homework2 porblem 1

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1. Assume that spot rates are as follows:

Maturity	Spot Rate
1	5%
2	5.5%
3	6%
4	6.3%

Spot rates are with annual compounding, coupon payments are annual, and par values are \$100. Compute the prices of the following bonds:

(a) A zero-coupon bond with 3 years to maturity.

$$\frac{100}{(1+0.06)^3} = 83.96$$

The price of such a zero-coupon bond is 83.96.

$$\frac{100}{(1+ytm)^3} = 83.96$$

Solve and we get ytm = 0.06

(b) A bond with coupon rate 6% and 2 years to maturity.

$$\frac{6}{(1+0.05)} + \frac{106}{(1+0.055)^2} = 100.95$$

The price of such a coupon bond is 100.95.

$$\frac{6}{(1+ytm)} + \frac{106}{(1+ytm)^2} = 100.95$$

Solve and we get ytm = 0.0548.

(c) A bond with coupon rate 8% and 4 years to maturity.

$$\frac{8}{(1+0.05)} + \frac{8}{(1+0.05)^2} + \frac{8}{(1+0.05)^3} + \frac{108}{(1+0.05)^4} = 106.11$$

The price of such coupon bond is 106.11.

$$\frac{8}{(1+ytm)} + \frac{8}{(1+ytm)^2} + \frac{8}{(1+ytm)^3} + \frac{108}{(1+ytm)^4} = 106.11$$

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Solve and we get ytm = 0.0623