BALAD

(Beginners Assembly Language and Debugger)

1 INTRODUCTION

BALAD is an assembly level programming language for an emulated virtual computer with a 15 bit word length. It is combined with a comprehensive debugging system which allows on line program assembly, execution of programs and the insertion of breakpoints to allow suspension of programs during execution.

Instructions are machine oriented, using integer and logical operations only. As a concession to the beginner, extra input/output instructions are provided for automatic Decimal to Binary conversion and the printing of Text Strings. These facilities will enable students to obtain reasonable print out of their results quickly, while concentrating their efforts on developing algorithms.

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https://github.com/JohnWulff/balad \$Id: BALAD.odt 1.4 2020/12/29

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generated with the BALAD program smiley.bl

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2 THE BALAD COMPUTER

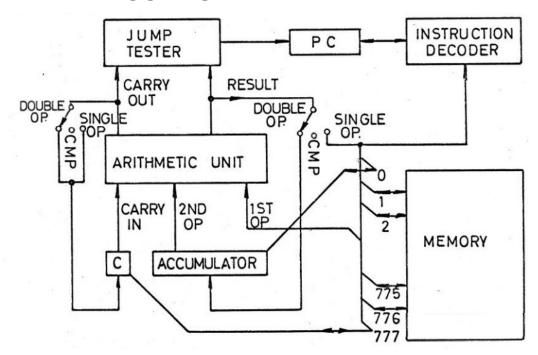


Fig. 1.

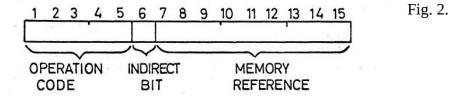
The BALAD computer is a one accumulator machine with an arithmetic unit for performing logical operations and 15 bit two's complement arithmetic. The Memory has 512 15 bit words with addresses 0 to 777 (octal numbering). Memory words may contain instructions, addresses of other memory words or data.

At the start of every instruction cycle the address in the Program Counter register (PC) is used by the computer to fetch the next instruction from memory into the Instruction Decoder. The program counter is normally incremented by 1 at the end of an instruction cycle so that the next instruction is fetched from the next location in Memory. Only a jump instruction can break this sequence by loading the Program counter (PC) with a new address which points to some arbitrary point in the memory from where the next instruction will then be fetched.

The Instruction Decoder isolates Bits 1 to 5 of the instruction and uses this as a number to distinguish between one of the 32 possible instructions. The instruction that has been identified is then executed. In a hardwired computer this process involves setting various switches to allow data to flow from various registers to other registers.

For illustration two such switches are shown in Fig. 1, which guide the result and carry out of an operation from the arithmetic unit either to the Accumulator and Carry for double operand instructions, ignore them for compare instructions or back to Memory and Carry for single operand instructions. The last 10 bits of the instruction are used to determine a memory reference address. This can again be thought of as setting a big switch which connects one data path to one of 512 words in memory.

2.1 THE INSTRUCTION FORMAT



Instructions are stored in 15 bit memory registers. Bits 1 to 5 are the operation code, which select 32 possible operations. Bit 6 is the Indirect bit. If it is zero (0) the value in bits 7 to 15 is taken as the address of the operation of the instruction. If the Indirect bit is a one (1), the address in bits 7 to 15 is used to locate another word whose value in bits 7-15 is used as the address of the first operand of the instruction. Before this is done the Indirect bit of this new word is first checked, and if it is a one (1) the process is repeated. Normally only one level of indirect addressing is used. If more than four levels of indirect address are attempted the computer will stop. This is to break up infinite indirect addressing chains which can happen accidentally if an indirect reference points to itself.

Of the 32 instructions, 4 are double operand arithmetic or logical operations, 2 are data moving operations, 10 are single operand operations, 8 are conditional or unconditional jump operations and the remaining 8 are Input/Output operations. Each instruction has a memory reference part, which addresses a word in memory.

2.1.1 Double Operand Operations

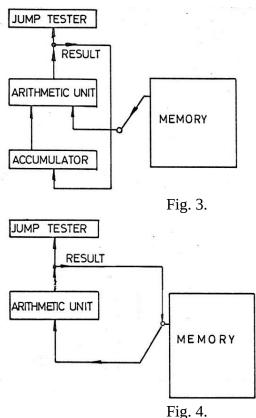
For double operand operations the 1st operand is taken from the addressed memory location, while the second operand is the Accumulator.

The result of the operation is stored in the Accumulator and in the Jump Tester as described later. One exception is the Compare (CMP) operation for which the result is only stored in the Jump Tester. The result in the Jump Tester is used by conditional jump instructions which follow an operation.

2.1.2 Single operand operations

For single operand operations the one operand is taken from the addressed memory location and the result is stored back in that same location. The result is also stored in the Jump Tester.

Six different conditions of the result in the Jump Tester can be tested and if the condition is *True* a jump to the memory reference address in the jump instruction is executed. If *False*, the next instruction is executed. Note that the result used in the test is the



result of the last operation executed before the test in the following jump instruction. It does not matter whether this result was also stored in the Accumulator, a memory location, or not stored at all, as in a CMP or TST instructions.

Most arithmetic operations are characterized by the fact that information is carried from one bit position to the next. All computers have an arithmetic unit of limited length (15 bits in this machine). Therefore arithmetic operations will sometimes overflow. So that this case can be accounted for, the output of the most significant bit (bit 1) is available to the programmer. In fact the arithmetic unit is extended by one bit to 16 bits, and for practical purposes the 1st operand is extended by 1 bit. Storage for this bit is in the "carry" register. The contents of the carry register also serves as input for most arithmetic operations, and the output of the "carry" position of the arithmetic unit is stored back in the carry register for both single and double operand operations. Only for the compare operation (CMP) and the test operation (TST) is the new value not stored. The output of the carry position is also stored in the jump tester for subsequent tests for the state of "carry". The Jump Tester is affected by CMP and TST.

For programmer convenience, the Accumulator and the carry register are both addressable by a memory reference. This means that all the single operand operations can also be carried out on the accumulator and the carry. Since the carry is only a one bit register some of the operations may not be very significant. The Accumulator has memory address 0 and the predefined label **ACC**; the carry register has address 777, the highest address and the predefined label **C**.

2.2 THE INSTRUCTIONS

2.2.1 Double Operand Operations

AND MR with Accumulator (OP CODE 20)

The logical **and** function of each bit of the contents of the Memory Reference and each bit of the Accumulator is stored in the Accumulator and the Jump Tester. Carry is not affected.

ADD MR to Accumulator (OP CODE 22)

Add the contents of the Memory Reference and Carry to the Accumulator and store the Result in the Accumulator. If the unsigned sum is $> 2^{15}$, set the Carry register, else reset it. Accumulator and Carry are also stored in the Jump Tester.

SUB MR from Accumulator (OP CODE 24

Subtract by adding the two's complement of the contents of the Memory Reference and Carry to the Accumulator and store the Result and Carry-out in the Accumulator, Carry and the Jump Tester.

CMP Accumulator with MR (OP CODE 26)

The same operation as SUB except that Carry-in is set to *zero* and the Result and Carry-out are only stored in the Jump Tester. Accumulator, Carry and Memory Reference are left unmodified.

2.2.2 Move data instructions

LDA Load Accumulator from MR. (OP CODE 30)

Load the contents of the Memory Reference into the Accumulator and the Jump Tester. The contents of the Memory Reference and Carry are unaffected. The original contents of the Accumulator is lost.

STA Store Accumulator at MR. (OP CODE 32)

Store the contents of the Accumulator at the Memory Reference location and the Jump Tester. The contents of the Accumulator and Carry are unaffected. The original MR contents is lost.

2.2.3 Single Operand Instructions

CLR Clear MR (OP CODE 34)

Zero is stored in the Memory Reference location and the Jump Tester. Carry is not affected.

TST Test MR (OP CODE 36)

Move the contents of the memory reference to the jump tester without changing the MR. Carry is not affected.

COM Complement MR (OP CODE 40)

Store the logical complement of the contents of the Memory Reference in the Memory Reference location and the Jump Tester. Carry is not affected. The logical complement is also the bit wise complement or the One's complement.

NEG Negate MR (OP CODE 42)

Store the Two's complement of the contents of the Memory Reference in the Memory Reference location and the Jump Tester. If the original contents was zero, complement Carry.

INC Increment MR (OP CODE 44)

Add 1 to the contents of the Memory Reference and store the result at the Memory Reference location and the Jump Tester. If the original contents was 2^{15} -1 (signed -1), complement carry.

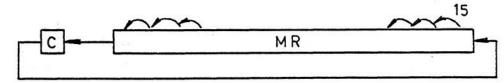
DEC Decrement MR (OP CODE 46)

Subtract 1 from the contents of the Memory Reference and store the result at the Memory Reference location and the Jump Tester. If the original contents was 0, complement Carry.

2.2.4 Rotate and shift instructions

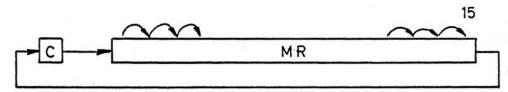
These are single operand operations for bit manipulation, scaling data by factors of 2 and byte manipulation. Rotates are used for testing sequential bits of a word. In each the Carry register and the contents of the Memory Reference are manipulated in different ways, and the result is stored in the Memory reference location, Carry and the Jump Tester.

ROL Rotate left MR and Carry (OP CODE 50) Fig. 5.



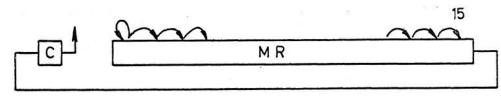
Rotate the contents of the Memory Reference and the Carry Register one bit left as shown in Fig. 5.

ROR Rotate Right MR and Carry (OP CODE 52) Fig. 6.

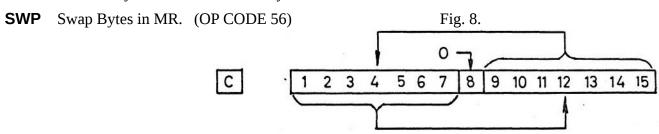


Rotate the contents of the Memory Reference and the Carry Register one bit right as shown in Fig. 6.

ASR Arithmetic Shift Right MR and Carry. (OP CODE 54) Fig. 7.



The sign bit (bit 1) is replicated and also shifted right. All other bits are also shifted right and bit 15 is shifted into Carry. The old value of Carry is lost.



Bits 1 to 7 and bits 9 to 15 of the contents of the Memory Reference are Swapped. Bit 8 is set to zero. Carry is not affected. The process is illustrated in Fig. 8. A 7 bit BYTE is normally used to store a 7 bit ASCII character. The **SWP** operation allows 2 7 bit ASCII characters to be stored and retrieved from one word. NOTE: no 8 bit extended ASCII characters can be used in BALAD.

2.2.5 Jump Instructions

These instructions allow the alteration of the normal program sequence by jumping to an arbitrary location in memory. Conditional jump instructions also test the copy of the last result or carry stored in the Jump Tester. If the condition tested is *True*, a jump is performed If the condition is *False*, the next instruction in the word sequence is executed. No registers, except the Program counter are modified in the operations.

A special case is a jump to location 0, which is also the Accumulator. This instruction is interpreted as a *HALT* (**HLT**) instruction and execution of a program stops and control is returned to the calling OS or the Debugging System. (A conditional halt can be implemented by making the memory reference of one of the conditional jump instructions 0 although this is deprecated).

JMP Unconditional Jump. (OP CODE 00)

Load the Memory Reference of the instruction (not its contents, unless the memory reference is indirect) into the Program Counter (PC). This has the effect, that the next instruction is fetched from the new location now pointed to by the PC

JZR Jump if Zero Result. (OP CODE 04)

JEQ Jump if equal. jump if ACC == MR following a CMP instruction

Load MR into PC if the last Result stored in the jump tester was zero. Otherwise execute the next instruction.

JNR Jump if Non-Zero Result. (OP CODE 06)

JNE Jump if not equal. jump if ACC != MR following a CMP instruction

Load MR into PC if the last Result stored in the jump tester was non-zero. Otherwise execute the next instruction.

JZC Jump if Zero Carry. (OP CODE 10)

JLT Jump if less than. jump if **ACC** < **MR** following a **CMP** instruction

Load MR into PC if the last Carry stored in the Jump Tester was *Zero*. Otherwise execute the next instruction.

JNC Jump if Non-Zero Carry. (OP CODE 12)

JGE Jump if greater than or equal. jump if ACC >= MR following a CMP instruction

Load MR into PC if the last Carry stored in the Jump Tester was *One*. Otherwise execute the next instruction.

JEZ Jump if ether zero. (OP CODE 14)

JLE Jump if less than or equal. jump if **ACC** <= MR following a CMP instruction

Load MR into PC if either the Result or the Carry stored in the Jump Tester were *Zero*. Otherwise execute the next instruction.

JBN Jump if both non-zero (OP CODE 16)

JGT Jump if greater than. jump if **ACC** > **MR** following a **CMP** instruction

Load MR into PC if both the Result and the Carry stored in the Jump Tester were *Non-zero*. Otherwise execute the next instruction.

JMS Jump to Subroutine. (OP CODE 02)

Load the contents of the incremented Program Counter (PC) into the Memory Reference location. This is the address of the next instruction in the normal program sequence. Then load MR + 1. (not its contents) into the PC. Thus a jump has been made to the location MR + 1.

Subroutines are written in this system with the first location free to store the "Return Address" (PC+1 as above). The first instruction in the subroutine follows this location. To return from a subroutine, an indirect jump is made via the first location of the subroutine. Then control is transferred to the location following the one from which the call was made. Indirect Memory references are written in the assembler language by preceding a location number by the symbol "@" e.g. JMP @400, which is jump indirect contents of location 400 for a subroutine at LOC 400.

2.2.6 Input instructions

KDN Key Decimal Number to MR (OP CODE 60)

When this instruction is executed the string <u>Enter a short number</u>: is output to indicate to the operator that a single precision decimal number is to be typed on the keyboard. The first character may be "+" or "-" or a decimal digit. If no sign is typed the number is assumed to be positive. A number is terminated by the Enter key and execution of the program continues. The number that was typed is converted to a 15 bit binary number and stored at the Memory Reference location. If the number is to be interpreted as signed the absolute magnitude must be less than 8,192 (2¹⁴). If unsigned, input must be positive and less than 16,384 (2¹⁵). If input exceeds these limits, the converted number will be reduced modulo 2¹⁵.

KDD Key Double Decimal to MR and MR+1. (OP CODE 62)

When this instruction is executed the string <u>Enter a long number</u>: is output to indicate to the operator that a double precision decimal number is to be typed on the keyboard. The first character may be "+" or "-" or a decimal digit. If no sign is typed the number is assumed to be positive. A number is terminated by the Enter key and execution of the program continues. The number that was typed is converted to a 30 bit binary number and stored at MR and MR+1. If the number is to be interpreted as signed the absolute magnitude must be less than 536,870,912 (2²⁹). If unsigned, input must be positive and less than 1,073,741,824 (2³⁰). If input exceeds these limits, the converted number will be reduced modulo 2³⁰.

KCH Key Character to MR. (OP CODE 64)

When this instruction is executed the first character that is typed on the keyboard is stored at the memory reference location as a 7 bit ASCII character in bits 9 to 15. Bits 1 to 8 are made zero. This is normally the only form of input from a keyboard on a simple computer. The character is not echoed. All the other input instructions echo the characters typed.

KCS Key Character String to MR+. (OP CODE 66)

Key in characters and store them two bytes to a word starting at MR. The Enter key terminates entry and stores a NULL to terminate the string. Care is taken not to overflow memory.

When *q* or *Ctrl-D* is entered at the keyboard when executing any of the Key input instructions **KDN**, **KDD** or **KCS**, this will stop the running BALAD program and return to the debug input >> if it was started from the debugger. Otherwise the program will terminate. **KCH** will only stop with *Ctrl-D*. *Ctrl-C* will always terminate a BALAD program.

2.2.7 Output Instructions

Print and Type are the same in BALAD

PDN Print Decimal Number at MR. (OP CODE 70)

TDN Type Decimal Number at MR.

Convert, the contents of Memory Reference, interpreted as a 15 bit two's complement number to a decimal character string and type this string on the screen.

PDD Print Double Decimal at MR and MR+1. (OP CODE 72)

TDD Type Double Decimal at MR and MR+1.

Convert the contents of MR and MR+1 interpreted as a 30 bit two's complement number to a decimal character string and type this string on the screen.

PCH Print Character at MR. (OP CODE 74)

TCH Type Character at MR.

Type the character corresponding to the ASCII code represented by bits 9 to 15 of the contents of the Memory Reference Bits 1 to 8 are ignored.

PRF Print Character String starting at MR. (OP CODE 76)

TCS Type Character String starting at MR.

A Character String is a sequence of characters terminated by a NULL character (ASCII 0). A convention for this machine, and for many other computers is that character strings are stored 2 characters per word in the following format:

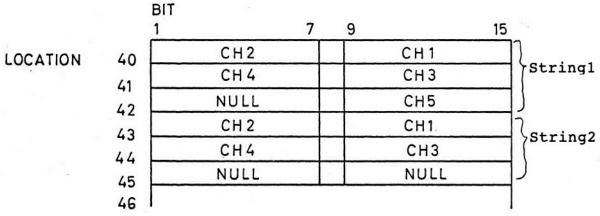


Fig. 9

Character strings may contain page formatting characters of the ASCII alphabet, such as a NEW LINE entered as \n, or a TAB entered as \t. A real \ must be entered as \\. In practice character strings are entered into the memory by the Debugging system during Program Assembly as "a character string in parenthesis". The addresses of the first character in each string is then known and an instruction PRF for that address will cause that character string to be printed at execution time. This facility can be used to provide spaces between numbers, to start printing on a new line, and to precede key number instructions with a printout of a short message to indicate what the number represents. Printout of results can also be preceded or followed by messages to make a reasonably workmanlike end result of a computation, and to aid in the identification of results, which is very important.

The **PRF** instruction has been extended so that the parameter string pointed to by **MR** is interpreted like the format string of a *printf* instruction in the Perl or *C* language. The % character in such a string starts a conversion defined as follows:

%d word at next ADR n after the PRF is output as a short signed decimal. word at next ADR n after the PRF is output as a short unsigned decimal. %u word at next ADR n after the PRF is output as a short unsigned octal. %0 word at next ADR n after the PRF is output as a short unsigned hexadecimal. %x %b word at next ADR n after the PRF is output as a short unsigned binary. string starting at next ADR n after the PRF is output as an embedded string. %s character at next **ADR n** after the **PRF** is output as an embedded character. %C %% print a single %.

When the letters d, u, o, x and b are preceded by a letter '1', the word ADR n after the PRF is interpreted as a long double precision word at ADR n and ADR n+1. The letters D, U and O are aliases for 1d, 1u and 1o. Field width numbering follows *printf* conventions in Perl or C.

ADR is a pseudo instruction, which tells the assembler that the following **MR** is an address.

2.3 THE ASSEMBLY LANGUAGE

Computer programs are stored in the computer Memory as binary numbers. This is the way a computer reads instructions. As human beings we devise short-cuts to make what is often referred to as a binary machine language program more tractable. The first step is to divide every binary number mentally into a number of groups of three bits. In our case for a 15 bit machine we would have five 3 bit groups.

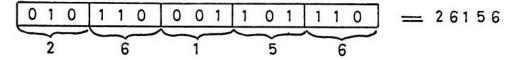


Fig. 10

Then each group of 3 bits can easily be converted into a number between 0 and 7. The 5 numbers together constitute the OCTAL representation of the binary number. OCTAL representations can be used for instructions or data. Certain sub-fields of a Memory location, e.g. the 9 bit Memory reference can be expressed as a 3 digit OCTAL number.

OCTAL representations are easier to handle in the long run than DECIMAL representations because they preserve the regularity of binary groups. OCTAL counting is easy as long as you remember that, you always stop at 7 and then go to the next highest position say 10 or 17 to 20, etc. The main use for OCTAL numbers in this machine is for addressing Memory locations¹.

Another simplification is to break up a binary number into arbitrary fields and to give each possible combination of bits in a field a label. This is a little like labeling 3 bit fields with digits 0 to 7 for the 8 possible bit combinations. In this assembly language the OP CODE field of instructions has been treated this way. The OP CODE field is bits 1 to 5 and there are 32 labels each of 3 characters to distinguish these 32 codes. The characters are chosen to convey the name of the operation mnemonically eg. **ADD** for add, **SUB** for subtract etc.

¹ NOTE: in modern assembly languages it is more common to break up binary numbers into 4 bit fields, which are expressed as HEXADECIMAL digits, which are 0-9 and a-f for 10-15. This is appropriate for word length of 16, 32 and 64 bits, which do not divide neatly by 3. In 1970, when BALAD was first implemented word length of 12 and 18 bits were more common.

The indirect bit of an instruction, bit 6, is expressed with the symbol "@" if the bit is a 1. No character implies bit 6 is 0. Numerical Memory references in an instruction may be written as OCTAL numbers. Memory locations can also be labeled with an arbitrary text, which is an alias for that numerical address. These labels can then be used instead of absolute OCTAL addresses anywhere in the assembly code, where a Memory reference address is required. The advantage of labels is, that code and data can be moved in memory without changing that code. Simply the value expressed by a label is changed automatically in the symbol table during program assembly.

An address can also be defined as the address of the current instruction with the symbol \cdot (FULL STOP). The \cdot or a label can be followed by + or – followed by a decimal displacement to evaluate an address.

To write a program or data block, the address of the first location must be defined. This is done with the LOC or BLK pseudo instructions. LOC followed by an OCTAL address defines the starting address of the block to follow. BLK followed by a DECIMAL displacement will leave a block of memory locations uninitialized, compute the new address and output that as before.

When typing program code into the computer follow an address defined by LOC or BLK with the 3 character mnemonic of the operation code followed by optional spaces or the @ symbol if the memory reference is indirect. Lastly type the memory reference of the instruction, either as an absolute OCTAL address, a relative address using . or a label optionally followed by a simple displacement. If no memory reference is typed 0 is assumed which means the operation refers to the Accumulator. Lastly type Enter, which will cause analysis of the instruction and cause the next address to be typed on the screen, ready for more program input, unless the instruction contained an error, in which case an appropriate error message will be output on the screen and the previous address is output on the screen again, ready for correct input. This ensures that only syntactically correct programs or data can be entered².

Alternatively to writing a block of program statements, we can initialize a block of numerical data. If the first character of a new entry is numeric the rest of the word must be filled by a single number. For convenience this number may be expressed as decimal, octal, hexadecimal or binary. The convention for modern programming languages is that a number starting with 1 to 9 is a decimal integer. A number starting with 0 is interpreted as octal with only digits 0 to 7. A number starting with 0x followed by digits 0 to 9 and a to f is interpreted as hexadecimal. A number starting with 0b followed by digits 0 or 1 only is interpreted as binary. Only decimal numbers may be preceded by an optional + or - sign. A number followed immediately by the letter 1 or L is considered to be a 30 bit double precision number using up two consecutive words.

Character strings are another form of constant that may be initialized during assembly. A character string is entered into memory by typing a parenthesis symbol " as the first character instead of a statement or a number. Any character following except another parenthesis " is regarded as another character in the string. Strings may contain two control characters written as \n for *new line* and \t for *tab* (space to the next column of 8). A real " character in a string is written as \" and a real \ as \\. A closing parenthesis terminates the string. After the following ENTER key, the next address after the string is typed.

2.3.1 Comments

In all cases, before typing ENTER, zero or more spaces followed by a ; or # followed by any text is a comment. For other variations, see the Debugging System.

² This does not mean a program is semantically correct – the algorithm may not do what it is intended to do.

Here is a small BALAD program example:

Comment block

```
LOC 10
                    ; initialized data block
op1:
        99
op2:
        81
sum:
        BLK 1
                    ; uninitialized data block
        LOC 100
                    ; code block
main:
        CLR C
                    ; clear carry before addition
        LDA op1
        ADD op2
        STA sum
        PDN sum
        HLT
```

This shows as the following assembler listing when run with balad -l

```
Comment block
             LOC 10 ; initialized data block
010
      00143
                   99
            op1:
011
      00121
            op2:
                   81
012
      00000
            sum:
                   BLK 1
                          ; uninitialized data block<sup>3</sup>
                   LOC 100; code block
100
      34777
            main:
                   CLR C
                          ; clear carry before addition
101
      30010
                   LDA op1
102
      22011
                   ADD op2
103
      32012
                   STA sum
104
      70012
                   PDN sum
105
      00000
                   HLT
```

The first two columns are the 3 digit octal memory address and the 5 digit octal memory contents, which may be code instructions or data numbers or strings.

³ Any memory not specifically initialized by the assembler is set to 00000

2.3.2 List of instructions in op code order

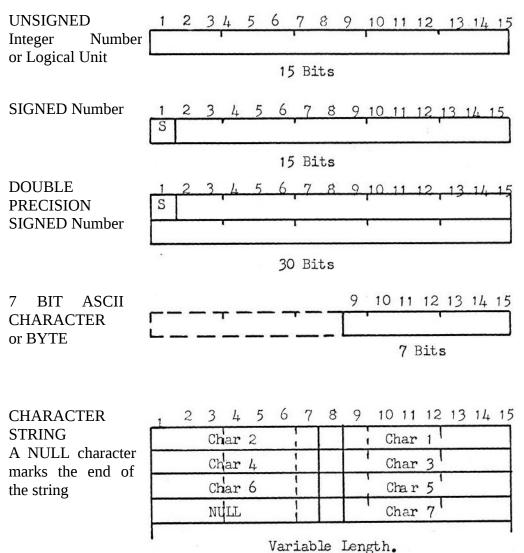
	OP CO.	DE	@		MEMORY RE	FERENCE	
JMP JMS JZR JNR	0 0 0 0	0 2 4 6					ADR JEQ JNE
JZC JNC JEZ JBN	1 1 1	0 2 46					JLT JGE JLE JGT
AND ADD SUB CMP	2 2 2 2	0 2 4 6					
LDA STA CLR TST	3 3 3 3	0 2 4 6					
COM NEG INC DEC	4 4 4 4	0 2 4 6	1				
ROL ROR ASR SWP	5 5 5 5	0 2 4 6					
KDN KDD KCH KCS	6 6 6	0 2 4 6			 		
PDN PDD PCH PRF	7 7 7 7	0 2 4 6		7			TDN TDD TCH TCS.
	1 2 3	4 5	6	7 8 9	10 11 12	13 14 15	

Table 1

Each 15 bit binary word can be expressed as a 5 digit OCTAL number. For instructions the first two digits are the OP CODE, which is written in assembler code as a three upper case letter mnemonic shown in the left hand column. A 1 is added to the second digit if MR is indirect (@). The Memory Reference is the remaining 3 OCTAL digits. Some op codes have alternate mnemonics useful for **unsigned** numerical comparisons with the CMP instruction.

```
CMP dest
JLT .+2 ; jump to .+2 if ACC < contents of location dest</pre>
```

2.3.3 Data Formats



Other Data formats can be devised and these are only limited by the programmers ingenuity.

2.4 HISTORY

The Balad system was developed in 1970 as an aid for teaching electronics technicians and their teachers the basics of how a computer works internally. Even at that time the instruction sets and the multitude of special registers were confusing the fundamental simplicity of a computer based on the original *von Neumann* architecture.

This is a much greater problem in the 21st century, with CPU's with very extended instructions sets and a much greater reliance on higher level languages, which hide what is happening inside the computer. This very simple BALAD virtual computer should give students some insights into how the very core of a computer functions. The details can easily be taught in one 45 minute lesson and from then on students can test their own skills in manipulating machine instructions to develop higher level functionality, like a multiply routine, which is not part of the basic instructions set. HINT: a very simple multiply algorithm is to add the *multiplicand* to the accumulator and decrement the *multiplier* in a loop. Terminate the loop when the *multiplier* is zero.

3 THE BALAD ASSEMBLER

The BALAD assembler is always executed first in two pass mode when BALAD is called with one or more source file arguments. Two pass mode means that the source(s) are read once to identify all symbolic labels followed by a colon (:), which builds a Symbol Table. Then the files are read a second time and all instructions, numeric data and strings are converted into 15 bit machine code and stored in the correct memory locations, ready to run. Any errors in the program are reported on the console and in an optional listing file. If there are errors or the call is made with the -c option the file(s) are only assembled. Otherwise the assembled program is started at main: if there is a label main – else the debugger is entered to allow starting the program manually with the r command.

```
balad george.bl
```

Linux and Unix operating systems allow automatic starting of a BALAD program when the following line is the first line of a program:

```
#!/usr/bin/balad
```

The file location /usr/bin/balad must contain the BALAD executable or a link to it. For this to work your BALAD application source must first be made executable with:

```
chmod +x george.bl
```

Then the following simple call will assemble and start the program automatically without mentioning balad:

```
george.bl
```

Any listing, help or debugging switches can follow that direct call.

3.1.1 BALAD Help

When BALAD is called with the **-h** option a Usage help output on the console describes all the command line switches and file parameters. This is followed by a detailed description of the Debugger commands.

The user can also add his own help output to a BALAD program by terminating the normal code and data with a line starting with ___END___. Any text following this terminator is interpreted as a help text, which can be displayed on the console with the BALAD call of the program followed by the -h switch. The following program has such a help text:

3.1.2 Interactive Input Mode

If BALAD is called without any parameters at all, *interactive input mode* is entered, which allows direct entry of BALAD labels, instructions and data from the keyboard. Each line is assembled as soon as the Enter key is typed. This is a quick way to try out a short program. This program entry is

terminated with **q** on a line by itself, which causes entry into the debugger from where the newly entered program can be run. Care must be taken to terminate code with an unconditional **JMP** or a **HLT** instruction before entering data, going to a new memory location with **LOC** or **BLK** or quitting interactive entry with **q**. Not doing so causes an Error message. *Interactive input mode* can also be entered from the debugger with the **e** command. This make it possible to make changes to existing code or enter extra code while debugging, if the semantics of the program are not correct. The debugger also allows single memory locations to be modified directly with the **<** command.

A program entered in *interactive mode* can be output to a file from the debugger with the O <file> command. If the <file> chosen already exists you will be asked if you want to overwrite it. You can also create a list file from the debugger with the L <file> command. *Interactive mode* is a quick and easy way for students to try their hand with BALAD code, without having to learn entering code in a text editor. It was the only way that was available with the original 1970's BALAD version, which had a teleprinter as a terminal on a Data General NOVA minicomputer. Programs could only be printed and saved on paper tape at 10 character/second – there was no disc.

3.1.3 Listing Options

Calling BALAD or a BALAD application with the **-l** switch will produce a complete listing of the program. Each line of the program which generates a value for a memory location will be preceded by the 3 digit octal address of that memory location and the 5 digit octal contents generated for that location. The listing of the main part of the program george.bl starts as follows:

```
balad -1 george,bl
                 LOC 100
 100
    30023
           main:
                 LDA stackA
                             ; top of stack - clear the stack
 101 32014
                 STA stackP
                             ; stack grows downwards towards 'expr'
           # Get a new RPN expression string
           102
     66700 loop: KCS expr
                            ; grow expression upwards towards stack
                 LDA expADR ; expr[] address
 103
     30022
                           ; word pointer first
                 STA expPTR
JMS iniDig
 104
     32013
                             ; clear digits, hexFl -1, decimal base, C
 105
     02373
                             ; skip first ROR - start with even byte of expr[0]
                 JMP .+2
```

The listing output is useful for debugging. It correlates with the tracing output at break points and normal tracing.

The listing can also be stored in a file specified with the -L switch. Normally a listing_file> name follows the -L switch. If no listing_file> is specified the base name of the <source_file> with the extension .bll is used. The -L switch should be put at the end of the command line, because if it is put just before the <source_file> name that is assumed to be the listing file. The -- switch before the <source_file> marks the end of all switches and fixes this also. The following calls are all equivalent:

```
balad -1 george.bl -L
balad -1 george.bl -L george.bll
balad -1 -L george.bll george.bl
balad -1 -L -- george.bl
```

A listing file can also be generated from the debugger with the **L <file>** command.

4 THE BALAD DEBUGGER

The debugger is an integral part of the BALAD system. which is invoked with one of five command line switches, either alone or in combination. The **-o** switch starts the debugger in *octal data tracing mode*. The normal debugger prompt is the current octal debugger location followed by **100** >>

```
balad -t george.bl
100 >>
```

The debugger can be in one of three modes with different prompts and individual commands:

```
    program is not running
    is stopped at a break point
    is stopped at a watch point
    is stopped at a watch point
    in s u c or a command allowed
    n s u c or a command allowed
```

The following additional commands work in all modes:

```
output the source text to STDOUT
O <file>
          output the source text to <file>
         output the listing text to STDOUT
L
L <file>
         output the listing text to <file>
         output the Symbol Table
         output the application Help text if any
          output the BALAD debugger help text
          QUIT balad
         set a BREAK or watch point at current location
         set a BREAK or watch point at location <n>
<n>*
<n>,<m>* set BREAK or watch points at locations <n> to <m>
          CLEAR all break or watch points
#
.#
         CLEAR a break or watch point at current location
<n>#
         CLEAR a break or watch point at location <n>
<n>,<m># CLEAR break or watch points at locations <n> to <m>
          list all break or watch points
<n>,<m>= list break or watch points in range <n> to <m>
< <code> assemble <code> or <data> at current location
<n> < <code> assemble <code> or <data> at location <n>
              this allows the modification of single locations
    List commands show an octal memory address and the contents
/c
         list current location as code
         list location <n> as code
<n>,<m>/c list locations <n> to <m> as code
    Similarly for different list modes
/d
     short signed decimal /D
                                      long signed decimal
                                /υ
/u
     short unsigned decimal
                                      long unsigned decimal
     short unsigned octal
                               /0
                                      long unsigned octal
/0
     short unsigned hexadecimal /X
                                      long unsigned hexadecimal
/x
                             /B
/b
     short unsigned binary
                                      long unsigned binary
     text string up to next NULL
    these apply to all other commands starting at * (set a BREAK)
             list location(s) in current list mode
     trace code during execution.
  -d additionally trace C, ACC and MR in decimal
  -o alternatively trace C, ACC and MR in octal
  -x alternatively trace C, ACC and MR in hexadecimal
  -b alternatively trace C, ACC and MR in binary
     In each case trace values before and after execution.
     Without -t trace only at break or watch points.
     stop tracing code and data during execution.
```

Memory addresses shown as <n> or <m> above can be entered in a number of ways:

- An octal number. The BALAD memory is only 512 words long, which makes 0-777 the only valid addresses.
- A defined symbolic address followed by an optional + or decimal offset. If the command following a symbolic address is a letter it must be separated from the address by a space.
- The symbol which stands for the current location followed by an optional + or decimal offset.
- Any of the above preceded by the symbol @, which means the address is the contents of the chosen location.

4.1.1 Running a program

A program is started from the debugger with the r command. Without a preceding address, the program is started at the label main:. If there is no such label the program is started at location 100, which is the default location where code is normally started. But it is safer to start with a specific location preceding the r command in this situation.

```
<u>100 >></u> 155r
```

Specifically start execution at location **155**. The **r** command can only be called when a program has not been running and stopped at a break or watch point.

4.1.2 Instruction Tracing

When a program is run after starting with the **-t** switch, every instruction that is executed is traced by printing the address and then the instruction code as an octal number and as a symbolic assembler instruction.

Other switches which start the debugger are **-to**, **-td**, **-tx** and **-tb** or without the tracing option as **-o**, **-d**, **-x** and **-b**. Adding the **-o** switch, calling the program with **-to** additionally traces the contents of the Carry and Accumulator as well as the Memory Reference address of the current instruction [in square brackets] and the contents of the Memory Reference - all before and after the instruction is executed. Lastly the binary values of the Jump Tester Carry register jC and Result register jR are traced. These are the only output of the **CMP** and **TST** instructions. The values of jC and jR influence subsequent conditional Jump instructions.

```
balad -to george.bl

100 >> r
100 ***** run *****

main: 100 30023 LDA stackA C 0 ACC 00000 [023] 00776 ==> C 0 ACC 00776 [023] 00776 jC 0 jR 1
101 32014 STA stackP C 0 ACC 00776 [014] 00000 ==> C 0 ACC 00776 [014] 00776 jC 0 jR 1
100p: 102 66700 KCS expr C 0 ACC 00776 [700] 00000
```

The example shows how the first instruction LDA stackA loads the stack address 00776 from location [023] into the Accumulator, which was previously 00000 and stores it with the STA stackP instruction in the stack pointer, location [014], which was also previously 00000. Any trace will stop when encountering an input instruction, which is the KCS instruction in this example with the prompt RPN: Entering a value at the prompt and typing Enter will continue the trace.

Note: only the data before the instruction is shown for an input instruction, because the instruction has not been fully executed yet. The trace data after execution is shown after typing Enter.

When tracing instructions in an arithmetic algorithm the contents of the Accumulator and the memory reference can be shown as decimal numbers with the **-td** switch. For completeness these contents can also be traced in hexadecimal with the **-tx** switch and binary with the **-tb** switch. The tracing modes can be changed from within the debugger using the same mnemonics **-to**, **-td**, **-tx** and **-tb**. In the debugger the mnemonic - switches tracing off altogether. The tracing modes **-o**, **-d**, **-x** and **-b** only output trace data just before and just after the occurrence of a **break point** or **watch point**, which will be covered next.

4.1.3 Break Points

Locations in a block of program code can be marked as a breakpoint. For this debugger any number of breakpoints can be set. Breakpoints are set with the * command. The following sets the current location 100 as a breakpoint:

```
100 >> *
100 * 30023 main: LDA stackA
100 >>
```

Setting the breakpoint echoes the listing line of that instruction with a * symbol after the memory address to show that a breakpoint has been set at that location. All subsequent listings will show that star until the breakpoint has been cleared with the # command, which will clear all breakpoints:

```
100 >> #
100 30023 main: LDA stackA
100 >>
```

A list of all breakpoints can be output with the = command. Most debugger commands can be preceded by an address or a range of addresses. The following sets breakpoints on 2 consecutive locations:

```
100 >> 103,104*

103 * 30022 LDA expADR

104 * 32013 STA expPTR

100 >>
```

Ranges are two addresses separated by a comma. The example shows the use of octal addresses but symbolic addresses can also be used. One gets pretty used to octal addresses, which are available from any listing.

Breakpoints come into play when a program is executed. When the instruction at location **103**, marked as a breakpoint, is about to be executed the instruction and trace data (if one of the data trace switches -o -d -x or -b is set) is output followed by the prompt **103** B>

```
100 >> r

RPN: 5 6 +

103 30022 LDA expADR C 0 ACC 00776 [022] 00700

103 B>
```

This shows that we are about to execute the LDA expadre instruction at location 103 with the value 00700 in location [022]. The most common command at a breakpoint is to **continue** execution to the next breakpoint, which is the **c** command:

```
103 B> c ==> C 0 ACC 00700 [022] 00700 jC 0 jR 1
104 32013 STA expPTR C 0 ACC 00700 [013] 01601
104 B>
```

The first output after the c command is the trace values after execution of the just completed breakpoint instruction. That shows that the value 00700 from location [022] has indeed been loaded into the Accumulator. The next breakpoint is at location 104, which again shows the appropriate trace information before executing that instruction. If no breakpoint had been set at location 104, the same effect would have been achieved with the **step** command s, which causes a break at the

very next instruction, even if that instruction steps into a subroutine. Alternatively the **n** command breaks at the **next** instruction, but will step over subroutine calls – treating the **JMS** instruction as if it were just one machine instruction. Once inside a subroutine, the **u** command will continue execution in that subroutine **until** it leaves that subroutine. The **abort** command **a** will take the system from a breakpoint to the *not running* state with the >> prompt, effectively stopping the program and returning to normal debug mode.

4.1.4 Watch Points

Watchpoints are very similar to breakpoints, but their operation during execution of a program is slightly different. Watchpoints are also set with the * command, but instead of marking an instruction, a data location is marked. Such a data location is normally not executed as an instruction, which means it is not a breakpoint. Instead data locations are read and sometimes modified by different instructions. Each time this happens for data at a watchpoint location (marked by a *) a trace line for the instruction referencing that data is output with the word *watch* appended. When the data is actually modified, execution of the program stops and the debugger is re-entered with the watchpoint prompt 502 B>. The address shown is the address of the instruction whose memory reference location is being watched. Unlike with a breakpoint, the instruction must be fully executed before it can be determined that a modification of the data has occurred. The following example shows a watchpoint in operation on a variable sign:

For the first two instructions at 502 and 505 the value at sign [012] has not changed. The INC sign instruction at location 507 does change sign from 00000 to 00001, thus causing a watchpoint break. Intermediate instructions operating on other memory reference locations are not traced unless in full tracing mode with the -t switch.

This particular watchpoint on the variable sign allowed me to find a subtle bug during the development of the *Reverse Polish Notation Calculator* GEORGE. sign is used in four different subroutines add, sub, mul and div, which execute the arithmetic operations in the calculator. sign is used to adjust the result of these double precision operations. I had forgotten that I also called double precision sub in the div routine. This led to the value of sign for the div result being altered by the embedded call to sub, leading to erroneous results. The use of a watchpoint on sign showed the change in sign in the routine sub during the execution of div very clearly.

To continue from a watchpoint the same commands **n s u** or **c** as for a breakpoint are used.

The way breakpoints and watchpoints work in BALAD is similar to their functionality in other assembler and higher level language Debuggers and *Integrated Development Environments*. In particular these other Debuggers all use the letters **n**, **s**, **c** and **u** as keyboard accelerators for the **next**, **step**, **continue** and **until** operations. Thus learning to debug simple programs or algorithms in BALAD should be a good learning experience for using Debuggers with other language systems. The main skill in debugging is seeing how variables vary by setting appropriate breakpoints and interpreting the values in the accumulator and the instruction memory reference locations. Other locations can be viewed at any time in different list modes, which will be discussed next.

4.1.5 Listing or viewing memory locations

Memory locations or groups of memory locations in any computer are fixed length bytes or words, which are identified by an address. In BALAD the word length is 15 bits. The interpretation of memory words depends on which part of the computer is accessing a particular memory location. There are three main ways of interpreting computer memory and a number of sub-categories:

- 1. Instructions. In BALAD these are very regular consisting of a three upper-case letter opcode followed by an optional '@' symbol and then an octal or symbolic memory reference.
- 2. Numbers. These may be single-precision 15 bit integers or 30 bit double-precision integers. BALAD instructions can only work directly on single-precision numbers, but many function algorithms deal with double-precision numbers, which makes it useful to be able to list pairs of memory locations as double-precision numbers while debugging. Numbers may be interpreted as signed or unsigned. The '-' can only be displayed with a decimal output. Numbers can also be displayed as octal numbers, which are identified by a leading '0', hexadecimal numbers with a leading '0x' and binary numbers with a leading '0b'. All octal, hexadecimal and binary numbers are displayed as unsigned. If signed the first bit of these numbers is the sign bit. Other computers also have floating point numbers, which are not supported by BALAD. In principle a group of functions to carry out floating point arithmetic is feasible, but the amount of memory available is not sufficient to do it. So the debugger does not support them either.
- 3. Strings. In BALAD strings are stored two 7 bit ASCII characters per word, terminated by a zero or NULL byte. Thus strings are variable length data structures.

The debugger command to start a list of one or more memory locations is /. The / is optionally preceded by a memory address (octal, symbolic or relative). The / is followed by a single letter list mode, which determines how this location or group is to be interpreted:

```
/c
      list current location as code
/d
      single-precision or short signed decimal
/u
      single-precision or short unsigned decimal
/0
      single-precision or short unsigned octal
/x
      single-precision or short unsigned hexadecimal
/b
      single-precision or short unsigned binary
/D
      double-precision or long signed decimal
/υ
      double-precision or long unsigned decimal
/0
      double-precision or long unsigned octal
/x
      double-precision or long unsigned hexadecimal
      double-precision or long unsigned binary
/B
/s
      text string up to next NULL
```

A subsequent / command or an Enter without a command optionally preceded by an address or address range will list memory locations in the most recently used list mode.

```
<u>100 >></u> main,loop /c
 100
       30023
               main:
                        LDA stackA
 101
        32014
                        STA stackP
 102
      66700 loop:
                       KCS expr
<u>103 >></u> /
 103
      30022
                        LDA expADR
104 >>
```

Here we inspect the contents of stackP, which is a memory address where double precision numbers are stored in the GEORGE RPN calculator:

```
        776
        >>
        stackP/o

        014
        00774
        stackP:
        0774

        015
        >>
        @stackP/O
        025004000

        774
        04000
        025004000

        776
        >>
        @stackP/D

        774
        04000
        5507072

        775
        00250

        776
        >>
```

The @stackP address uses the contents of stackP as the location to display the two word octal number. The next display shows the number as a decimal. As with all listing modes the 5 digit octal memory value for each word is shown also. Any labels are also shown.

4.1.6 Modifying memory locations

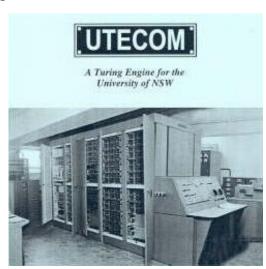
An important aspect of debugging is being able to modify the contents of memory locations, either before a program is run or at a break or watch point. The debugger command to do this is <. Any text after the < command is passed to the assembler to interpret and convert to correct binary value(s) to store in the memory location preceding the < command. That location may be the current location if no new address is typed, an octal or symbolic address or a range, which will all be modified with the same value. Values passed may be BALAD instructions if modifying code, numerical short or long numbers (double precision numbers have a trailing l or L) in any of the input bases – decimal, octal, hexadecimal or binary. Finally a number of locations can be modified by supplying a "string". The first line of output shown after the < command is a listing of the previous contents, which is followed by the assembly line of the new contents. No listing mode letter may follow a < command. The temporary listing mode is determined by the type of value to be assembled – code, number or string.

```
111 >> 103<LDA expPTR
 103
        30022
                        LDA expADR
 103
        30013
                LDA expPTR
104 >> 770<55
 770
       00041
                             33
        00067
                55
 770
771 >> 772<1234567L
 772
        00041
                           1081377L
 773
        00041
 772
        53207
                12345671
 773
        00045
774 >> 720<"Hello world\n"
 720
        00000
  720
        62510
                "Hello world\n"
 721
        66154
  722
        20157
 723
        67567
  724
        66162
 725
        05144
  726
727 >>
```

5 "GEORGE" a Reverse Polish Notation Calculator

To show the power of the BALAD computer, I developed the program *GEORGE* (*george.bl*), which is a complete implementation of a Reverse Polish Notation (RPN) Calculator for double precision integer arithmetic (30 bit precision). I did this with two aims in mind:

- 1. To demonstrate what can be done with a minimal Turing complete instruction set computer and a limited memory of 512 words (1024 bytes). Most of the demonstration programs I have supplied are toy programs to demonstrate various aspects of the instruction set. *george.bl* is a full application with many of the capabilities of the calculator *dc* developed for early UNIX systems and still available in Linux systems (*dc* is a reverse-polish desk calculator which supports unlimited precision arithmetic). Other well known RPN calculators are the *HP-42S* RPN Scientific calculator introduced in 1988 and the *PCalc* calculator available on iPads and other mobile devices, which has an RPN mode. The main limitation of *george.bl* compared with these systems is the lack of floating point arithmetic and the ability to use named variables. Only the lack of memory stops one adding these capabilities.
- 2. To show to 21st century students how computer languages developed in the early days of computing and the importance of the stack concept in computer languages. *Charles Leonard Hamblin* was professor of philosophy at the NSW University of Technology, which later became the University of NSW from 1955. Among his most well-known achievements in
 - the area of computer science was the introduction (some sources also say invention) of the Reverse Polish Notation and the invention of the stack in computing. This was arguably independent of and about the same time as the work of Friedrich Ludwig Bauer and Klaus Samelson on the invention of the push-pop stack. In the second half of the 1950s, he became active with UTECOM, the third computer available in Australia, which was a DEUCE computer produced by the English Electric company. DEUCE was based on the ACE computer which Alan Turing had designed. For UTECOM Charles Hamblin sketched one of the first programming languages, GEORGE, which was based on Reverse Polish Notation, including the associated compiler (language translator),



which translated the programs formulated in GEORGE into the machine language of the computer. In 1957 the GEORGE compiler was operational and I had the pleasure of attending *Charles Hamblins* philosophy lectures during the early part of my Electrical Engineering studies at UNSW. He explained the workings of GEORGE to us and the use of Reverse Polish Notation. I wrote my first computer program in this language and had it run on this very large machine. An incidental memory I have of that computer run was being allowed to take a pocket full of vacuum tubes out of a bucket – they had been discarded as being below specs. I used them to make radios at the time.

About a year later *Friedrich Ludwig Bauer*, *Klaus Samelson* and *Peter Naur* specified the computer language *ALGOL58*, which also used push pull stacks for variable manipulation and subroutine nesting – a strategy which has been maintained via *PASCAL* and *C* through to all modern computer languages.

Here are some extracts from the original GEORGE <u>Programming and Operation Manual</u>.

GEORGE, or the General Order Generator, is a program for DEUCE permitting mathematical problems to be presented to the machine in a simple "addressless" instruction language, here called "G-Code". To use this code the programmer must learn a special method of writing

mathematical formulae, known as "reverse Polish" notation. Once this is mastered, however, programming is considerably easier and quicker than by other methods. "G-Code" is a highly simplified and condensed instruction language. The program in G-Code in fact resembles a mathematical formula for the result required more than it does an orthodox machine program. In particular, the programmer never has to specify any "addresses" for numbers or instructions inside the machine.

As written, a program in G-Code is a sequence of mathematical <u>symbols</u> such as numerals, variables and arithmetical and other special signs; the symbols are transcribed to cards in a numerical code (on today's computers a program is stored in a file in ASCII code – which is also a numerical code). Broadly, each symbol may be regarded as an individual "instruction" of the program.

5.1 PROGRAMMING GEORGE

5.1.1 Reverse Polish Notation

The majority of the symbols used in programming are those normally used in mathematics, but the <u>order</u> in which they occur is different from the usual order: formulae are written in "reverse Polish" notation. This notation has a number of advantages which fit it for use with machine computation.

In this preliminary description let us take for granted that we can use the letters "a", "b", "c", … as ordinary algebraic variables. A mathematical formula is a prescription for operating on the numbers such variables represent.

IMPORTANT NOTE for the BALAD implementation *george.bl*: variables in formulae have not been implemented because of lack of memory. Integer numbers are put directly into the formulae, which are then executed just like the 1957 version of GEORGE.

We can classify the operators involved as:

- i. monadic operators, or operators on a single number, such as the minus-sign in "-a".
- ii. <u>diadic</u> operators, or operators on a pair of numbers, such as the operators for addition, subtraction, multiplication and division.

In ordinary mathematical notation, a monadic operator is most frequently written <u>in front</u> of the number concerned, as in "-5", and a diadic operator <u>between</u> two numbers, as in "7 + 9". Because the sign "-" is used indifferently for subtraction and as a minus-sign (subtraction from zero), brackets are needed to distinguish, say, "-4 + 6" and "- (4 + 6)".

In reverse Polish notation the operator-signs, whether monadic or diadic, are written after the numbers concerned, as follows:

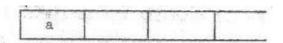
For	7 + 9	write	7 9 +
"	7 - 9	II .	7 9 -
"	7 * 9	II .	7 9 *
II .	774 / 9	II .	774 9 /
II .	- 5	II .	5 n and so on.

One result of this is that brackets are never needed: any of the above expressions may be used directly and without ambiguity as an element in a longer expression. For example:

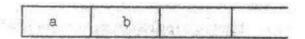
For	- (7 + 9)	write		7 9 + n
"	7 + 9 + 15	"		7 9 + 15 +
			or	7 9 15 + +
"	(7 + 9) * 15	"		7 9 + 15 *
"	7 + 9*15	"		7 9 15 * +
<i>II</i>	7*9 + 15/3	II .		7 9 * 15 3 / +

In understanding the use of this notation in GEORGE it will be of assistance to have in mind a picture of the internal logic of operation. The pseudo-machine into which DEUCE (BALAD in our case) is converted by the basic GEORGE program can be envisaged as equipped with a "running stack": this is a set of storage locations (known as "cells") arranged in linear order and operated on the "last-in-first-out" principle. When a number occurs in a program, its "value", as a binary number, is placed in the first vacant cell of the stack, i.e. in cell 1 if this does not already contain a number, otherwise in cell 2 etc.: and when an operator-symbol occurs, the specified operation is carried out on the contents of the <u>last occupied cell</u> or the <u>last two occupied cells</u>, depending on whether the operator is monadic or diadic. The operation of the formula "a b +" may for example be pictured as follows: (I am using variables "a" "b" "c" of the original GEORGE handbook, which have to be numbers for the BALAD version *george.bl*)

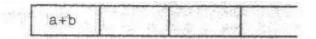
i. "a": number is transferred to cell 1.



ii. "b": number is transferred to cell 2.

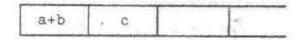


iii. "+" contents of last two occupied cells added together; cells cleared and result replaced.



The result is exactly the same as if a single number, the sum of $\bf a$ and $\bf b$, had been specified. In consequence, this number is available for further operations if required. For example to calculate "($\bf a + \bf b$) * $\bf c$ " we can write " $\bf a \, b + \bf c$ *". The first three steps are as above, after which:

iv. "c": number c is transferred to cell 2.



v. "*": contents of last two cells multiplied; cells cleared and result replaced.

(a+b)xc	
And the second district of the second distric	The state of the s

Alternatively this calculation could have been carried out in the form "c a b + *". In this case three cells would first have been filled with numbers before any calculations were carried out: the result of the addition would go into cell 2, and the final result as before into cell 1.

Quite generally, the overall effect of any calculation of a number is to place the number concerned in the first vacant cell of the stack.

5.1.2 Other Operators

There are two special operators which, although not strictly necessary, are frequently useful:

i. <u>"dup"</u> this "duplicates" the contents of the last cell of the stack in the next cell. In *george.bl* duplication is executed by "E" the Enter operation in conformity with HP-42S and PCalc.

```
For (a + b)^2 write a b + dup * or for george.bl 9 7 + E *
```

ii. "rev" this "reverses" (i.e. interchanges) the contents of the last two occupied cells. In *george.bl* "rev" is executed by "S" for Swap in conformity with HP-42S and PCalc.

```
For a + b + c / (a + b) write a b + dup c rev / + or for george.bl 9 7 + E 100 S / +
```

- iii. "n" is negate in *george.bl* instead of "neg" in GEORGE.
- iv. "(a)" in GEORGE means store the contents of the last cell in variable a. *george.bl* has no variables, hence no such operator.

The following useful stack manipulation operators from HP-42S and PCalc were not available in GEORGE but have been implemented in *george.bl*:

- v. "R" for Roll. Move the last cell on the stack to the first cell of the stack after moving all other cells across one position.
- vi. "D" for Drop. Free the last cell on the stack, making it available for a new number.
- vii. "C" for Clear the whole stack. This allows starting a new set of calculations.

White space, which is a SPACE, a TAB or a CR (enter) character, as well as any other operator (including E) immediately after entry of a new number will push that number on the stack. Only then is the operation executed if it was an operator. After that white space is ignored until a new number is entered and further operators carry out their function on numbers already on the stack.

Numbers in *george.bl* can be input and output in different bases, namely decimal, octal (base 8), hexadecimal (base 16) and binary (base 2). This is a very useful feature for supporting machine level programming to do address arithmetic. Assemblers (including the BALAD assembler) present memory addresses and their contents either in octal or hexadecimal. Binary presentation is useful for bit manipulation. All the calculators which served as a model for *george.bl*, namely *dc*, *HP-42S* and *PCalc* have input and output in the four number bases.

For *george.bl* the format of different base numbers follow the strategy of modern computer languages like *C* and *Perl*:

- A number starting with 1-9 followed by digits 0-9 is decimal.
- A number starting with 0 followed by up to 10 digits 0-7 is octal.
- A number starting with 0x followed by up to 8 digits 0-9 and a-f is hexadecimal.
- A number starting with 0b followed by up to 30 digits 0 and 1 only is binary.

Numbers may only be integers. Therefore no decimal point is allowed. The result of a calculation is shown in decimal at the end of a reverse Polish expression string. Normally there is only one result, but some expression strings leave values on the stack. For this reason the whole of the current stack is output at the end of the expression string. For debugging your reverse Polish expression this information is very useful. Most calculators only show the last value on the stack or at most the last two values. The ability to see the whole stack was a feature I always wanted.

george.bl has four extra operators to output numbers in the different bases. These are \mathbf{d} for decimal, \mathbf{o} for octal, \mathbf{x} for hexadecimal and \mathbf{b} for binary. These operators can be put at the end of an expression, in which case the result will be shown in the requested number base. The operators \mathbf{d} , \mathbf{o} , \mathbf{x} and \mathbf{b} serve a dual purpose. They can also be placed more than once in the middle of a reverse Polish expression. This has the effect that each time one of these display operators occur in the expression the stack, as it is at that point of the expression evaluation, will be output in the requested base. On top of that, if the display operator is not at the end of the expression the remainder of the expression will be output after the stack results. The net result is a tracing feature for debugging more complicated reverse Polish expressions. Let me demonstrate this feature with an example taken from the original GEORGE handbook:

```
To evaluate e = ay^2 + by + c, one wrote a y dup \times b y \times c + c + (e).
For values of a = 15, y = 30, b = 12 and c = 45 the george.bl RPN expression is:
           15 30 E E R * * R 12 * + 45 +
                                                which evaluates as follows:
RPN: 15 30 E E R * * R 12 * + 45 +
 13905
With extra trace output d before every value input and operator the output is as follows:
RPN: 15 d30 dE dE dR d* d* dR d12 d* d+ d45 d+
                30 dE dE dR d* d* dR d12 d* d+ d45 d+
 15
 15 30
                E dE dR d* d* dR d12 d* d+ d45 d+
15 30 30
              E dR d* d* dR d12 d* d+ d45 d+
 15 30 30 30 R d* d* dR d12 d* d+ d45 d+
 30 15 30 30
                * d* dR d12 d* d+ d45 d+
                * dR d12 d* d+ d45 d+
 30 15 900
 30 13500
                R d12 d* d+ d45 d+
 13500 30
                12 d* d+ d45 d+
 13500 30 12
                * d+ d45 d+
 13500 360
                + d45 d+
                45 d+
 13860
 13860 45
 13905
```

A similar effect can of course be achieved by entering every input value and operator on a separate line, but the output is not quite as compact and informative:

RPN: 15 15 RPN: 30

```
15 30
RPN: E
 15 30 30
RPN: E
 15 30 30 30
RPN: R
 30 15 30 30
RPN: *
 30 15 900
RPN: *
 30 13500
RPN: R
 13500 30
RPN: 12
 13500 30 12
RPN: *
 13500 360
RPN: +
 13860
RPN: 45
 13860 45
RPN: +
 13905
```

5.2 Overall strategy of GEORGE

It is important to remember that computers in the 50's like UTECOM were mainly seen as *Number Crunchers* — in other words evaluating numerical formulae. Up till then the word *computer* had been a *job description* for workers, whose job it was to compute numbers for such projects as the dimensions of beams for building sites or statistical projections for businesses using pencil and paper with mechanical calculators as the only aid.

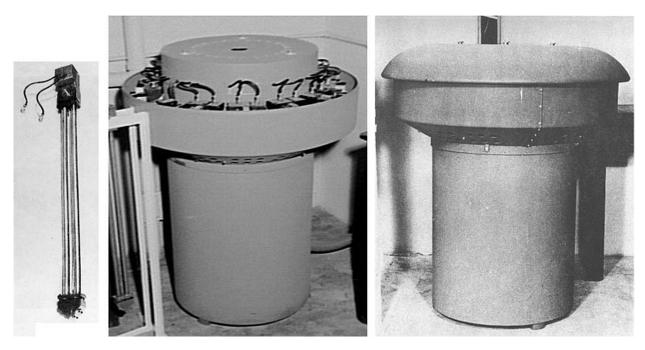
I did such a project with my father, who was a lecturer in Mechanical Engineering at UNSW. He had undertaken to produce a chart for selecting suitable steel tubes from those produced by the company *Tubewrights* in Port Kembla for use as columns for building projects. It was known that long columns fail by buckling. A Swiss mathematician named Leonhard Euler (1707 –1783) was the first to investigate the buckling behavior of slender columns within the elastic limit of the column's material. Euler's equation shows the relationship between the load that causes buckling of a (pinned end) column and the material and stiffness properties of the column. The critical buckling load can be determined by the following equation.

```
\begin{split} P_{\text{critical}} &= \pi^2 E I_{\text{min}}/L^2 \\ \text{where} \\ P_{\text{critical}} &= \text{critical axial load that causes buckling in the column (pounds or kips)} \\ E &= \text{modulus of elasticity of the column material (psi or ksi)} \\ I_{\text{min}} &= \text{smallest moment of inertia of the column cross-section (in}^2) \\ &\qquad \qquad \text{(Most sections have $I_x$ and $I_y$; angles have $I_x$, $I_y$ and $I_z$.)} \\ L &= \text{column length between pinned ends (inches)} \end{split}
```

The chart my father made showed a curved line for each type of tube with load in pounds on the Y axis and length in inches on the X axis. For a tube to be suitable as a column the point of intersection of load and length had to be below the line for that tube on the chart. For each of about 50 types of tube we had to compute 200 points, which meant 10,000 evaluations of Eulers equation. At the time I had just done my exercise with GEORGE on the UTECOM computer. My father tried to get time on UTECOM for his project, but it was rejected. So we worked for a fortnight with a large notebook and a FACIT mechanical calculator to do these computations.



It was not until the 60's that computers started getting away from solely *number crunching*, because now they were byte oriented, which made it much easier to do text manipulation. At the time it was realized that a larger proportion of actual computing time was being spent on manipulating text rather than on crunching numbers. Particularly compilers are very text oriented.



But in 1957 this was not so. UTECOM was a general-purpose vacuum-tube digital computer, with a serial organization and a 1Mhz clock rate. The word size was 32 bits, and the machine's arithmetic units were capable of performing single, double, and mixed-precision binary integer arithmetic. Negative values were held in two's complement form. A hardware unsigned integer multiplier and a signed integer divider were included. Its primary memory consisted of 12 mercury filled delay lines. These were "folded" with quartz crystal transmitter and receiver at the top and a pair of acoustic mirrors at the bottom. Each delay line circulated 32 words of 32 bits each, making a total of 384 words (1536 bytes). Of the 384 words, 256 words (1024 bytes) were used for program memory and 128 words for data memory. This means that the program memory was of similar size as the BALAD memory of 512 x 15 bit words (1024 bytes). UTECOM just had an extra 50% of data memory, which made the storage of variables and other extras possible.

The overall strategy of GEORGE was to use the UTECOM library functions add, subtract, multiply and divide to do the actual arithmetic. But first GEORGE programs, coming in via punched cards, had to be compiled, either directly into machine code, or later into code, which was executed by an interpreter, which was more flexible and allowed calling more functions, like **LOG** and **SINE**.

george.bl uses the latter strategy, which will be looked at in detail in the next section.

5.3 Analysis of the BALAD implementation george.bl

The core of the RPN system are the five subroutines add, sub, mul, div and negate, which carry out signed double-precision integer arithmetic (very similar to the capabilities of UTECOM). The single precision multiply function mult is used to multiply the value of incoming numerical digits to binary by multiplying them by the number base. It is also used to implement the double-precision mul function. These basic functions are supplemented by the functions push and pop, which implement a stack for double-precision numbers. Another stack function is showst, which is called in two places to display the whole stack.

The program is very short on available memory, so manual optimization was undertaken to eliminate any groups of code which were duplicated and replace them with subroutines, which are called instead of duplicated code.

5.3.1 Variables and Constants

LOC 0 and LOC 1 are the accumulator and its extension for double precision values. These locations are pre-defined with the label ACC and ACC+1. The following locations are double-precision variables dest, src and mulcnd initialised with the double-precision constant OL. The variables src, mulcnd and mulplr are shared in a number of different routines for quite different purposes. Great care must be taken when doing this, that the variables can be safely shared. savACC and sign are also shared but the remaining variables carry global states and cannot be shared.

Variables whose contents start with the pseudo-operator ADR hold the address of other locations. **expADR** holds the start of the locations where RPN expressions are stored and **stackA** holds the top of the **stack**. A special case is **funPAd**, which hold the indirect address ADR @funAdr, which points to the array **funAdr** containing the four function pointers **add**, **sub**, **mul** and **div**. The rest are character constants for identifying operators, number constants and character strings.

5.3.2 Main Program

The first thing done in the main program is to initialize the stack. This point is also looped to when executing the Clear instruction "C".

```
100 30020 main:
                    LDA stackA
                                 ; top of stack - clear the stack
  101 32012
                    STA stackP
                                 ; stack grows downwards towards 'expr'
Then we get a new RPN expression string:
  102 66707 loop:
                                 ; grow expression upwards towards stack
                    KCS expr
  103 30017
                                 ; expr[] address
                    LDA expADR
  104 32011
                    STA expPTR
                                 ; word pointer first
  105 02411
                                 ; clear digits, hexFl -1, decimal base, C
                    JMS iniDig
                    JMP gettok+1; skip first ROR - start with even byte
  106 00110
```

We loop to this point every time the execution of the previous RPN expression is finished. The **KCS** instruction reads a character string from the keyboard (or alternatively from a batch file with STDIN). Next the **expPtr** is initialized with the word address of the first character [0] of the

RPN expression. This pointer is later turned into a byte pointer, which is incremented to point to the next character. To do this with the BALAD instruction set the byte pointer is right shifted and if the carry is one, the bytes in the word are swapped with the SWP instruction. The subroutine iniDig (which is called in a number of other places) resets the counter digits, which counts the digits as a number is built from a series of input digits. When digits is zero no new number has been built yet. hexF1 is used in hexadecimal conversion and asBase is set for decimal conversion. Lastly the Carry register C is set to zero. This is important for subsequent additions and subtractions. The initial entry into the gettok loop skips the initial ROR instruction.

The following loop picks up consecutive character tokens for numerical digits, operators and white space:

```
107 52011 gettok: ROR expPTR ; change to word pointer and carry
110 31011
                LDA @expPTR ; two bytes from the expression
111 10113
                 JZC .+2
                             ; skip SWP for even bytes
112 56000
                 SWP ACC
                             ; swap bytes for odd bytes
113 50011
                 ROL expPTR ; change to byte pointer
                 INC expPTR ; increment expression byte pointer
114 44011
115 20062
                 AND C177
                             ; mask to 7 bit character from expression
```

String characters are stored two to a word and the code above picks those up in consecutive order. Finally the word is masked with **AND C177** to leave just the character in the word accumulator for comparisons. Next we check whether the input character is a numerical digit, by comparing with **ASC 0** and **asBase** whose initial value is for decimal conversion.

```
116 26035 CMP ASC_0 ; "0"

117 10173 JLT notDig

120 26016 CMP asBase ; "9"+1, "8", "2", "f"+1

121 12173 JGE notDig
```

If the character lies outside this range it is not a numerical digit and the program jumps to **notDig**. The code up to **num1:** is mostly concerned with setting up octal, hexadecimal or binary conversion, whose workings are left as an exercise for the reader. In each case the variable **inBase** is set to 10, 8, 16, or 2 and temporarily saved in **savACC**.

The actual code to do character string to binary conversion is the following:

```
151 44013 num1:
                 INC digits
                             ; number is growing
152 30015
                            ; 10, 8, 16 or 2
                 LDA inBase
153 32010
                 STA mulplr ; multiplier
154 30002
                 LDA dest
                            ; lo part of previous number
155 32006
                 STA mulcnd ; multiplicand
156 34007
                 CLR mulcnd+1
157 30407
                 LDA savACC ; restore accumulator - new binary digit
160 02462
                 JMS mult
161 32002
                 STA dest
                             ; store lo part of number
162 30015
                 LDA inBase ; 10, 8, 16 or 2
163 32010
                 STA mulplr ; multiplier
164 30003
                 LDA dest+1
165 32006
                 STA mulcnd ; multiplicand
```

```
166 34007 CLR mulcnd+1
167 30001 LDA ACC+1 ; hi part of lo order multiplication
170 02462 JMS mult
171 32003 STA dest+1 ; store hi part of number
172 00107 JMP gettok ; get next digit or next operator
```

A double precision binary number is generated from the next numerical digit by first multiplying the previously built number's low and high part by inBase (usually 10) and then adding the binary value of the new digit. The result is stored in dest and dest+1.

The code from **notDig** to **notNum** checks for **x** or **b** after an initial **0** to detect **0x** or **0b**, the leading markers for identifying hexadecimal or binary numbers.

Then the RPN token in the **ACC** is tested for the operations "**q**", "**C**" or "**E**", which are executed, even if no new number has been pushed on the stack.

```
215 26053 notNum: CMP ASC_q
216 04077
                  JZR errMsg+3; quit the program
217 26041
                  CMP ASC C
                              ; "C"
                  JZR main
220 04100
                              ; Clear the stack
                              ; "E"
221 26043
                  CMP ASC E
222 06227
                  JNR tstNum
                              ; Enter or duplicate number on stack
223 02423
                  JMS push
224 02411
                              ; clear digits, hexFl -1, decimal base, C
                  JMS iniDig
225 34410
                  CLR sign
                              ; show stack after pushing a new number
226 00107
                  JMP gettok
```

For all other operators push a newly built number if a new number has been built. This includes white space, which is otherwise ignored.

```
227 36013 tstNum: TST digits
                              ; has a number been built ?
230 04234
                  JZR noNum
                              ; no - no new number
231 02423
                  JMS push
                              ; yes - push the new number
232 02411
                              ; clear digits, hexFl -1, decimal base, C
                  JMS iniDig
                  CLR sign
233 34410
                              ; show stack after pushing a new number
234 30021 noNum: LDA funPAd ; address of function pointer array funAdr
235 32010
                 STA mulplr
                              ; funAdr[0] add
236 30406
                 LDA savACC
                              ; restore accumulator
237 04400
                 JZR expEnd
                             ; end of expression - show result
                              ; unless just shown with 'd' 'o' 'x' or 'b'
240 26026
                  CMP space
241 04107
                  JZR gettok ; ignore white space
242 26027
                  CMP tab
243 04107
                  JZR gettok
```

Now we come to calling the arithmetic functions add, sub, mul and div, which are the main reason for having a calculator. They have all been designed to have a similar calling strategy namely to pop two values from the stack, the first to the double-precision variable src and the second to the double-precision variable dest. Rather than repeat this for each of the four arithmetic functions, it is done once at execOp. Leading up to this is a short section, which generates the values 0, 1 2 or 3 in the shared variable mulplr depending on whether the current operator is "+", "-", "*" or "/".

```
244 34407
                  CLR sign
                              ; all other tokens force showing the stack
                              ; funAdr[0] add (in mulplr shared)
                              ; "+"
245 26031
                  CMP addOp
246 04260
                  JZR execOp
247 44010
                  INC mulplr
                              ; funAdr[1] sub
                              ; "-"
250 26032
                  CMP subOp
251 04260
                  JZR execOp
252 44010
                  INC mulplr
                              ; funAdr[2] mul
253 26033
                  CMP mulOp
254 04260
                  JZR execOp
255 44010
                  INC mulplr
                             ; funAdr[3] div
256 26034
                  CMP divOp
                              ; "/"
257 06270
                  JNE test n
```

At this point we pop **src** and **dest** and call one of the subroutines **add**, **sub**, **mul** or **div**, namely the one whose pointer is in **mulplr**. The address is a double indirect, which is not often used, but is a very useful feature of the BALAD instructions set. This computed call of a subroutine is similar to *Lambda* functions in Python, which are used in various Python implementations of reverse Polish calculators. *Lambda* functions are called *anonymous* functions in Python, i.e. functions without a name.

```
260 02432 execOp: JMS pop
                               ; popped value to src and src+1
261 30002
                  LDA dest
262 32004
                  STA src
263 30003
                  LDA dest+1
264 32005
                  STA src+1
                               ; popped value is in dest and dest+1
265 02432
                  JMS pop
                  JMS @mulplr ; execute the selected op add sub mul div
266 03010
267 00274
                  JMP pushDs
                               ; push result from dest and dest+1
```

The final arithmetic function is negate, which has only one parameter **dest** popped from the stack. All five arithmetic functions return their double-precision result in **dest** and **dest+1**, which is pushed back on the stack.

; "n"

270 26046 test n: CMP ASC n

```
271 06276
                   JNE test D
 272 02432
                               ; n negate last value on the stack
                   JMS pop
 273 02503
                   JMS negate
                               ; DP negate destination
 274 02422 pushDs: JMS push
                               ; push result from dest and dest+1
 275 00107
                   JMP gettok
                               ; next token
Three stack manipulation operations follow.
 ; "D"
 277 06302
                   JNE test S
 300 02432
                   JMS pop
                               ; Drop last value on the stack
 301 00107
                   JMP gettok
 302 26045 test_S: CMP ASC_S
                               ; "S"
 303 06307
                  JNE test R
 304 30012
                   LDA stackP
                               ; Swap last two numbers on the stack
                   ADD D4
 305 22057
 306 00312
                   JMP swpNow
                               ; "R"
 307 26044 test_R: CMP ASC_R
 310 06343
                   JNE test d
  311 30020
                   LDA stackA
                               ; Roll last number on stack with top of stack
```

Drop simply pops the last number on the stack. This is equivalent to clearing the last number entry.

Swap and Roll share a common execution strategy. The only difference is the value in the accumulator, which is four words back from the contents of the current stack pointer stackP for Swap and the top of the stack stackA for Roll.

```
312 32010 swpNow: STA mulplr
                              ; shared
313 30012
                 LDA stackP
314 32406
                 STA savACC
                             ; save stack pointer
315 02432
                 JMS pop
                             ; last number on the stack (checks empty stack)
316 30012
                 LDA stackP
                             ; last number now in 'dest'
317 26020
                 CMP stackA
320 10323
                 JLT swp1
321 76074
                 PRF errMsg
                             ; "? err\n"
322 00337
                 JMP swp2
                              ; restore stack
323 32004 swp1:
                 STA src
                             : shared
324 24056
                 SUB D2
325 32006
                 STA mulcnd ; shared
326 30010
                 LDA mulplr
327 32012
                 STA stackP
330 31004 swpLp: LDA @src
                              ; move numbers down on the stack
331 44004
                 INC src
332 33006
                 STA @mulcnd
333 44006
                 INC mulcnd
334 30004
                 LDA src
335 26012
                 CMP stackP
                              ; until top for swap or roll is reached
336 10330
                 JLT swpLp
337 02422 swp2:
                 JMS push
                              ; push last number further up the stack
340 30406
                 LDA savACC
341 32012
                 STA stackP
                              ; restore stack pointer
342 00107
                 JMP gettok
```

Next we deal with the four debugging operators "d", "o", "x" and "b", which show intermediate results on the stack in either decimal, octal, hexadecimal or binary. First select the number base.

```
343 26047 test d: CMP ASC d
                               ; "d"
                                        decimal
344 04353
                  JEQ show
345 26050
                  CMP ASC o
                               ; "0"
                                        octal
346 04353
                  JEQ show
347 26051
                  CMP ASC x
                               ; "x"
                                        hexadecimal
350 04353
                  JEQ show
351 26052
                  CMP ASC b
                               ; "b"
                                        binary
352 06375
                  JNE inpErr
```

This is followed by the common **show** code, which uses the characters "d", "o", "x" and "b" in the accumulator to modify the format string **fmtDP** to **"** %#1d**"**, **"** %#1o", **"** %#1x" and **"** %#1b" for the **PRF fmtDP** formatted print call in the function '**showSt**, which is also called for decimal output when the RPN expression ends to show the result of an expression.

```
353 02447 show: JMS showSt ; " %#ld" " %#lo" " %#lx" " %#lb"
```

This is followed by the remainder of the RPN expression at that point, which is a useful tracing feature, when debugging a complex RPN expression.

```
354 74027
                 PCH tab
                             ; "\t" show remainder of RPN expression
355 74027
                 PCH tab
                             ; "\t" separated by a wide space
356 30011
                 LDA expPTR
357 32010
                 STA mulplr
                             ; shared
360 52010
                 ROR mulplr
361 31010
                 LDA @mulplr ; two bytes from the expression
                             ; skip SWP ACC ... CLR C for even bytes
362 10371
                 JZC show1
363 56000
                 SWP ACC
                             ; swap bytes for odd bytes
364 20062
                 AND C177
365 04372
                 JZR show2
                             ; terminates on 2nd byte
366 44010
                 INC mulplr
367 74000
                 PCH ACC
                             ; print first odd byte of rest of expression
370 34777
                 CLR C
371 77010 show1: PRF @mulplr ; print rest of expression
372 44407 show2: INC sign
                             ; no need to show stack again if terminated now
373 74030
                PCH nl
                             ; "\n"
374 00107
                 JMP gettok
```

Any other character token in the RPN expression is not recognized and produces a short but informative error message.

```
375 76071 inpErr: PRF inpEms ; "? %c\n"
376 00000 ADR ACC ; token is character in the accumulator
377 00107 JMP gettok
```

Finally the **expEnd** code, which is executed when the **NULL** terminator of the RPN expression is detected near **noNum** above.

```
400 36407 expEnd: TST sign
                             ; was output shown already
401 06102
                 JNR loop
                             ; yes - don't show again
402 30047
                 LDA ASC_d
                             ; no - restore decimal output
                             ; " %#1d"
403 02447
                 JMS showSt
                 PCH nl
404 74030
                              ; "\n"
405 00102
                 JMP loop
                              ; get new RPN expression
```

This code is skipped, if the variable **sign** was set at **show2** above, which means the stack has just been shown already with no RPN expression remaining. Otherwise the display base is set to decimal and **JMS showSt** is called. The program then returns to **loop** to request a new RPN expression. This is the end of the main program.

5.3.3 Subroutines

The subroutines are relatively short and self-contained with hopefully informative comments. The **pop** function checks, that no attempt is made to pop a number when the stack is empty. If the stack is empty an error message is printed and a **JMP loop** is executed to request a new RPN expression. Such a direct **JMP** out of a subroutine is allowed in BALAD because nested subroutine returns are not organized on a stack like in most modern languages. The **JMP loop** out of the subroutine **pop** is similar to a **longjmp** in the *C* language.

Extra code at the beginning and end of each of the four arithmetic routines add, sub, mul and div make sure the result is correct for signed integers. Arithmetic overflow for add and sub as well as divide by zero are flagged as errors. There was not enough memory to detect arithmetic overflow for mul. Also because of lack of memory the division algorithm is very simple and very slow. For the same reason there is no modulo division operator. For div the double-precision divisor is

subtracted from the double-precision dividend until it reaches zero. The number of subtractions are counted and that is the quotient. Division of 536,000,000 by 1 takes over an hour. For more reasonable numbers and larger divisors it works well with division times in the range of milliseconds to a few seconds. But divisions are correct making this a useful calculator.

5.3.4 Help text

As mentioned in section <u>3.1.1</u>. the BALAD system makes it possible to extend the program code with a help text, which is output with the -h switch as follows:

```
george.bl -h
Reverse Polish Notation Calculator 'GEORGE'
              Enter a number terminated by white space or an operator,
              at which point the number is pushed on the stack.
      0 - 7
              A number starting with 0 is octal (0-7 only).
      0-7 a-f A number starting with 0x is hexadecimal (0-9a-f).
              A number starting with 0b is binary (0-1 only).
      + - * / Arithmetic operators which act on the last two numbers
              popped from the stack. Result is pushed back on the stack.
              Error if there are less than two values on the stack.
              NEGATE the last number on the stack.
      n
      Enter
              display numbers on the stack as signed decimal.
      đ
              display numbers on the stack as signed decimal numbers
             before any further operations.
      oxb
              display numbers on the stack in octal, hexadecimal or
              binary notation before any further operations.
              ENTER a number on the stack if 'E' immediately follows
      E
              a number; else duplicate the last number on the stack.
              DROP the last number on the stack.
     ח
      S
              SWAP the last two numbers on the stack.
      R
              ROLL the stack - move last number to the top of the stack.
      C.
              CLEAR the stack.
              QUIT the RPN calculator.
```

5.3.5 BALAD on Windows 10

BALAD is a *Perl* program and to run BALAD on Windows, you need to install either *Strawberry Perl* or *Active State Perl* from https://www.perl.org/get.html. BALAD works with both, although I prefer *Active State Perl*, because it provides a more UNIX like environment. BALAD runs as a command line program in a Command window. Both systems initially produce the following error message: *Unable to get terminal size*. To fix that, execute the following once:

```
set TERM=dumb
```

Windows makes no provision to start interpreted scripts automatically from a Command window. For that reason all BALAD programs must be called as follows eg. for george.bl:

```
perl balad <flags> george.bl
```

6 FINALLY

Best of luck with trying out some of your own algorithms using either your favourite editor or *interactive entry mode*. This handbook should provide enough information to do serious programs. Any suggestions or bug reports are very welcome. Please contact me – John Wulff – on:

```
immediatec@gmail.com with the Subject: BALAD ...
```

The complete BALAD system can be cloned from https://github.com/JohnWulff/balad.