

3.1 Given a time Function, $T(n) = 2n^2 + 4n + 3$, find Constants C and N that prove that the Big O of the growth function $T(n)$ is n^2 .

$$T(n) = 2n^2 + 4n + 3$$

$$[C * g(n)]$$

$$2n^2 + 4n + 3 \leq 2n^2 + 4n^2 + 3n^2$$

$$2n^2 + 4n + 3 \leq 10n^2$$

$$[C = 10 \quad n_0 = 1]$$

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Guessing
 $O(n^2)$ for
time Complexity.

Find The Big O of $T(n) = 2n^3 + 5n^2 + n + 2$.
Justify your answer by finding Constants C and N .

Guessing $O(n^3)$ for time Complexity.

3.2 $T(n) = 2n^3 + 5n^2 + n + 2$

$$2n^3 + 5n^2 + n + 2 \leq 2n^3 + 5n^3 + n^3 + 2n^3$$

$$2n^3 + 5n^2 + n + 2 \leq 10n^3$$

In the form $C * g(n)$

$$[C = 10, \quad n_0 = 1]$$

Big O: $O(n^3)$

3.3

Find the Big O of the following Code:

```
for (int i = 0, i < n/2; i++)  
    {  
        for (int j = 0; j < n/2; j++)  
            {  
                System.out.println("Hello");  
            }  
    }
```

The Big O is : $O(n^2)$

The inner loop can be expressed as $2n+2$, and for every iteration of the outer loop (equal to n times) there's a full n iterations from the inner loop:

$$(2n+2) * N = 2n^2 + 2n$$

This "nested loop" is an n^2 time Complexity Contribution.