

# Deriving $E_{\text{reheat}}$

$$V_{\text{vir}}^2 = \frac{GM_{\text{vir}}}{R_{\text{vir}}} , \quad k_B T_{\text{vir}} = \frac{1}{2} \mu m_p V_{\text{vir}}^2$$

$$T_{\text{vir}} = \frac{\mu m_p}{2k_B} \frac{GM_{\text{vir}}}{R_{\text{vir}}}$$

from Virial Shock heating

$$T_g = \frac{3}{16} \frac{\mu m_p}{k_B} V^2 , \quad T_{\text{shock}} \sim \frac{3}{16} \frac{\mu m_p}{k_B} V_{\text{vir}}^2$$

$$T_{\text{vir}} = \frac{1}{2} \frac{\mu m_p}{k_B} V_{\text{vir}}^2 , \quad \mathcal{U} = \frac{3}{2} \frac{k_B T}{\mu m_p}$$

$$\mathcal{U} = M_g \quad \mathcal{U} = \frac{3}{8} \frac{M_g k_B T}{\mu m_p}$$

$$\Delta E = \frac{3}{8} \frac{M_g k_B}{\mu m_p} (T_f - T_i)$$