

1 Pseudocode for the exact algorithm

Input : Graph G and source s
Output: For each halfedge, a TreeSet of windows

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for  $v \in \text{Neighbors}(s)$  do
   $e \leftarrow \text{edge}(u, v)$ 
   $l \leftarrow \text{length}(e)$ 
   $Q \leftarrow \text{Window}(0, l, 0, l, e, \sigma = 0)$ 
end
while  $Q \neq \emptyset$  do
   $w \leftarrow Q.\text{pop}$ 
   $e_1 = w.e.\text{next.opposite}$ 
   $e_2 = w.e.\text{next.next.opposite}$ 
  for  $i \leftarrow 1$  to 2 do
     $W_i = \text{propagation of } w \text{ on } e_i$ 
     $w_i\text{First} = \text{leftmost window on } e_i \text{ to intersect with } W_i \text{ on } e_i$ 
     $w_i\text{Last} = \text{rightmost window on } e_i \text{ to intersect with } W_i \text{ on } e_i$ 
    for  $w'$  on  $e_i$  with  $w' \geq w_i\text{First}$  and  $w' \leq w_i\text{Last}$  do
      if  $W_i$  "wins the fight" on an interval  $\neq \emptyset$  then
        Update  $w'$ 
        Add  $W_i$  with correct parameters
         $Q \leftarrow W_i$ 
      end
    end
  end
end

```

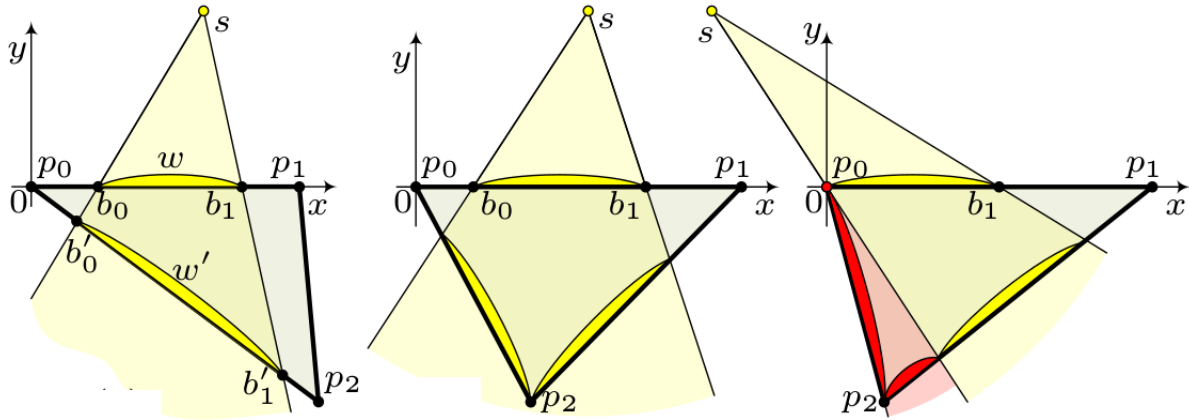
Algorithm 1: Exact Algorithm for computing shortest paths

Some operations still have to be explained a bit more accurately. The first one is :

$$Q \leftarrow \text{Window}(e, 0, l, 0, l, \sigma = 0)$$

Here Q is a priority queue containing windows with the order : $w_1 \leq w_2$ if and only if the minimal distance from w_1 to its pseudosource plus the distance from the pseudosource to the real source is \leq to the same real number for w_2 .

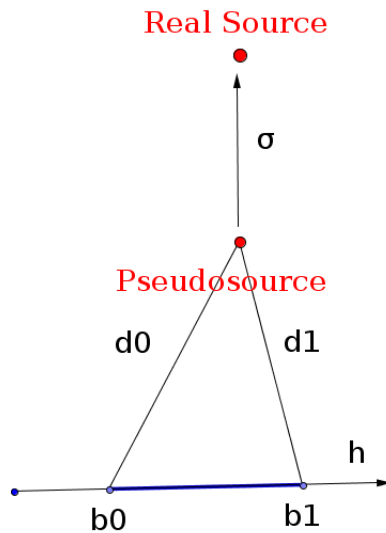
Then we pick the "closest" window according to our distance and we propagate it over the two opposite halfedges (orientation is important to know on which side of the edge is the pseudosource). We have these three (plus two with symetries) cases :



The yellow line is the propagated window and the red ones are the propagated windows when the blue segment touches one of the edge ends. These new windows have the red dot as a new pseudosource.

The orientation of halfedges is important. By convention, we decided that the source was on your left when you are oriented like the halfedge (for instance, in the five example the top halfedge with the blue segment is oriented from left to right). Therefore a window is described as a six-tuple: $w = (d_0, d_1, b_0, b_1, h, \sigma)$

Where $d_0, d_1, b_0, b_1, \sigma$ are defined like the article suggested. We only use h the halfedge instead of τ the orientation because every time we pop a window out of Q we need to know where it is in the graph.



Then we need to explain : " w_iFirst = leftmost window on e_i to intersect with W_i on e_i "

This sentence implies two things : given an edge, we can find the windows on it and we can perform a quick search on these windows to find the right ones. Therefore we chose to implement that with an **ArrayList of TreeSets**. The ArrayList is indexed by halfedges' indexes and TreeSets contain the windows on one halfedge.

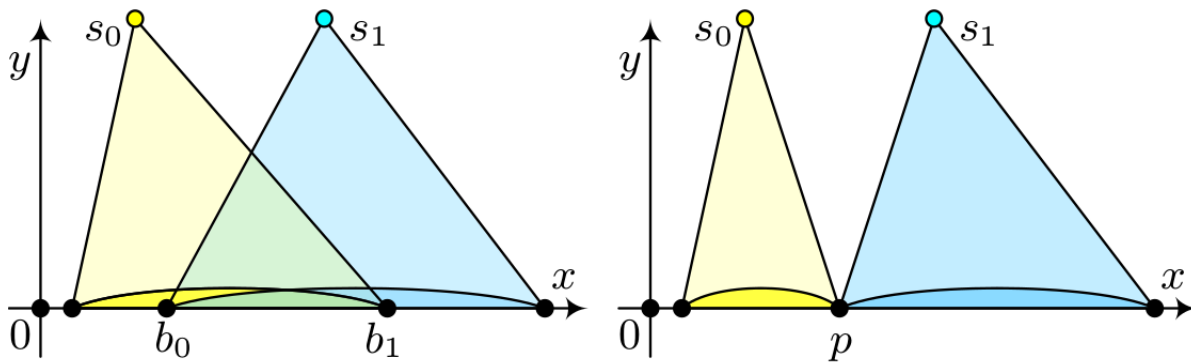
But we still need to specify an order on the windows to be able to perform a binary search. We chose to sort the windows according to their b_0 . This is ok because at every iteration of the while loop, windows on each edge are not overlapping so we have for instance w_iFirst as the last window whose b_0 is \leq to the propagated window's b_0 .

Therefore we have $O(\log(n))$ for inserting, removing or searching operations.

Finally, we can explain " W_i "wins the fight" on an interval $\neq \emptyset$ "

This means that we need to compute intervals on which the new propagated window and old windows are overlapping. If they are, we then need to compute the interval on which the new window offers a shorter path and the interval on which the old one is better (ie we have to find the right p on the figure).

We can do this in $O(1)$ with geometry formulas.



During this step we have to be careful with the orientation of the edges because if the propagated window goes downwards we don't want to compare it with windows going upwards.

Finally, we push something in the priority queue Q if and only if some distances have been updated.