0.0247329069 0.0038895447 0.0077649924 -
0.0431742658
[295] -0.0043196434 -0.0254671003 0.0083657994 0.0071534647 0.0548272400 -
0.0116891448
[301] -0.0635142749 0.0113620634 0.0598294511 -0.0054481050 -0.0094946386 -
0.0301831115
[307] -0.0081585370 0.0427995797 0.0447169631 -0.0053675430 0.0048537414
0.0646456279
[313] -0.0306931010 -0.0235736950 0.0129734342 0.0433336298 0.0197250172
0.0264210062
[319] 0.0126179429 0.0028420309 0.0749691892 -0.0057802298 -0.0673525345 -
0.0234858127
[325] -0.0450812303 -0.0525830523 0.1238687790 -0.1099298508 -0.0587542357 -
0.1140493237
[331] 0.0617813325 -0.0066934981 -0.0782626815 -0.2093516706 -0.1130254595 -
0.0377095973

```

[337] -0.2221604422 -0.2388135922 0.2068504111 0.2856134533 0.0678133934 -
0.1158645464
[343] 0.1541279071 0.0380178696 0.2074238013 -0.1232619325 0.1313617549 -
0.0481168564
[349] 0.0648021423 0.0049873959 0.1425355965 0.0369295598 -0.1246101947 -
0.1058904749
[355] 0.1251225916 -0.0967329203 0.1394264252 -0.0140543031 -0.0117899474
0.1785030130
[361] 0.1064403828 0.0467394007 -0.0407341244 0.0201503312 -0.0388348187 -
0.0315679901
[367] -0.0491234162 -0.0854617629 -0.0560036695 0.1028491858 -0.0467470638
0.1461310889
[373] 0.0456806363 0.0276328979 0.0550023559 -0.0241193648 -0.0247154457
0.1058076799
[379] -0.0043096865 -0.0019261426 0.1104662809 -0.0700784024 0.0033295306
0.0023688012
[385] 0.0633858334 0.0520261801 -0.0042977382 -0.0352632377 0.0472932724
0.0025763130
[391] 0.0522008309 -0.0492194498 0.0414583599 0.0987597020 0.0200921843
0.0614543542
> t.test(lr)

```

One Sample t-test

```

data: lr
t = 4.3019, df = 395, p-value = 2.137e-05
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
 0.00843089 0.02262218
sample estimates:
mean of x
0.01552653

```

```

> skewness(ge)
[1] -0.2261597
attr("method")
[1] "moment"
> tm3=skewness(ge)/sqrt(6/length(ge))
> tm3
[1] -1.83733
attr("method")
[1] "moment"
>
> kurtosis(ge)

```



```

[1] 1.373376
attr("method")
[1] "excess"
> tk=kurtosis(ge)/sqrt(24/length(ge))
> tk
[1] 5.578679
attr("method")
[1] "excess"
>
> #-----
> ### Part 3 ###
> require(forecast)
Loading required package: forecast
> suppressMessages(require(fpp))
>
> # a) Make a plot of the data
> plot(visitors)
> plot
standardGeneric for "plot" defined from package "graphics"

```

```

function (x, y, ...)
standardGeneric("plot")
<environment: 0x108c1d6d0>
Methods may be defined for arguments: x, y
Use showMethods("plot") for currently available ones.
>

```

```

> # b) forecast the next two years using Holt-Winters' multiplicative method
> aust <- window(visitors)
> fit_multi <- hw(aust,seasonal="multiplicative")
> print(fit_multi)

```

	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
May 2005	369.3175	343.3002	395.3348	329.5275	409.1076
Jun 2005	395.5080	365.2767	425.7393	349.2733	441.7427
Jul 2005	485.9444	446.0391	525.8497	424.9145	546.9743
Aug 2005	436.7465	398.5070	474.9859	378.2643	495.2287
Sep 2005	422.9069	383.6657	462.1481	362.8927	482.9211
Oct 2005	478.2627	431.4628	525.0627	406.6885	549.8370
Nov 2005	502.5833	450.9301	554.2365	423.5865	581.5800
Dec 2005	615.6455	549.4181	681.8728	514.3595	716.9314
Jan 2006	461.1564	409.3845	512.9284	381.9781	540.3348
Feb 2006	511.8202	452.0068	571.6335	420.3436	603.2968
Mar 2006	498.9206	438.3614	559.4798	406.3033	591.5378
Apr 2006	443.9647	388.1032	499.8261	358.5320	529.3974
May 2006	383.5190	333.5830	433.4550	307.1484	459.8896

Jun 2006	410.6680 355.4225 465.9134 326.1774 495.1585
Jul 2006	504.5116 434.4881 574.5350 397.4199 611.6032
Aug 2006	453.3808 388.5399 518.2217 354.2152 552.5464
Sep 2006	438.9632 374.3497 503.5767 340.1454 537.7811
Oct 2006	496.3635 421.2456 571.4814 381.4806 611.2464
Nov 2006	521.5446 440.4747 602.6146 397.5588 645.5305
Dec 2006	638.7996 536.9011 740.6982 482.9592 794.6400
Jan 2007	478.4461 400.1915 556.7008 358.7660 598.1263
Feb 2007	530.9496 441.9744 619.9248 394.8738 667.0255
Mar 2007	517.5100 428.7206 606.2994 381.7183 653.3017
Apr 2007	460.4553 379.6266 541.2840 336.8384 584.0721

```
> plot(fit_multi)
```

```
> plot
```

standardGeneric for "plot" defined from package "graphics"

```
function (x, y, ...)
```

```
standardGeneric("plot")
```

```
<environment: 0x108c1d6d0>
```

Methods may be defined for arguments: x, y

Use `showMethods("plot")` for currently available ones.

```
>
```

```
> # d) compare with exponential or damped and compare
```

```
> fit_multi_damped <- hw(aust,seasonal="multiplicative",damped=TRUE)
```

```
> plot(forecast(fit_multi_damped))
```

```
> plot
```

standardGeneric for "plot" defined from package "graphics"

```
function (x, y, ...)
```

```
standardGeneric("plot")
```

```
<environment: 0x108c1d6d0>
```

Methods may be defined for arguments: x, y

Use `showMethods("plot")` for currently available ones.

```
>
```

```
> fit_multi_exp <- hw(aust,seasonal="multiplicative",exponential=TRUE)
```

```
> plot(forecast(fit_multi_exp))
```

```
> plot
```

standardGeneric for "plot" defined from package "graphics"

```
function (x, y, ...)
```

```
standardGeneric("plot")
```

```
<environment: 0x108c1d6d0>
```

Methods may be defined for arguments: x, y

Use `showMethods("plot")` for currently available ones.

```
>
```

```
> fit_multi_exp_damped <- hw(aust,seasonal="multiplicative",
+                             exponential=TRUE,damped=TRUE)
> plot(forecast(fit_multi_exp_damped))
> plot
```

standardGeneric for "plot" defined from package "graphics"

```
function (x, y, ...)
standardGeneric("plot")
<environment: 0x108c1d6d0>
Methods may be defined for arguments: x, y
Use showMethods("plot") for currently available ones.
```

```
>
> accuracy(fit_multi)
      ME  RMSE  MAE   MPE  MAPE  MASE  ACF1
Training set -0.9498442 14.8295 10.96716 -0.8150922 4.271167 0.4050069 0.2223887
> accuracy(fit_multi_damped)
      ME  RMSE  MAE   MPE  MAPE  MASE  ACF1
Training set 0.9123468 14.44801 10.64909 0.07071844 4.064322 0.3932608 0.01740636
> accuracy(fit_multi_exp_damped)
      ME  RMSE  MAE   MPE  MAPE  MASE  ACF1
Training set 0.7230142 14.45533 10.72791 0.03798703 4.090931 0.3961716 0.01218167
```

```
>
> #-----
```

```
> ### Part 4 ###
```

```
>
> # a)
> fit_multi <- hw(aust,seasonal="multiplicative")
> plot(fit_multi)
> plot
```

standardGeneric for "plot" defined from package "graphics"

```
function (x, y, ...)
standardGeneric("plot")
<environment: 0x108c1d6d0>
Methods may be defined for arguments: x, y
Use showMethods("plot") for currently available ones.
```

```
> hist(residuals(fit_multi),nclass=20)
> plot
```

standardGeneric for "plot" defined from package "graphics"

```
function (x, y, ...)
standardGeneric("plot")
<environment: 0x108c1d6d0>
Methods may be defined for arguments: x, y
```

Use showMethods("plot") for currently available ones.

```
> plot(residuals(fit_multi))
```

```
> plot
```

standardGeneric for "plot" defined from package "graphics"

```
function (x, y, ...)
```

```
standardGeneric("plot")
```

```
<environment: 0x108c1d6d0>
```

Methods may be defined for arguments: x, y

Use showMethods("plot") for currently available ones.

```
> accuracy(fit_multi)
```

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
--	----	------	-----	-----	------	------	------

Training set	-0.9498442	14.8295	10.96716	-0.8150922	4.271167	0.4050069	0.2223887
--------------	------------	---------	----------	------------	----------	-----------	-----------

```
>
```

```
> # b)
```

```
> fit_mam <- ets(visitors, model="ZZZ")
```

```
> plot(forecast(fit_mam))
```

```
> hist(residuals(fit_mam),nclass=20)
```

```
> plot(residuals(fit_mam))
```

```
> accuracy(fit_mam)
```

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
--	----	------	-----	-----	------	------	------

Training set	-1.536043	15.86105	11.53405	-0.7017724	4.076346	0.4259416	-0.004687451
--------------	-----------	----------	----------	------------	----------	-----------	--------------

```
>
```

```
> # c)
```

```
> fit_ana_box <- ets(visitors,additive.only=TRUE,lambda=TRUE)
```

```
> plot(forecast(fit_ana_box))
```

```
> hist(residuals(fit_ana_box),nclass=20)
```

```
> plot(residuals(fit_ana_box))
```

```
> accuracy(fit_ana_box)
```

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
--	----	------	-----	-----	------	------	------

Training set	2.346807	17.51126	13.18528	0.5506054	5.103531	0.4869199	0.02105629
--------------	----------	----------	----------	-----------	----------	-----------	------------

```
>
```

```
> # d)
```

```
> fit_naive <- snaive(visitors,lambda=TRUE)
```

```
> plot(forecast(fit_naive))
```

```
> hist(residuals(fit_naive),nclass=20)
```

```
> plot(residuals(fit_naive))
```

```
> accuracy(fit_naive)
```

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
--	----	------	-----	-----	------	------	------

Training set	18.22368	32.56941	27.07895	7.011798	10.12935	1	0.6600405
--------------	----------	----------	----------	----------	----------	---	-----------

```
>
```

```
> # e)
```

```
> fit_stld <- stlf(visitors,method="ets",lambda=TRUE)
```

```
> plot(forecast(fit_stld))
```

```
>  
> hist(residuals(fit_std),nclass=20)  
> plot(residuals(fit_std))  
> accuracy(fit_std)  
      ME   RMSE   MAE   MPE   MAPE   MASE   ACF1  
Training set -0.3615751 12.17064 9.129055 -0.226499 3.252608 0.3371274 -0.02051013
```