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HERE ARE THE WORKS cited in this book. Numbers in the margin specify the page numbers where citations occur.

References to published problems are generally made to the places where solutions can be found, instead of to the original problem statements.

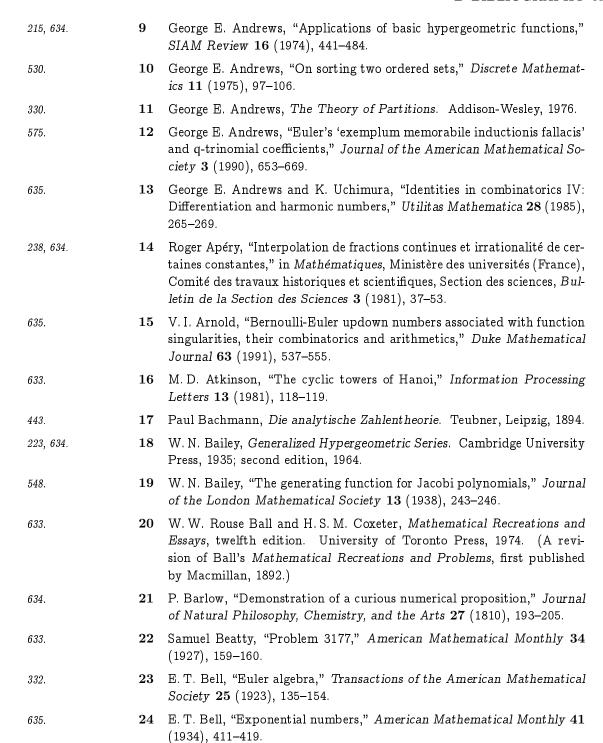
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ein Quadrat von der Form

$$z \; = \; 1 + \frac{\alpha'}{1} \cdot \frac{\beta'}{\gamma'} \cdot \frac{\delta'}{\varepsilon'} \, x \, + \, \frac{\alpha'.\alpha' + 1}{1.2} \cdot \frac{\beta'.\beta' + 1}{\gamma'.\gamma' + 1} \cdot \frac{\delta'.\delta' + 1}{\varepsilon'.\varepsilon' + 1} \, x^2 + \text{etc. hat,"}$$

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