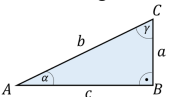
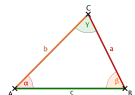


| Grundlagen | |
|--|------------------------|
| Mengen: | |
| $\mathbb{N} = \{1, 2, 3, \dots\}$ | Natürliche Zahlen |
| $\mathbb{N}_0 = \{0, 1, 2, \dots\}$ | Natürliche Zahlen (+0) |
| $\mathbb{Z} = \{\dots, -1, 0, 1, \dots\}$ | Ganze Zahlen |
| $\mathbb{Q} = \{\frac{p}{q}\}$ | Rationale Zahlen |
| $\mathbb{R} = \{\dots, \sqrt{3}, \pi, \dots\}$ | Reelle Zahlen |

| Trigonometrie | |
|---|--|
| Rechtwinkliges Dreieck: | |
|  | |
| $\sin(\alpha) = \frac{a}{c}$ | $\cos(\alpha) = \frac{b}{c}$ |
| $\tan(\alpha) = \frac{a}{b}$ | |
| $\tan(\alpha) = \frac{\sin(\alpha)}{\cos(\alpha)}$ | $\cos(\alpha) = \frac{\sin(\alpha)}{\tan(\alpha)}$ |
| $\sin(\alpha) = \tan(\alpha) \cdot \cos(\alpha)$ | |

| | |
|---|--|
| Allgemeines Dreieck: | |
|  | |
| Sinussatz: | |
| $\frac{a}{\sin(\alpha)} = \frac{b}{\sin(\beta)} = \frac{c}{\sin(\gamma)}$ | |
| Kosinussatz: | |
| $a^2 = b^2 + c^2 - 2bc \cos(\alpha)$ | |
| $b^2 = a^2 + c^2 - 2ac \cos(\beta)$ | |
| $c^2 = a^2 + b^2 - 2ab \cdot \cos(\gamma)$ | |
| Umrechnung Gradmass/Bogenmass: | |
| $x_{\text{Bogenmass}} = \frac{\alpha}{180^\circ} \cdot \pi$ | $x_{\text{Gradmass}} = \frac{\alpha}{\pi} \cdot 180^\circ$ |

| Binomische Formeln | |
|-------------------------------------|--|
| $(a + b)^2 = a^2 + 2ab + b^2$ | |
| $(a - b)^2 = a^2 - 2ab + b^2$ | |
| $(a + b) \cdot (a - b) = a^2 - b^2$ | |

| Brüche | |
|---|--|
| $\frac{\frac{a}{b}}{\frac{c}{d}} = \frac{a}{b} \cdot \frac{d}{c} = \frac{a \cdot d}{b \cdot c} = \frac{ad}{bc}$ | |

| Summenzeichen | |
|---|--|
| $\sum_i^n a = a_i + a_{i+1} + \dots + a_n$ | |
| Gaussche Summenformel: | |
| $\sum_{k=1}^n k = \frac{n(n+1)}{2}$ | |
| Für k^2 : | |
| $\sum_{k=1}^n k^2 = \frac{n(n+1)(2n+1)}{6}$ | |

| | |
|--|--|
| Rechenregeln: | |
| $\sum_{k=s}^n (c \cdot a_k) = c \cdot \sum_{k=s}^n a_k$ | |
| $\sum_{k=s}^n (a_k + b_k) = \sum_{k=s}^n a_k + \sum_{k=s}^n b_k$ | |
| $\sum_{k=s}^n (a_k \cdot b_k) = \sum_{k=s}^n a_k \cdot \sum_{k=s}^n b_k$ | |
| $\sum_{k=s}^n a_k + \sum_{k=n+1}^m a_k = \sum_{k=s}^m a_k$ | |
| $\sum_{k,l=s}^n a_{kl} = \sum_{k=s}^n \sum_{l=s}^n a_{kl}$ | |
| Indexttransformation: | |
| $\sum_{k=s}^n a_k = \sum_{k=s-k_0}^{n-k_0} a_k + k_0 \rightarrow$ | |

| Produktzeichen | |
|---|--|
| $\prod_i^n a = a_i \cdot a_{i+1} \cdot \dots \cdot a_n$ | |

| | |
|---|------------------------|
| Logarithmen $a^y = x \rightarrow \log_a x = y$ | |
| $\log_a(u \cdot v) = \log_a u + \log_a v$ | $\log_{10} x = \log x$ |
| $\log_a \frac{u}{v} = \log_a u - \log_a v$ | $\log_e x = \ln x$ |
| $\log_a u^x = x \cdot \log_a u$ | |
| $\log_a(x) = \frac{\log(x)}{\log(a)} = \frac{\ln(x)}{\ln(a)} = \frac{\log_c(x)}{\log_c(a)}$ | Basiswechsel |
| $\log_a(a^x) = x$ | $\log_a(1) = 0$ |
| $a^n = x \rightarrow n = \frac{\log(x)}{\log(a)}$ | |
| $\ln(x) = y \quad (e^{\dots} \rightarrow x = e^y$ | |

| | |
|---|-------------------------------------|
| Potenzen $a^n = a \cdot a \cdot \dots \cdot a$ | |
| $a^m \cdot a^n = a^{m+n}$ | $\frac{a^m}{a^n} = a^{m-n}$ |
| $a^n \cdot b^n = (a \cdot b)^n$ | $\frac{a^n}{b^n} = (\frac{a}{b})^n$ |
| $(a^n)^m = a^{m \cdot n} = (a^m)^n$ | |
| $a^0 = 1$ | $a^{-n} = \frac{1}{a^n}$ |
| Tricks: | |
| $x^{1+a} = y \cdot (a+2) \rightarrow x = (y \cdot (a+2))^{\frac{1}{1+a}}$ | |

| | |
|--|--|
| Wurzel | |
| Quadratwurzel: | |
| $\sqrt{a} = b \rightarrow b^2 = a$ | |
| $\sqrt{a} \cdot \sqrt{a} = a$ | $\frac{\sqrt{a}}{\sqrt{a}} = 1$ |
| $\sqrt{a} \cdot \sqrt{b} = \sqrt{ab}$ | $\frac{\sqrt{a}}{\sqrt{b}} = \sqrt{\frac{a}{b}}$ |
| $\sqrt{a^2} = a \rightarrow a \in \mathbb{R}$ | |
| Wurzel Tricks: | |
| $\frac{\sqrt{x}}{x} = \frac{1}{\sqrt{x}}$ | |
| $2\sqrt{x} \cdot \sqrt{1+\frac{1}{x}} = 2\sqrt{x \cdot (1+\frac{1}{x})} = 2\sqrt{x+1}$ | |

| | |
|---|---|
| Algem. Wurzel: | |
| $\sqrt[n]{a} = b \rightarrow b^n = a$ | |
| $\sqrt[n]{a} \cdot \sqrt[n]{a} = a^{\frac{1}{n}} \cdot a^{\frac{1}{n}} = a^{\frac{m+n}{m \cdot n}}$ | |
| $\sqrt[n]{a} : \sqrt[n]{a} = a^{\frac{1}{n}} : a^{\frac{1}{n}} = a^{\frac{m-n}{m \cdot n}}$ | |
| $\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{a \cdot b}$ | $\sqrt[n]{a^m} = a^{\frac{m}{n}} = (\sqrt[n]{a})^m$ |
| $\frac{\sqrt[n]{a}}{\sqrt[n]{b}} = \sqrt[n]{\frac{a}{b}}$ | $\sqrt[n]{\sqrt[n]{a}} = \sqrt[n]{\sqrt[n]{a}} = \sqrt[n]{a}$ |
| $\sqrt[n]{a} \rightarrow$ nicht definiert | $2\sqrt[n]{-1} \rightarrow$ nicht definiert |
| $2n+\sqrt[n]{-1} = 1$ | |

| Exponentialfunktion | |
|--|--|
| $f(x) = a \cdot b^x$ | |
| $a \rightarrow$ Anfangswert | |
| $b \rightarrow$ Wachstumsfaktor | |
| $\rightarrow b > 1$ Wachstum | |
| $\rightarrow b < 1$ Abnahme | |
| Prozentuale Zu- oder Abnahme (p%) | |
| $b = 1 \pm \frac{p}{100}$ | |

| Volumen und Flächen | |
|--|------------------------------------|
| Quadrat: | |
| $A = a^2$ | $U = 4 \cdot a$ |
| $d = \sqrt{2} \cdot a$ | |
| Rechteck: | |
| $A = a \cdot b$ | $U = 2a + 2b$ |
| $d = \sqrt{a^2 + b^2}$ | |
| Dreieck: | |
| $A = \frac{1}{2} \cdot a \cdot h$ | $U = a + b + c$ |
| Kreis: | |
| $A = \pi \cdot r^2$ | $U = 2\pi \cdot r$ |
| $A = \frac{d^2 \cdot \pi}{4}$ | |
| Zylinder: | |
| $V = \pi \cdot r^2 \cdot h$ | $A = 2 \cdot \pi(r^2 + r \cdot h)$ |
| Pyramide: | |
| $G \rightarrow$ Grundfläche (Quadrat, Rechteck, Dreieck) | |
| $V = \frac{1}{3} \cdot G \cdot h$ | $A = G + S_1, S_2, \dots$ |
| Kugel: | |
| $V = \frac{4}{3} \cdot \pi \cdot r^3$ | $A = 4 \cdot \pi \cdot r^2$ |

| Nullstellen von Gleichungen | |
|--|--|
| Grad 1 | |
| $x_0 = -\frac{b}{a}$ | |
| Grad 2 | |
| $x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ | |
| Weitere Methoden: | |
| <ul style="list-style-type: none"> Polynomdivision Faktorisierung Binomisierung | |

| Tricks mit lim | |
|---|--|
| $\lim_{n \rightarrow \infty} (1 + \frac{2}{5n})^{-\frac{2n}{5}} = \lim_{n \rightarrow \infty} (1 + \frac{1}{\frac{5n}{2}})^{-\frac{2n}{5}} =$ | |
| $\lim_{n \rightarrow \infty} (1 + \frac{1}{\frac{5n}{2}})^{\frac{5n}{2} \cdot \frac{-4}{25}} = e^{-\frac{4}{25}}$ | |
| $\lim_{n \rightarrow \infty} (\sqrt{n^2 + n} - \sqrt{n^2 - 2n}) = \lim_{n \rightarrow \infty} (\sqrt{n^2 + n} - \sqrt{n^2 - 2n}) \cdot \frac{\sqrt{n^2 + n} + \sqrt{n^2 - 2n}}{\sqrt{n^2 + n} + \sqrt{n^2 - 2n}} =$ | |
| $= \lim_{n \rightarrow \infty} \frac{n^2 + n - (n^2 - 2n)}{\sqrt{n^2 + n} + \sqrt{n^2 - 2n}} = \lim_{n \rightarrow \infty} \frac{3n}{\sqrt{n^2 + n} + \sqrt{n^2 - 2n}} \cdot \frac{1}{1} =$ | |
| $= \lim_{n \rightarrow \infty} \frac{3}{\sqrt{1 + \frac{1}{n}} + \sqrt{1 - \frac{2}{n}}} = \lim_{n \rightarrow \infty} \frac{3}{\sqrt{1 + \frac{1}{n}} + \sqrt{1 - \frac{2}{n}}} = \frac{3}{\sqrt{1} + \sqrt{1}} = \frac{3}{2}$ | |