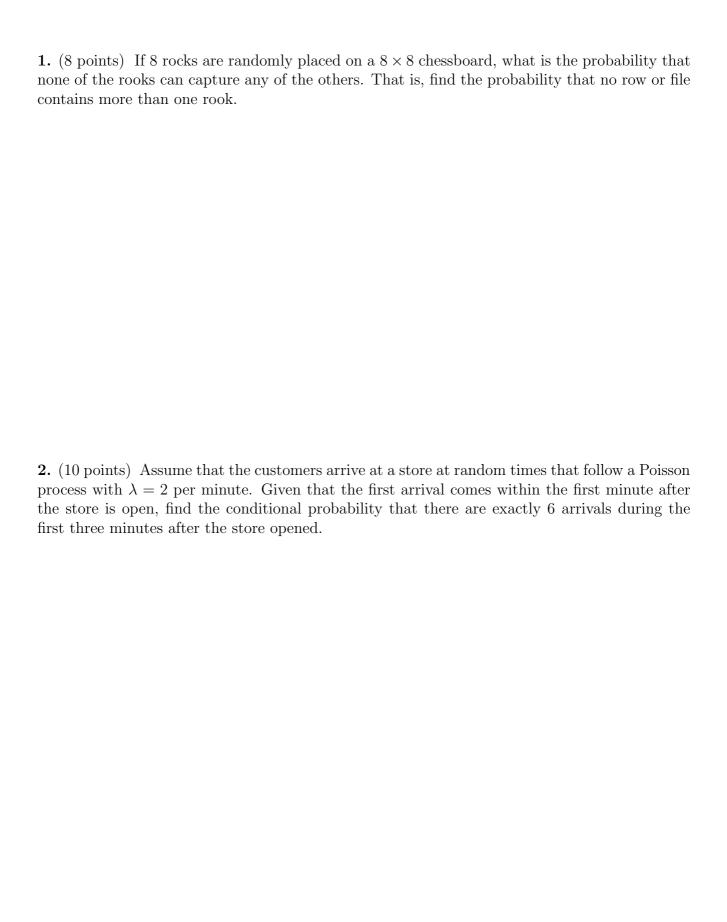
Your Name		
Student Number $_$		
Signature		

- 1. Print your name, student ID number and section number on this page. Do **NOT** separate the pages of the exam.
- 2. WRITE LEGIBLLY AND SHOW ALL OF YOUR WORK. Partial credit will only be given where you have made it clear that you understand part of the solution. Answers without justification may not receive full credit. Place a box around your final answer to each equation.
- 3. If you use a trial and error (or guess and check) method when an algebraic method is available, you will not receive full credits.
- 4. You may use two sheets (two-sided) of handwritten notes and a basic scientific calculator. **Do not share notes and no graphing calculator is allowed.** If you need more space to solve a problem, use the back of the page preceding that problem.
- 5. Read each question carefully. Work the problems in an order that will maximize your score. Good Luck!

Score

1.	(8)	
2.	(10)	
3.	(10)	
4.	(10)	
5.	(12)	
Total	(50)	



3. (10 points) 10 men went to a party, each wearing a hat. They put their hats on a table when they got there. After the party, each picks up a hat randomly from the hats that are on the table, one by one. Let X be the number of people who got his own hat back. Find $\mathbf{E}[X]$ and $\mathrm{Var}(X)$.

(*Hint*: Let $X_k = 1$ if the k^{th} man got his own hat back, and $X_k = 0$ otherwise. Then $X = \sum_{k=1}^{10} X_k$.)

4. (10 points) Random variable Y is of standard normal distribution. that the equation $x^2 + 2Yx + 2 - Y = 0$ has no real roots?	What is the probability

5 .	(12 points)	Suppose that a	continuous	random	variable	X h	nas	density	function	$f_X(x)$	=
c x	$ e^{-x^2}$ for $-\infty$	$0 < x < \infty$.									

(a) Find the constant c;

(b) Find the density function of $Y = X^2$.