

Deriving E_{reheat}

$$V_{\text{vir}}^2 = \frac{GM_{\text{vir}}}{R_{\text{vir}}}, \quad k_B T_{\text{vir}} = \frac{1}{2} \mu_{\text{mp}} V_{\text{vir}}^2$$

$$T_{\text{vir}} = \frac{\mu_{\text{mp}}}{2k_B} \frac{GM_{\text{vir}}}{R_{\text{vir}}}$$

from virial shock heating

$$T_{\text{e}} = \frac{3}{16} \frac{\mu_{\text{mp}}}{k_B} V^2, \quad T_{\text{shock}} \sim \frac{3}{16} \frac{\mu_{\text{mp}}}{k_B} V_{\text{vir}}^2$$

$$T_{\text{vir}} = \frac{1}{2} \frac{\mu_{\text{mp}}}{k_B} V_{\text{vir}}^2, \quad u = \frac{3}{2} \frac{k_B T}{\mu_{\text{mp}}}$$

$$U = M_{\text{g}} u = \frac{3}{2} \frac{M_{\text{g}} k_B T}{\mu_{\text{mp}}}$$

$$\Delta E = \frac{3}{2} \frac{M_{\text{g}} k_B}{\mu_{\text{mp}}} (T_{\text{f}} - T_{\text{i}})$$