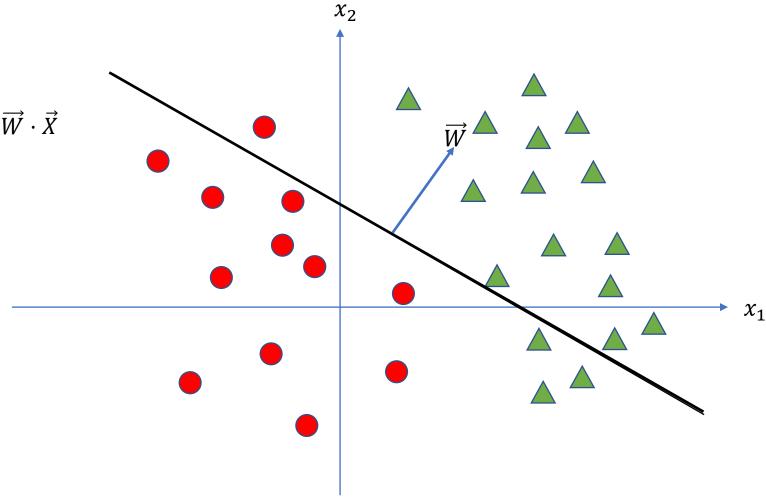


Prediction:

$$z = \overrightarrow{w} \cdot \overrightarrow{x} + b$$

$$z = \begin{bmatrix} w_1 & w_2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + b$$

$$z = \begin{bmatrix} b & w_1 & w_2 \end{bmatrix} \begin{bmatrix} 1 \\ x_1 \\ x_2 \end{bmatrix} = \overrightarrow{W} \cdot \overrightarrow{X}$$

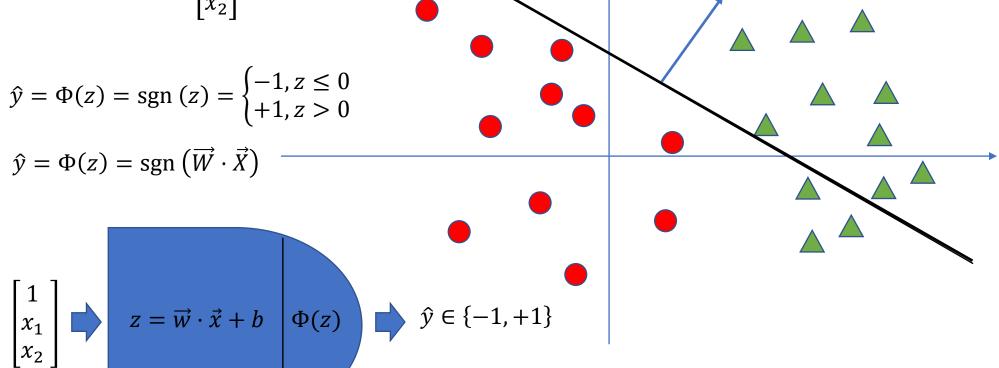


Prediction:

$$z = \overrightarrow{w} \cdot \overrightarrow{x} + b$$

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$$z = \begin{bmatrix} b & w_1 & w_2 \end{bmatrix} \begin{bmatrix} 1 \\ x_1 \\ x_2 \end{bmatrix} = \overrightarrow{W} \cdot \overrightarrow{X}$$



Prediction:

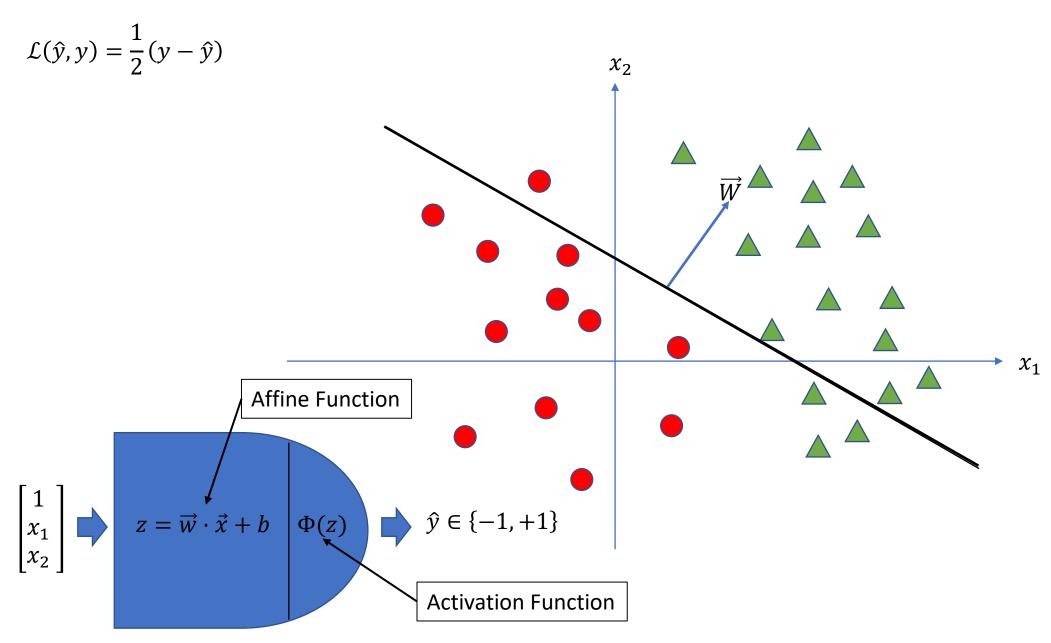
$$z = \overrightarrow{w} \cdot \overrightarrow{x} + b$$

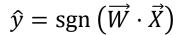
$$z = \begin{bmatrix} w_1 & w_2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + b$$

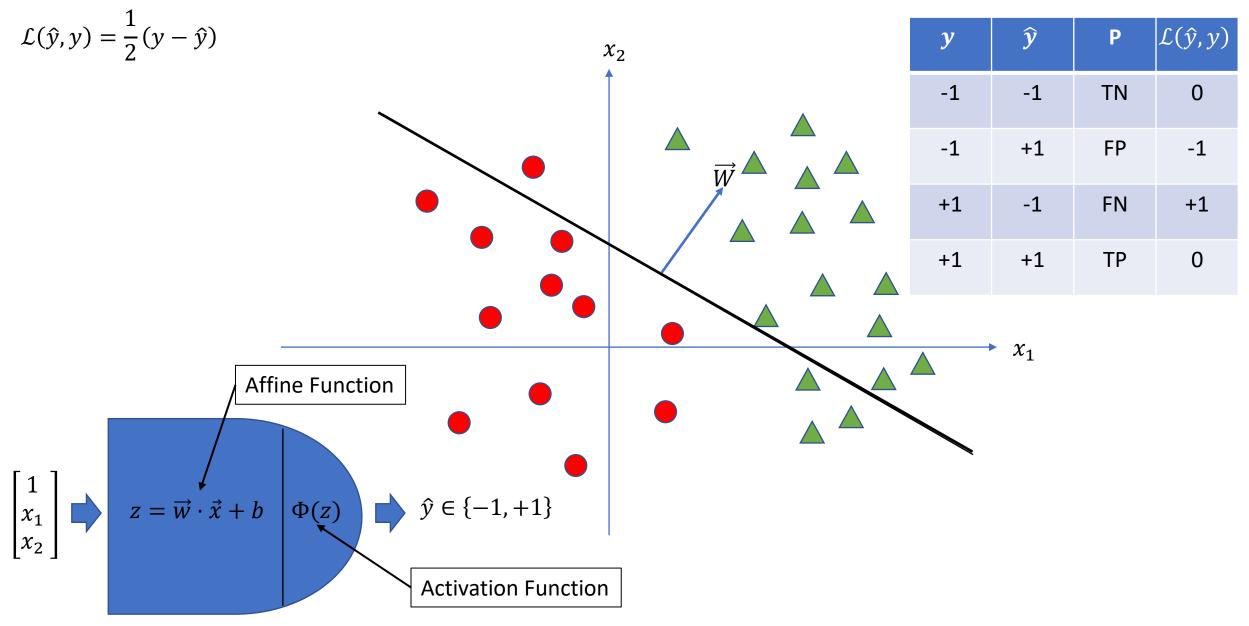
$$z = \begin{bmatrix} b & w_1 & w_2 \end{bmatrix} \begin{bmatrix} 1 \\ x_1 \\ x_2 \end{bmatrix} = \overrightarrow{W} \cdot \overrightarrow{X}$$

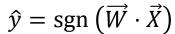
$$\hat{y} = \Phi(z) = \operatorname{sgn}(z) = \begin{cases} -1, z \le 0 \\ +1, z > 0 \end{cases}$$

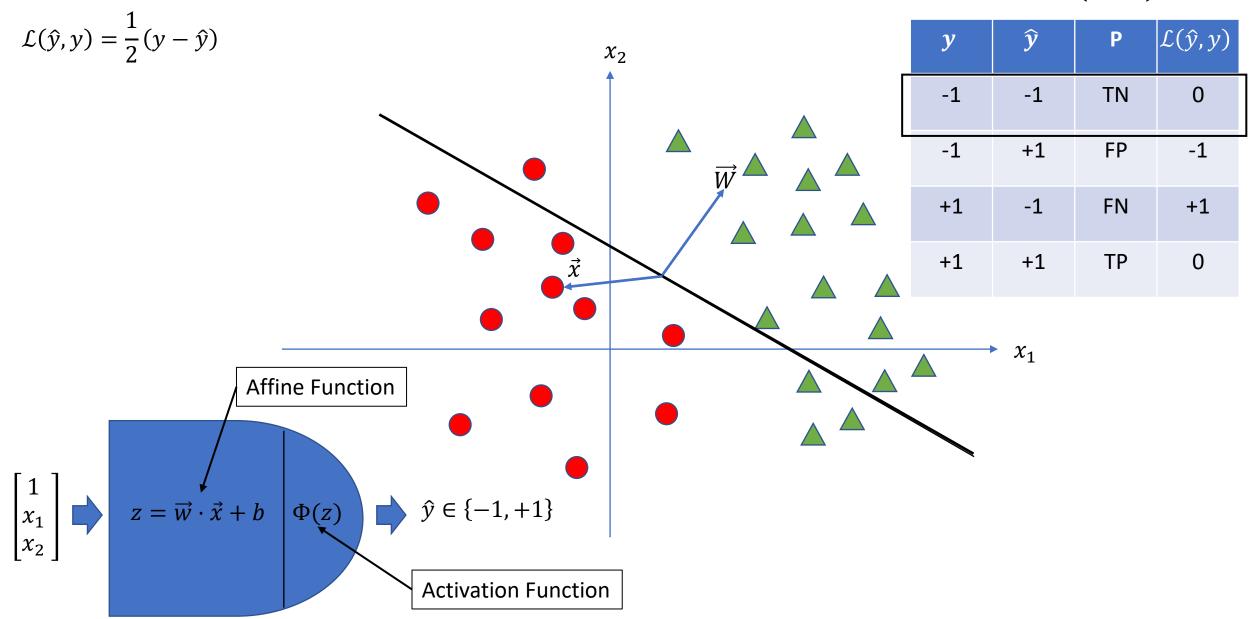
$$\hat{y} = \Phi(z) = \operatorname{sgn}(\overrightarrow{W} \cdot \overrightarrow{X})$$
Affine Function
$$\begin{bmatrix} 1 \\ x_1 \\ x_2 \end{bmatrix} \Rightarrow z = \overrightarrow{w} \cdot \overrightarrow{x} + b \quad \Phi(z)$$
Activation Function



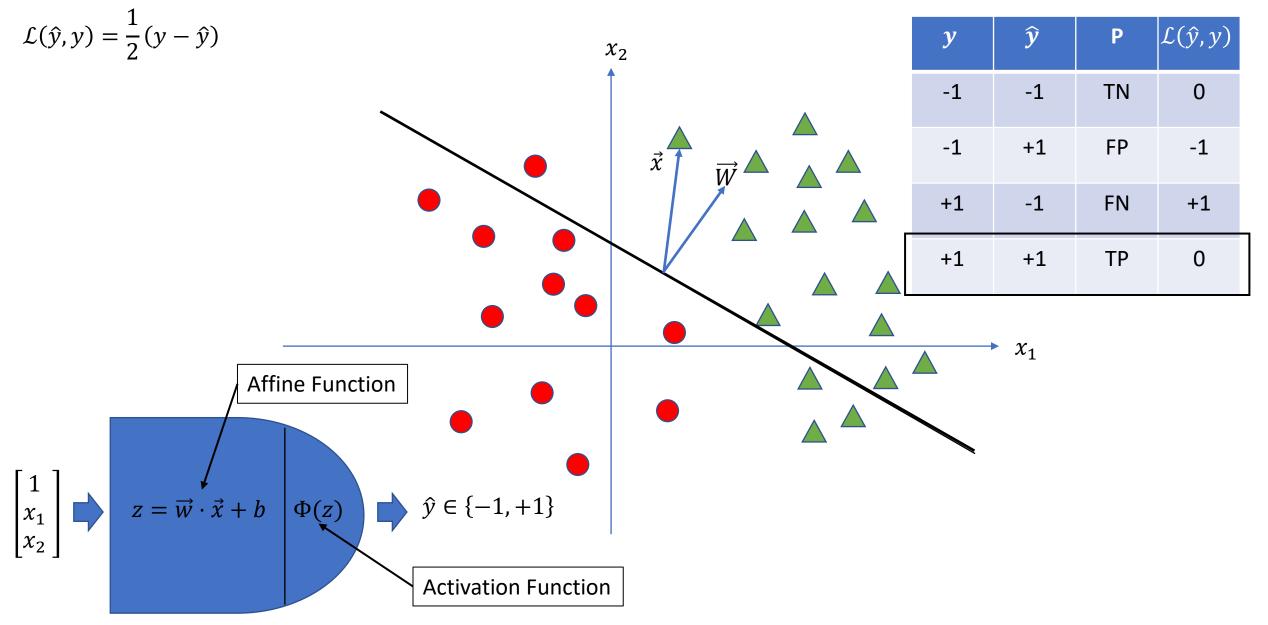


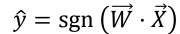


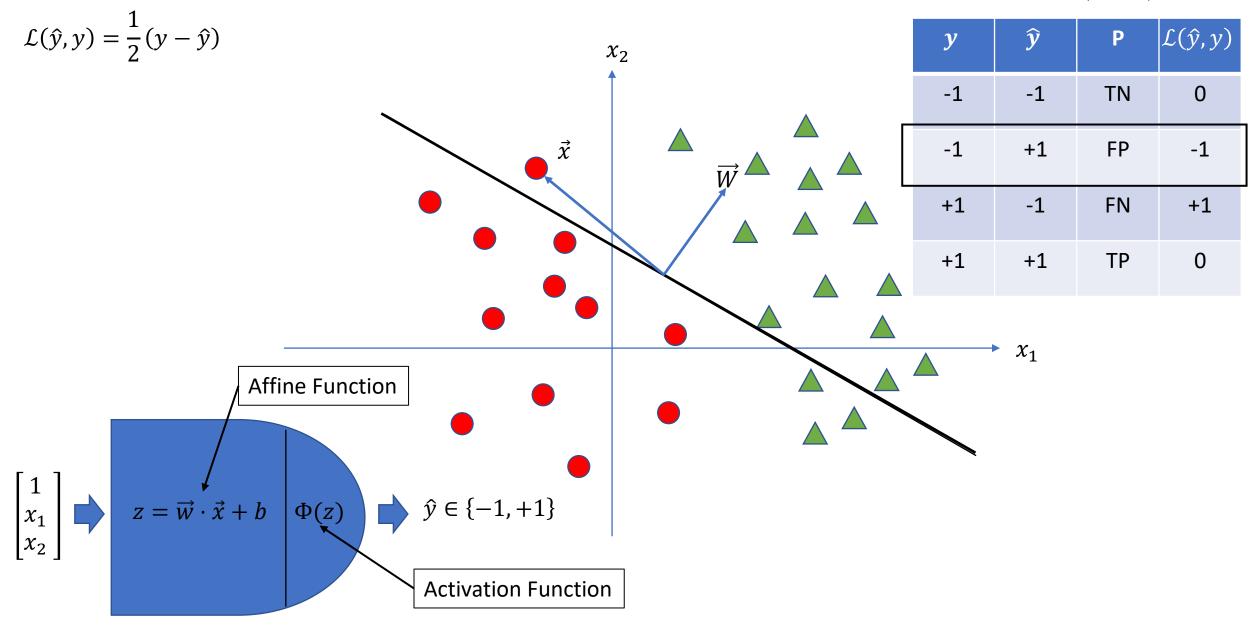


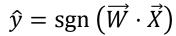


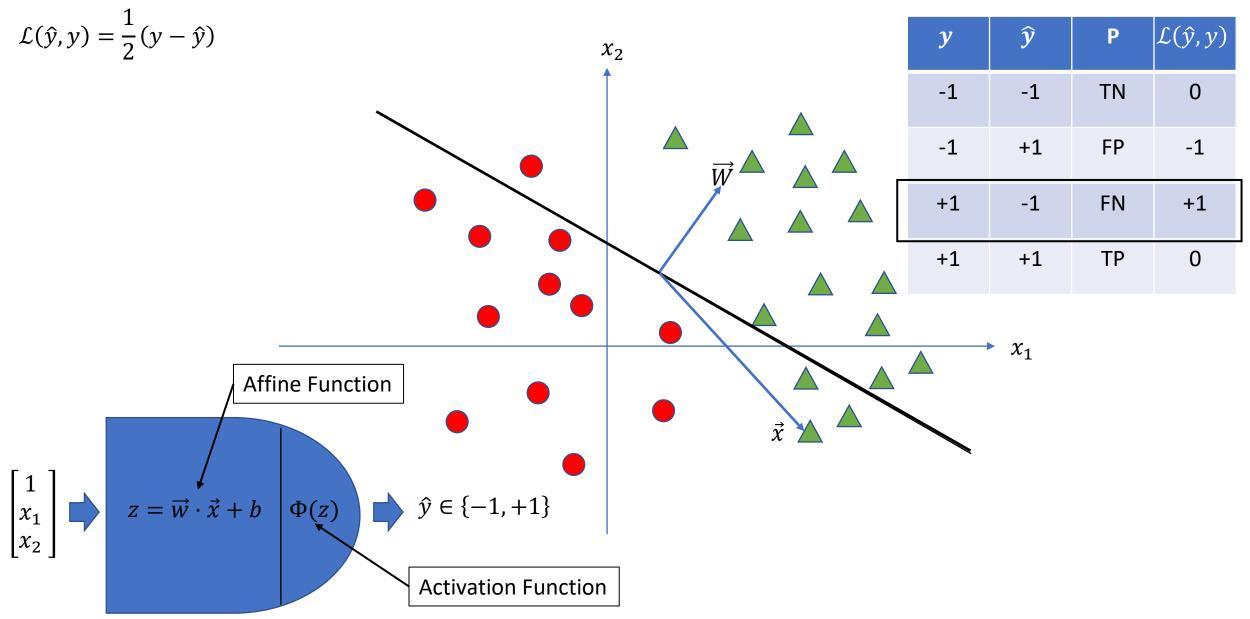












$$\hat{y} = \operatorname{sgn}\left(\overrightarrow{W} \cdot \overrightarrow{X}\right)$$

P

TN

FP

FN

TP

 $\mathcal{L}(\hat{y}, y)$

0

-1

+1

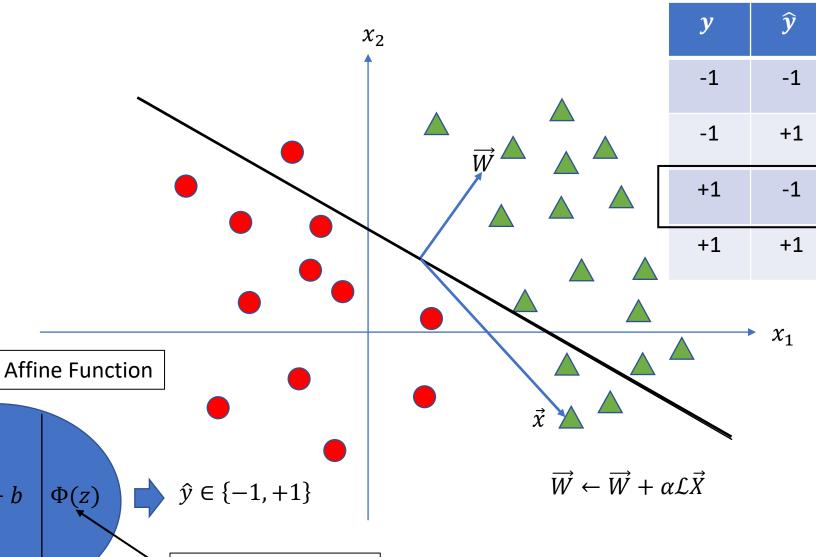
0

$$\mathcal{L}(\hat{y}, y) = \frac{1}{2}(y - \hat{y})$$

UPDATE:

$$\overrightarrow{W} \leftarrow \overrightarrow{W} + \alpha \mathcal{L}(\widehat{y}, y) \, \overrightarrow{X}$$

 α = Learning Rate



$$\begin{bmatrix} 1 \\ x_1 \\ x_2 \end{bmatrix}$$

$$z = \vec{w} \cdot \vec{x} + b \quad \Phi(z) \qquad \hat{y} \in \{-1, +1\}$$

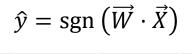
Activation Function

$$\mathcal{L}(\hat{y}, y) = \frac{1}{2}(y - \hat{y})$$

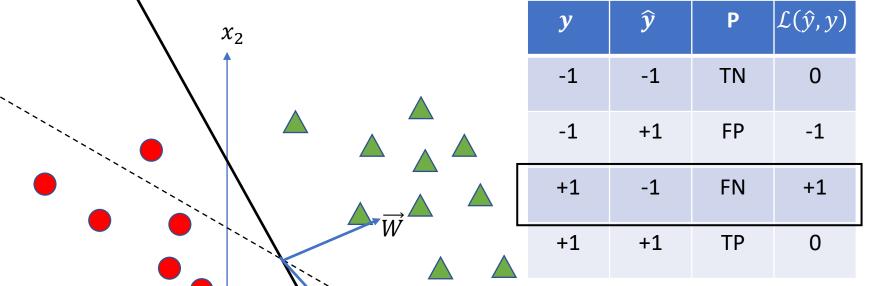
UPDATE:

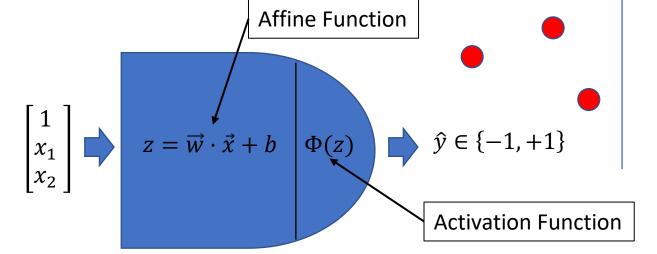
$$\overrightarrow{W} \leftarrow \overrightarrow{W} + \alpha \mathcal{L}(\widehat{y}, y) \, \overrightarrow{X}$$

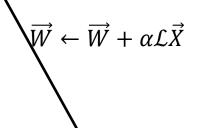
 α = Learning Rate



 x_1







$$\mathcal{L}(\hat{y}, y) = \frac{1}{2}(y - \hat{y})$$

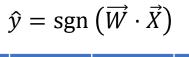
UPDATE:

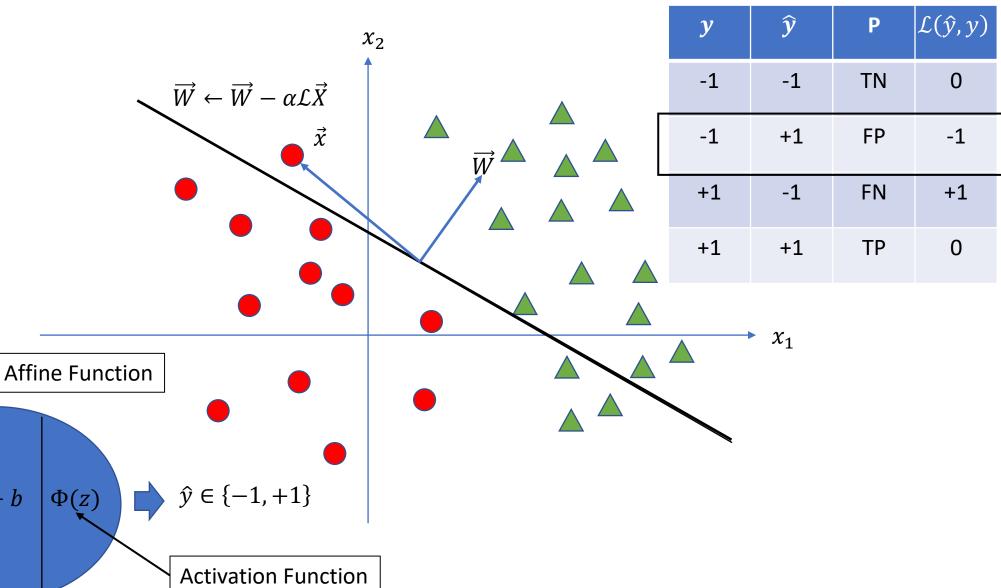
$$W \leftarrow W + \alpha \mathcal{L}(\hat{y}, y) \vec{X}$$

 $z = \overrightarrow{w} \cdot \overrightarrow{x} + b$

 $\Phi(z)$

 α = Learning Rate





$$\mathcal{L}(\hat{y}, y) = \frac{1}{2}(y - \hat{y})$$

UPDATE:

$$W \leftarrow W + \alpha \mathcal{L}(\hat{y}, y) \, \vec{X}$$

 α = Learning Rate

