Lecture 28 (CR.11) In Lab

we have been talking about inference on B (and a),
the conditional mean of y, given x, and a single y, at K.

What about multiple regression?

In going from y = x+Bx (1+1 parm) # of B's.

to Y= x+ Bixi+ Bzxz +--- + Bkxk (k+1 params)

things generalize in a straight forward way.

Basically, all That happens is (N-2) - N- (k+1).

This happens every where, e-g.

- 1) The estimate of σ_{ϵ}^{2} is $S_{e}^{2} = \frac{SSE}{N-(K+1)}$
- 2) The df associated with t-test changes: n-2 -> n-(h+1)
- 3) Even, CI & PI formulas are the same, except for

ŷ± t* Sŷ , ŷ± t* (\$\frac{1}{2}\) = \frac{55E}{N-(N+1)}

In This class we did not develop a formula for Sq in multiple regression, but it does exist. As far as you are concerned, you can always get Sq from R.

Finally, don't lorget That The issues of collinearity and interaction come back again when doing multiple regression.

The presence of multiple B's allows for one more test:

Ho: $\beta_1 = \beta_2 = \dots = \beta_k = 0$ Test of model utility.

Ho: At least 1 B; is to

The $\gamma = \alpha + \beta_1 \times_1 + \beta_2 \times_2 + \dots + \beta_k \times_k$, if all $\beta_i = 0$, then none of the predictors are useful for prediction y.

This F-test allows you to do ONE test to find out if any of The predictors are useful for predicting y. This is very useful if k is large, because it tells you if any of the predictors are useful. I.e. it tells you if there is a "needle in the hay stack," to begin with!

So, if you have a lot of possible / potential predictors, but you are not save if any of Them are useful, what you can do is to include all of Them in The regression model, and do The F-test of model utility. IF you get a significant result (ie. p-value <a), Then There is evidence that at least one of the prodictors is useful. [THEN] you can do separates tests on each of the p's to see which predictors are the waful ones. But IF The F-test comes back as non-significant, Then there is no evidence that any of the predictors are useful. [THEN], you don't have to test each predictor separately.

	The main Theorem for The F-test is:
Thm:	$F = \frac{R^2/[k]}{(l-R^2)/[n-(k+1)]} = \frac{R^2/[k]}{(l-R^2)/[n-(k+1)]}$
	has an F- distr. with df= (k, n-(k+1))
	: p-value = Right area under F when the is "at least ", then The p-value is just the right tail
	Then, if p-value $\angle x$, we can reject the $(\beta_i = \beta_2 = \cdots = \beta_k = 0)$ in favor of the (atleast 1 β_i is not zero)
	IF The p-value La, we can start testing each of The Bi separately. Fortunately, The test for each Bi is The
	Same as The test for a single B, except for df= n-(k+1) Erg. Suppose we want to test B3:
	Ho: B3 D Bo (e-g. D) C.I. for B3:
	$t_{obs} = \frac{\hat{\beta}_{3} - \beta_{o}}{\sum_{s} \frac{\hat{\beta}_{3} - \beta_{o}}}{\sum_{s} \frac{\hat{\beta}_{3} - \beta_{o}}$
	p-value = (1,2) pr (+ [] + > b)
d	f=n-(h+1) in Table VI (or IV)
	Note: eventhough we are testing ONE Bi, The off is n-(h+1)



To make the above thus. more believable, note that The
above F-vatio is similar to the F-vatione write
in the context of 1-way ANOVA (ch. 9):
B2/L (SSeyl.)/L
F = (1-02)/1
In the context of 1-way ADBVA (Ch. 9): $F = \frac{R^2/k}{(1-R^2)/[n-(h+1)]} = \frac{(SSexpl.)/k}{(1-\frac{SSexpl.})/[n-(h+1)]} = \frac{(SSexpl.)/[n-(h+1)]}{(1-\frac{SSexpl.})/[n-(h+1)]} = \frac{SSexpl./k}{SSE/(n-(h+1))} = \frac{SSexpl./k}{SSE/(n-(h+1))} = \frac{SSexpl./k}{SSW; thin/[n-(h+1)]} = \frac{SSw; thin/[n-(h+1)]}{SSW; thin/[n-(h+1)]}$
SSovelile SSLA 1000 /1
- CSF/(u-k)
SSwithin [n-(4+1)]

```
he regression equation is
   durpr = -0.912 + 0.161 formconc + 0.220 catratio + 0.0112 temp + 0.102 time
                       StDev
   Predictor
                Coef
                                                In This example
    Constant
             -0.9122
                      0.8755
                             -1.04
                                   0.307
   formconc
             0.16073
                      0.06617
                              2.43
                                   0.023
             0.21978
                                  0.000
    catratio
                      0.03406
                             6.45
                                              you are going to
    temp
             0.011226 0.004973
                              2.26
                                   0.033
            0.10197 0.05874
                              1.74 0.095
    time
    S = 0.8365 \text{ R-Sq} = 69.2\% \text{ R-Sq(adj)} = 64.3\%
                                            Learn what all These
   Analysis of Variance
   Source
             DF SS
             4 39.3769 9.8442 14.07 0.000
    Regression
             25 17.4951 0.6998
   Error
             29 56.8720
   Total
a) Is The fitted model useful?
     proble = prob (F> Fobs) = prob (F>14.04)
     According to Table VIII, If=(4,25)
     So, at any reasonable &, we can rejet the null
      hyp. (That all B: are Zero) in favor of The
     alt. (That attent one of The B: is not zero)
     I.e. The mold is useful
```

b) Estimate, in a way that conveys into about precision & reliability, We average change in durability press rating associated with a 1- degree increase in caring temperature, when all other predictors remain fixed. (if There is NO collinearity) I.e. what's the C.I for B temp 95% C.I. $\beta \pm t^* \frac{5e}{S_{xx}} = .0112 \pm 2.060 \frac{0.8365}{2.51ded}$ 0112 ± 2,060 (.004973) => this is The interval estimate for B. It's useful as it is, but we can also see That Brang to. We can build the C.I. for the other B's i C.T. form conc $(1607 \pm 2.060 (.06617) = (0.02, 0.30)$ Catratio · 2198 I " · 03406 = (0.15, 0.29) temp .0112 ± 1 .00497 = (0.001, 0.02) time 10197 t ; 0587 = (-0.02, 0.22)

	In part a, we found out that afterit one of The B: +0.
	To see which one(s), we test each of Them!
	Ho: B; =0 vs. H; B; &0 for eali.
(2	E-g- Ho: Bformold. =0
	H1: Borrold. (7)
S _t	ton, = -(6073-0) = 2.43 Sane as atgut in book. P-value = 2 prob(t>tons) = 2(.012)
formaldo	p-value = (2) prob(t>toss) = 2(.012)
(from	So, p-value La => formaldelyde provides useful info,
	In fact, look at all the p-values: look at
	023, 000, 033, 095 Last Col.
	$I = \{1, 2, \dots, 2,$
	At a= 05 B +0 B+0 B+0 B= cannot tell Sumall. Cate temp time
	consistent with The conclusions in part 6.
(Note Trese p-values are different from what you would
	Note Trese p-values are different from what you would get if you did y= x+B,x,, y=x+Bzxz, Etc. and tested if each of these B; are zero.
	and tested if each of there no see 3013
	- , , , - , , , ave -2 ev = 0

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