

**MAU22C00: TUTORIAL 12 PROBLEMS**  
**GRAPH THEORY**

- 1) Let  $(V, E)$  be the graph with vertices  $a, b, c, d, e$ , and  $f$  and edges  $ab, ac, bc, bd, cd, de, df$ , and  $ef$ .
- (a) Draw this graph.
  - (b) Is this graph connected? Justify your answer.
  - (c) What is the minimum number of edges you would have to remove for the resulting subgraph to have two connected components? Justify your answer.
  - (d) What about three connected components? Justify your answer.
  - (e) What about four connected components? Justify your answer.
  - (f) What about five connected components? Justify your answer.
  - (g) Give an example of a shortest possible circuit in the graph. Justify your answer.
  - (h) Give an example of a longest possible circuit in the graph. Justify your answer.