## Live TUS Uncertainty Calculation

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Uncertainty is calculated by combining the repeatability (Type A) and fixed systematic (Type B) components:

$$\nu = mn - 1 \quad \text{(degrees of freedom)}$$
 
$$o_i = o_i^{DaqBook} + o_i^{TC} \quad \text{(cumulative offset for channel } i \text{)}$$
 
$$x'_{i,j} = x_{i,j} + o_i \quad \text{(corrected reading for channel } i \text{ at time } j \text{)}$$
 
$$u_A^2 = \frac{1}{\nu} \sum_{i=1}^n \sum_{j=1}^m (x'_{i,j} - T_N)^2 \quad \text{(Type A standard uncertainty squared)}$$
 
$$u_c = \sqrt{u_A^2 + u_B^2} \quad \text{(combined standard uncertainty)}$$
 
$$U = k \cdot u_c \quad \text{(expanded uncertainty, } k = t_{0.9545, \nu} \text{)}$$
 Reported Uncertainty =  $\max (U, U_{\text{CMC}})$ 

Symbol	Definition
$\overline{n}$	Number of thermocouples
m	Number of readings per thermocouple
i	Thermocouple index $(i \in 1, \dots, n)$
j	Survey time index $(j \in 1, \dots, m)$
$\nu$	Degrees of freedom $(mn-1)$
$x_{i,j}$	Raw measured temperature from probe $i$ , reading $j$
$o_i^{\mathrm{DaqBook}}$	Offset for DaqBook channel $i$
$o_i^{ m DaqBook} \ o_i^{ m TC}$	Offset for the probe assigned to channel $i$
$o_i$	Total correction offset for probe/channel $i$
$x'_{i,j}$	Corrected temperature for probe $i$ , reading $j$
$T_N$	Nominal temperature
$u_A$	Type A standard uncertainty
$u_B$	Type B standard uncertainty from the MUG
$u_c$	Combined standard uncertainty
k	Coverage factor (t-distribution, $95.45\%$ )
U	Expanded uncertainty
$U_{\rm CMC}$	Minimum reportable uncertainty, as listed in the current scope.