

Índice

1. Referencia

Algorítmo	Parámetros	Función
sort, stable_sort	f, 1	ordena el intervalo
nth_element	f, nth, l	void ordena el n-esimo, y
		particiona el resto
fill, fill_n	f, l / n, elem	void llena [f, l) o [f,
		f+n) con elem
lower_bound, upper_bound	f, l, elem	it al primer / ultimo donde se
		puede insertar elem para que
		quede ordenada
binary_search	f, l, elem	bool esta elem en [f, l)
copy	f, l, resul	hace resul+ i =f+ $i \forall i$
find, find_if, find_first_of	f, l, elem	it encuentra i \in [f,l) tq. i=elem,
	/ pred / f2, l2	$pred(i), i \in [f2,l2)$
count, count_if	f, l, elem/pred	cuenta elem, pred(i)
search	f, l, f2, l2	busca $[f2,l2) \in [f,l)$
replace, replace_if	f, l, old	cambia old / pred(i) por new
	/ pred, new	
reverse	f, 1	da vuelta
partition, stable_partition	f, l, pred	pred(i) ad, !pred(i) atras
min_element, max_element	f, l, [comp]	it min, max de [f,l]
lexicographical_compare	f1,l1,f2,l2	bool con [f1,l1];[f2,l2]
next/prev_permutation	f,l	deja en [f,l) la perm sig, ant
set_intersection,	f1, l1, f2, l2, res	[res,) la op. de conj
set_difference, set_union,		
set_symmetric_difference,		
push_heap, pop_heap,	f, l, e / e /	mete/saca e en heap [f,l),
make_heap		hace un heap de [f,l)
is_heap	f,l	bool es [f,l) un heap
accumulate	f,l,i,[op]	$T = \sum / \text{oper de [f,l)}$
inner_product	f1, l1, f2, i	$T = i + [f1, 11) \cdot [f2, \dots)$
partial_sum	f, l, r, [op]	$r+i = \sum /oper de [f,f+i] \forall i \in [f,l)$
builtin_ffs	unsigned int	Pos. del primer 1 desde la derecha
builtin_clz	unsigned int	Cant. de ceros desde la izquierda.
builtin_ctz	unsigned int	Cant. de ceros desde la derecha.
builtin_popcount	unsigned int	Cant. de 1's en x.
builtin_parity	unsigned int	1 si x es par, 0 si es impar.
builtin_XXXXXXII	unsigned ll	= pero para long long's.

2. Estructuras

2.1. RMQ (static)

```
1 // Dado un arreglo y una operacion asociativa idempotente:
  // get(i, j) opera sobre el rango [i, j).
   // Restriccion: LVL >= ceil(log n). Usar [ ] para llenar
   // el arreglo y luego build().
   struct RMQ {
     #define LVL 17
6
     tipo vec[LVL][1 << (LVL + 1)];
7
     tipo &operator [](int p){ return vec[0][p]; }
8
     tipo get(int i, int j){ // intervalo [i, j)
9
       int p = 31 - \_builtin\_clz(j - i);
10
       return min(vec[p][i], vec[p][j - (1 << p)]);</pre>
11
12
     void build(int n) { // O(n \log n)
13
       int mp = 31 - __builtin_clz(n);
14
       forn(p, mp) forn(x, n - (1 << p))
15
         vec[p + 1][x] = min(vec[p][x], vec[p][x + (1 << p)]);
16
     }
17
18 };
```

2.2. RMQ (dynamic)

```
// Dado un arreglo y una operacion asociativa con neutro:
   // get(i, j) opera sobre el rango [i, j).
   typedef int node; // Tipo de los nodos
   #define MAXN 100000
   #define operacion(x, y) max(x, y)
   const int neutro = 0;
   struct RMQ {
7
     int sz;
8
     node t[4*MAXN];
9
     node &operator [](int p){ return t[sz + p]; }
10
     void init(int n){ // O(n lg n)
11
       sz = 1 << (32 - __builtin_clz(n));</pre>
12
       forn(i, 2*sz) t[i] = neutro;
13
14
     void updall(){//0(n)}
15
       dforn(i, sz){
16
         t[i] = operacion(t[2*i], t[2*i + 1]);
17
       }
18
```

```
19
     node get(int i, int j){ return get(i, j, 1, 0, sz); }
20
     node get(int i, int j, int n, int a, int b){ // O(\lg n)
21
       if(j <= a || i >= b) return neutro;
22
       if(i <= a && b <= j) return t[n];
23
       int c = (a + b)/2;
24
       return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n + 1, c, b));
25
26
     void set(int p, node val){ // O(lg n)
27
       for(p += sz; p > 0 && t[p] != val;){
         t[p] = val;
29
         p /= 2;
         val = operacion(t[p*2], t[p*2 + 1]);
32
    }
   } rmq;
  // Uso:
36 | cin >> n; rmq.init(n); forn(i, n) cin >> rmq[i]; rmq.updall();
                            2.3. RMQ (lazy)
1 // Dado un arreglo y una operacion asociativa con neutro:
2 // get(i, j) opera sobre el rango [i, j).
   typedef int node; // Tipo de los elementos del arreglo
   typedef int alt; // Tipo de la alteracion
   #define operacion(x, y) (x + y)
   const node neutro = 0; const alt neutro_alt = 0;
   #define MAXN 100000
   struct RMQ {
     int sz;
     node t[4*MAXN];
     alt dirty[4*MAXN];
11
     node &operator [](int p){ return t[sz + p]; }
12
     void init(int n){ // O(n lg n)
13
       sz = 1 \ll (32 - \_builtin\_clz(n));
14
       forn(i, 2*sz){
15
         t[i] = neutro;
16
         dirty[i] = neutro_alt;
17
       }
18
19
     void push(int n, int a, int b){ // Propaga el dirty a sus hijos
20
       if(dirty[n] != neutro_alt){
21
         t[n] += dirty[n]*(b - a); // Altera el nodo
22
```

```
if(n < sz){
23
           dirty[2*n] += dirty[n];
^{24}
           dirty[2*n + 1] += dirty[n];
25
26
         dirty[n] = 0;
27
28
29
     node get(int i, int j, int n, int a, int b){ // O(lg n)
30
       if(j <= a || i >= b) return neutro;
31
       push(n, a, b); // Corrige el valor antes de usarlo
32
       if(i <= a && b <= j) return t[n];
33
       int c = (a + b)/2;
34
       return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n + 1, c, b));
35
36
     node get(int i, int j){ return get(i, j, 1, 0, sz); }
37
     // Altera los valores en [i, j) con una alteración de val
38
     void alterar(alt val, int i, int j, int n, int a, int b){ // O(lg n)
39
       push(n, a, b);
40
       if(i \le a \mid | i >= b) return:
41
       if(i <= a && b <= j){
42
         dirty[n] += val;
43
         push(n, a, b);
44
         return;
45
46
       int c = (a + b)/2;
47
       alterar(val, i, j, 2*n, a, c); alterar(val, i, j, 2*n + 1, c, b);
48
       t[n] = operacion(t[2*n], t[2*n + 1]);
49
50
     void alterar(alt val, int i, int j){ alterar(val, i, j, 1, 0, sz); }
51
52 | } rmq;
                        2.4. RMQ (persistente)
   typedef int tipo;
   tipo oper(const tipo &a, const tipo &b){
```

```
typedef int tipo;
tipo oper(const tipo &a, const tipo &b){
    return a + b;
}
struct node {
    tipo v; node *1, *r;
    node(tipo v):v(v), l(NULL), r(NULL) {}
    node(node *1, node *r) : l(l), r(r){
    if(!1) v = r->v;
    else if(!r) v = l->v;
```

```
else v = oper(1->v, r->v);
    }
12
13
   };
   node *build (tipo *a, int tl, int tr) { // modificar para tomar tipo a
     if(tl + 1 == tr) return new node(a[tl]);
     int tm = (tl + tr) >> 1;
16
     return new node(build(a, tl, tm), build(a, tm, tr));
17
18
   node *upd(int pos, int new_val, node *t, int tl, int tr){
19
     if(tl + 1 == tr) return new node(new_val);
     int tm = (tl + tr) >> 1;
21
     if(pos < tm) return new node(upd(pos, new_val, t->1, tl, tm), t->r);
     else return new node(t->1, upd(pos, new_val, t->r, tm, tr));
23
24
   tipo get(int 1, int r, node *t, int tl, int tr){
25
     if(1 == tl && tr == r) return t->v;
     int tm = (tl + tr) >> 1;
     if (r \le tm) return get (l, r, t \rightarrow l, tl, tm);
     else if(l \ge tm) return get(l, r, t \ge r, tm, tr);
     return oper(get(1, tm, t->1, tl, tm), get(tm, r, t->r, tm, tr));
31 }
```

2.5. Fenwick Tree

```
1 // Para 2D: tratar cada columna como un Fenwick Tree,
2 // agregando un for anidado en cada operacion.
   struct Fenwick {
     static const int sz = 1000001;
     tipo t[sz];
5
     void adjust(int p, tipo v) { // p en [1, sz), 0(\lg n)
6
       for(int i = p; i < sz; i += (i \& -i)) t[i] += v;
7
8
     tipo sum(int p){ // Suma acumulada en [1, p], O(lg n)
9
       tipo s = 0;
10
       for(int i = p; i; i -= (i \& -i)) s += t[i];
11
       return s;
12
13
     tipo sum(int a, int b){ return sum(b) - sum(a - 1); }
14
     // Obtener mayor valor con suma acumulada menor o igual que x.
15
     // Para el menor, pasar x - 1 y sumar 1 al resultado.
16
     int getind(tipo x){ // O(lg n)
17
       int idx = 0, mask = n;
18
       while(mask && idx < n) {</pre>
19
```

```
int z = idx + mask;
20
         if(x >= t[z])
^{21}
           idx = z, x = t[z];
^{22}
         mask >>= 1;
23
       }
^{24}
       return idx;
25
26
27 | };
                             2.6. Union Find
   struct UnionFind{
     vector<int> p; // Arreglo que contiene los padres de cada nodo
     void init(int n){ f.clear(); f.insert(f.begin(), n, -1); }
3
     int comp(int x){ return f[x] == -1 ? x : f[x] = comp(f[x]); } // O(1)
     bool join(int i, int j){
5
      bool con = comp(i) == comp(j);
6
       if(!con) f[comp(i)] = comp(j);
7
       return con;
8
     }
9
10 };
                         2.7. Disjoint Intervals
   // Guarda intervalos como [first, second]
   // En caso de colision, los une en un solo intervalo
   bool operator <(const ii &a, const ii &b){ return a.first < b.first; }</pre>
   struct disjoint_intervals {
     set<ii>> segs:
5
     void insert(ii v){ // O(lg n)
6
       if(v.snd - v.fst == 0.0) return; // Cuidado!
       set<ii>>::iterator it, at;
8
       at = it = segs.lower_bound(v);
9
       if(at != segs.begin() && (--at)->snd >= v.fst){
10
         v.fst = at->fst;
11
         --it;
12
       }
13
       for(; it!=segs.end() && it->fst <= v.snd; segs.erase(it++))</pre>
14
         v.snd = max(v.snd, it->snd);
15
       segs.insert(v);
16
17
18 | };
                             2.8. RMQ (2D)
```

```
struct RMQ2D { // n filas, m columnas
2
     int sz;
     RMQ t[4*MAXN]; // t[i][j] = i fila, j columna
     RMQ & operator [](int p){ return t[sz/2 + p]; }
     void init(int n, int m) { // O(n*m)
       sz = 1 \ll (32 - \_builtin\_clz(n));
       forn(i, 2*sz) t[i].init(m);
7
    }
8
     void set(int i, int j, tipo val){ // O(\lg(m)*\lg(n))
       for(i += sz; i > 0;){
         t[i].set(j, val);
11
         i /= 2;
12
         val = operacion(t[i*2][j], t[i*2 + 1][j]);
13
14
15
     tipo get(int i1, int j1, int i2, int j2){
16
       return get(i1, j1, i2, j2, 1, 0, sz);
17
    }
18
     // O(lg(m)*lg(n)), rangos cerrado abierto
19
     int get(int i1, int j1, int i2, int j2, int n, int a, int b){
       if(i2 <= a || i1 >= b) return 0;
21
       if(i1 <= a && b <= i2) return t[n].get(j1, j2);</pre>
22
       int c = (a + b)/2;
23
       return operacion(get(i1, j1, i2, j2, 2*n, a, c),
                        get(i1, j1, i2, j2, 2*n + 1, c, b));
25
     }
26
   } rma;
27
   // Ejemplo para inicializar una matriz de n filas por m columnas
   RMQ2D rmq; rmq.init(n, m);
  forn(i, n) forn(j, m){
    int v; cin >> v; rmq.set(i, j, v);
31
32 }
                               2.9. Big Int
1 #define BASEXP 6
   #define BASE 1000000
   #define LMAX 1000
   struct bint {
    int 1:
    11 n[LMAX];
     bint(11 x = 0){
7
       1 = 1;
```

```
forn(i, LMAX){
                                                                                           c.n[i] = (q + BASE) \% BASE;
9
         if(x) l = i + 1;
                                                                                           q = (q + BASE)/BASE - 1;
                                                                                    53
10
         n[i] = x \% BASE;
                                                                                        }
11
                                                                                    54
                                                                                         c.invar();
         x /= BASE;
                                                                                    55
12
       }
                                                                                         return make_pair(c, !q);
13
14
                                                                                    57
     bint(string x){
                                                                                       bint &operator -=(bint &a, const bint &b){
15
       1 = ((int) x.size() - 1) / BASEXP + 1;
                                                                                         return a = lresta(a, b).first;
16
       fill(n, n + LMAX, 0);
17
                                                                                    60
                                                                                       bint operator -(const bint &a, const bint &b){
       11 r = 1;
18
       forn(i, sz(x)){
                                                                                         return lresta(a, b).first;
19
                                                                                    62
         n[i / BASEXP] += r*(x[x.size() - 1 - i] - '0');
20
                                                                                    63
         r *= 10; if(r == BASE) r = 1;
                                                                                       bool operator <(const bint &a, const bint &b){
21
       }
                                                                                         return !lresta(a, b).second;
22
     }
23
                                                                                    66
     void out(){
                                                                                       bool operator <=(const bint &a, const bint &b){
24
                                                                                         return lresta(b, a).second;
       printf("%11d", n[1-1]);
25
       dforn(i, l - 1) printf("\%6.61lu", n[i]); // 6 = BASEXP!
26
                                                                                    69
                                                                                       bool operator ==(const bint &a, const bint &b){
     }
27
     void invar(){
                                                                                         return a <= b && b <= a;
28
       fill(n + 1, n + LMAX, 0);
                                                                                       }
                                                                                    72
29
       while(l > 1 && !n[l - 1]) l--;
                                                                                       bint operator *(const bint &a, ll b){
30
     }
                                                                                   74
                                                                                           bint c;
31
                                                                                           11 q = 0;
                                                                                    75
32
   bint operator+(const bint &a, const bint &b){
                                                                                           forn(i, a.1){
                                                                                    76
33
     bint c;
                                                                                             q += a.n[i]*b;
34
                                                                                             c.n[i] = q \% BASE;
     c.1 = max(a.1, b.1);
35
     11 q = 0;
                                                                                             q /= BASE;
                                                                                    79
36
     forn(i, c.1){
                                                                                           }
                                                                                    80
37
       q += a.n[i] + b.n[i];
                                                                                           c.1 = a.1;
38
       c.n[i] = q \% BASE;
                                                                                           while(q){
39
       q /= BASE;
                                                                                             c.n[c.l++] = q \% BASE;
40
     }
                                                                                             q /= BASE;
41
     if(q) c.n[c.l++] = q;
                                                                                           }
     c.invar();
                                                                                           c.invar();
43
     return c;
                                                                                           return c;
44
                                                                                    88
45
   pair \langle bint, bool \rangle lresta(const bint &a, const bint &b){ // c = a - b
                                                                                       bint operator *(const bint &a, const bint &b){
     bint c;
                                                                                           bint c;
                                                                                    90
47
     c.1 = max(a.1, b.1);
                                                                                           c.l = a.l + b.l;
                                                                                   91
48
     11 q = 0;
                                                                                           fill(c.n, c.n + b.l, 0);
49
    forn(i, c.1){
                                                                                           forn(i, a.1){
                                                                                   93
50
       q += a.n[i] - b.n[i];
                                                                                               11 q = 0;
51
                                                                                   94
```

```
forn(j, b.1){
                                                                                           c.n[i] = u:
95
              q += a.n[i]*b.n[j] + c.n[i+j];
                                                                                           rm -= b*u:
                                                                                   139
96
              c.n[i + j] = q \% BASE;
                                                                                        }
97
                                                                                   140
                                                                                         c.1 = a.1;
              q /= BASE;
                                                                                   141
98
                                                                                         c.invar();
                                                                                   142
99
            c.n[i + b.1] = q;
                                                                                        return make_pair(c, rm);
100
                                                                                   143
                                                                                   144
101
                                                                                       bint operator /(const bint &a, const bint &b) {return ldiv(a, b).first;}
        c.invar();
102
        return c;
                                                                                   146 bint operator %(const bint &a, const bint &b) {return ldiv(a, b).second;}
103
104
                                                                                                                2.10. HashTables
    pair<br/><br/>bint, ll> ldiv(const bint &a, ll b){ // c = a / b; rm = a %b
105
      bint c;
106
                                                                                    1 // Compilar con: g++ --std=c++11
      11 \text{ rm} = 0:
107
                                                                                    2 struct Hash {
      dforn(i, a.1){
108
                                                                                         size_t operator()(const ii &a) const {
       rm = rm*BASE + a.n[i];
109
                                                                                           size_t s = hash<int>()(a.fst);
       c.n[i] = rm/b:
110
                                                                                           return hash<int>()(a.snd) + 0x9e3779b9 + (s << 6) + (s >> 2):
                                                                                    5
       rm %= b;
111
                                                                                    6
      }
112
                                                                                         size_t operator()(const vector<int> &v) const {
                                                                                    7
      c.1 = a.1:
113
                                                                                           size t s = 0:
      c.invar();
114
                                                                                           for(auto &e : v)
      return make_pair(c, rm);
115
                                                                                             s = hash(int)(e) + 0x9e3779b9 + (s << 6) + (s >> 2);
116
                                                                                           return s;
                                                                                    11
    bint operator /(const bint &a, ll b){ return ldiv(a, b).first; }
117
                                                                                        }
                                                                                    12
    ll operator %(const bint &a, ll b){ return ldiv(a, b).second; }
                                                                                       };
                                                                                    13
    pair<bint, bint> ldiv(const bint &a, const bint &b){
119
                                                                                       unordered_set<ii, Hash> s;
      bint c;
120
                                                                                    unordered_map<ii, int, Hash> m; // map<key, value, hasher>
      bint rm = 0;
121
                                                                                                                  2.11. Modnum
      dforn(i, a.1){
122
        if(rm.l == 1 && !rm.n[0])
123
                                                                                    1 struct mnum {
          rm.n[0] = a.n[i]:
124
        else {
                                                                                         static const tipo mod = 12582917;
125
                                                                                         tipo v;
          dforn(j, rm.l) rm.n[j+1] = rm.n[j];
126
                                                                                         mnum(tipo v = 0):v(v \mod) {}
          rm.n[0] = a.n[i]:
127
                                                                                         mnum operator +(mnum b){ return v + b.v; }
          rm.l++:
                                                                                    5
128
                                                                                         mnum operator -(mnum b){ return v \ge b.v ? v - b.v : mod - b.v + v; }
        }
129
                                                                                         mnum operator *(mnum b){ return v * b.v; }
        ll q = rm.n[b.1]*BASE + rm.n[b.1 - 1];
130
                                                                                         mnum operator ^(int n){
        ll u = q / (b.n[b.l - 1] + 1);
131
       ll v = q / b.n[b.l - 1] + 1;
                                                                                           if(!n) return 1:
                                                                                    9
132
                                                                                           return n \% 2 ? (*this)^(n/2)*(this) : (*this)^(n/2):
        while(u < v - 1){
133
                                                                                        }
          11 m = (u + v)/2;
                                                                                    11
134
                                                                                    12 };
          if(b*m \le rm) u = m;
135
          else v = m;
136
                                                                                                              2.12. Treap para set
        }
137
```

```
1 typedef int Key;
                                                                                  44
   typedef struct node *pnode;
                                                                                     ostream& operator<<(ostream &out, const pnode &t){
   struct node {
                                                                                        if(!t) return out;
       Key key;
                                                                                          return out << t->l << t->key << '' << t->r;
                                                                                  47
                                                                                     }
       int prior, size;
                                                                                  48
       pnode 1, r;
                                                                                     pnode find(pnode t, Key key){
       node(Key key = 0): key(key), prior(rand()), size(1), l(0), r(0) {}
                                                                                          if(!t) return 0;
                                                                                  50
7
                                                                                          if(key == t->key) return t;
                                                                                  51
8
   static int size(pnode p){ return p ? p->size : 0; }
                                                                                          if(key < t->key) return find(t->1, key);
                                                                                  52
                                                                                          return find(t->r, key);
   void push(pnode p){
                                                                                  53
     // modificar y propagar el dirty a los hijos aca (para lazy)
                                                                                     | }
                                                                                  54
                                                                                      struct treap {
12
   // Update function and size from children's Value
                                                                                          pnode root;
                                                                                  56
   void pull(pnode p){ // recalcular valor del nodo aca (para rmg)
                                                                                          treap(pnode root = 0): root(root) {}
                                                                                  57
     p->size = 1 + size(p->1) + size(p->r);
                                                                                          int size(){ return ::size(root); }
                                                                                  58
15
                                                                                          void insert(Key key){
16
                                                                                  59
   //junta dos arreglos
                                                                                              pnode t1, t2; split(root, key, t1, t2);
   pnode merge(pnode 1, pnode r){
                                                                                              t1 = ::merge(t1, new node(key));
     if(!1 || !r) return 1 ? 1 : r;
                                                                                              root = ::merge(t1,t2);
                                                                                  62
19
     push(1), push(r);
20
     pnode t;
                                                                                          void erase(Key key1, Key key2){
                                                                                  64
21
     if(1-prior < r-prior) 1-r = merge(1-r, r), t = 1;
                                                                                              pnode t1, t2, t3;
22
                                                                                  65
     else r\rightarrow 1 = merge(1, r\rightarrow 1), t = r;
                                                                                              split(root, key1, t1, t2);
                                                                                  66
23
     pull(t);
                                                                                              split(t2, key2, t2, t3);
                                                                                  67
24
     return t;
                                                                                              root = merge(t1, t3);
                                                                                  68
25
                                                                                  69
26
                                                                                          void erase(Key key){ ::erase(root, key); }
   //parte el arreglo en dos, l < key <= r</pre>
                                                                                  70
27
                                                                                          pnode find(Key key){ return ::find(root, key); }
   void split(pnode t, Key key, pnode &1, pnode &r){
                                                                                  71
                                                                                          Key &operator[](int pos){ return find(pos)->key; }//ojito
       if(!t) return void(l = r = 0);
                                                                                  72
29
       push(t);
                                                                                     }:
                                                                                  73
30
       if(key \le t->key) split(t->1, key, 1, t->1), r = t;
                                                                                  treap merge(treap a, treap b){ return treap(merge(a.root, b.root)); }
31
       else split(t->r, key, t->r, r), l = t;
32
                                                                                                          2.13. Treap para arreglo
       pull(t);
33
34
                                                                                   typedef ii Value;//ii(profundidad, nodo)
35
   void erase(pnode &t, Key key){
                                                                                   typedef struct node *pnode;
36
       if(!t) return;
37
                                                                                     struct node{
       push(t):
                                                                                          Value val, mini;
38
       if(key == t->key) t = merge(t->1, t->r);
                                                                                          int dirty;
39
                                                                                   5
       else if(key < t->key) erase(t->1, key);
                                                                                          int prior, size;
40
                                                                                   6
       else erase(t->r, key);
41
                                                                                          pnode 1,r,parent;
       if(t) pull(t);
                                                                                          node(Value val): val(val), mini(val), dirty(0), prior(rand()), size
42
43 }
                                                                                              (1), 1(0), r(0), parent(0) {}
```

```
9 | };
                                                                                    50
   static int size(pnode p) { return p ? p->size : 0; }
                                                                                   51
   void push(pnode p) {//propagar dirty a los hijos(aca para lazy)
                                                                                    52
     p->val.fst+=p->dirty;
     p->mini.fst+=p->dirty;
                                                                                   54
     if(p->1) p->1->dirty+=p->dirty;
     if(p->r) p->r->dirty+=p->dirty;
                                                                                    56
     p->dirty=0;
17
   static Value mini(pnode p) { return p ? push(p), p->mini : ii(1e9, -1);
                                                                                    60
    // Update function and size from children's Value
                                                                                   61
   void pull(pnode p) {//recalcular valor del nodo aca (para rmq)
     p->size = 1 + size(p->1) + size(p->r);
     p->mini = min(min(p->val, mini(p->l)), mini(p->r));//operacion del rmq
                                                                                    64
                                                                                    65
     p->parent=0;
     if(p->1) p->1->parent=p;
     if(p->r) p->r->parent=p;
25
26
   //junta dos arreglos
   pnode merge(pnode 1, pnode r) {
     if (!1 || !r) return 1 ? 1 : r;
29
     push(1), push(r);
30
     pnode t;
31
     if (1->prior < r->prior) 1->r=merge(1->r, r), t = 1;
     else r\rightarrow l=merge(1, r\rightarrow 1), t = r;
33
     pull(t);
     return t;
35
36
    //parte el arreglo en dos, sz(l)==tam
                                                                                    5
   void split(pnode t, int tam, pnode &1, pnode &r) {
                                                                                    6
     if (!t) return void(1 = r = 0);
39
     push(t):
40
                                                                                    8
     if (tam \le size(t->1)) split(t->1, tam, 1, t->1), r = t;
41
                                                                                    9
     else split(t->r, tam - 1 - size(t->l), t->r, r), l = t;
                                                                                    10
     pull(t);
43
                                                                                   11
44
                                                                                   12
   pnode at(pnode t, int pos) {
                                                                                   13
     if(!t) exit(1);
                                                                                   14
     push(t);
47
                                                                                   15
     if(pos == size(t->1)) return t;
48
                                                                                   16
     if(pos < size(t->1)) return at(t->1, pos);
                                                                                   17
```

```
return at(t->r, pos - 1 - size(t->1));
   int getpos(pnode t){//inversa de at
     if(!t->parent) return size(t->1);
     if(t==t->parent->l) return getpos(t->parent)-size(t->r)-1;
     return getpos(t->parent)+size(t->1)+1;
   void split(pnode t, int i, int j, pnode &1, pnode &m, pnode &r) {
     split(t, i, l, t), split(t, j-i, m, r);}
   Value get(pnode &p, int i, int j){//like rmg
     pnode 1,m,r;
       split(p, i, j, l, m, r);
       Value ret=mini(m):
       p=merge(1, merge(m, r));
       return ret;
   void print(const pnode &t) {//for debugging
     if(!t) return;
       push(t):
       print(t->1);
       cout << t->val.fst << '';
       print(t->r);
72 }
```

2.14. Convex Hull Trick

```
struct Line{tipo m,h;};
tipo inter(Line a, Line b){
      tipo x=b.h-a.h, y=a.m-b.m;
      return x/y+(x\%?!((x>0)^(y>0)):0);//==ceil(x/y)
  }
  struct CHT {
    vector<Line> c;
    bool mx;
    int pos;
    CHT(bool mx=0):mx(mx),pos(0){}//mx=1 si las query devuelven el max
    inline Line acc(int i){return c[c[0].m>c.back().m? i : sz(c)-1-i];}
    inline bool irre(Line x, Line y, Line z){
      return c[0].m>z.m? inter(y, z) <= inter(x, y)
                           : inter(y, z) >= inter(x, y);
    void add(tipo m, tipo h) {//0(1), los m tienen que entrar ordenados
          if (mx) m*=-1, h*=-1;
```

```
Line l=(Line){m, h};
18
           if(sz(c) && m==c.back().m) { l.h=min(h, c.back().h), c.pop_back
19
                (); if(pos) pos--; }
           while(sz(c) \ge 2 \&\& irre(c[sz(c)-2], c[sz(c)-1], 1)) { c.pop_back
20
                (); if(pos) pos--; }
           c.pb(1);
21
22
     inline bool fbin(tipo x, int m) {return inter(acc(m), acc(m+1))>x;}
23
     tipo eval(tipo x){
24
       int n = sz(c);
25
       //query con x no ordenados O(lgn)
26
       int a=-1, b=n-1;
27
       while(b-a>1) { int m = (a+b)/2;
28
         if(fbin(x, m)) b=m:
29
         else a=m:
30
       }
31
       return (acc(b).m*x+acc(b).h)*(mx?-1:1);
32
           //query 0(1)
33
       while(pos>0 && fbin(x, pos-1)) pos--;
34
       while(pos<n-1 && !fbin(x, pos)) pos++;</pre>
35
       return (acc(pos).m*x+acc(pos).h)*(mx?-1:1);
36
37
  } ch;
38
```

2.15. Convex Hull Trick (Dynamic)

```
const ll is_query = -(1LL<<62);</pre>
  struct Line {
2
       ll m, b;
3
       mutable multiset<Line>::iterator it;
4
       const Line *succ(multiset<Line>::iterator it) const;
5
       bool operator<(const Line& rhs) const {</pre>
6
           if (rhs.b != is_query) return m < rhs.m;</pre>
7
           const Line *s=succ(it);
8
           if(!s) return 0;
9
           11 x = rhs.m;
10
           return b - s->b < (s->m - m) * x;
11
       }
12
13
  struct HullDynamic : public multiset<Line>{ // will maintain upper hull
       for maximum
       bool bad(iterator y) {
15
           iterator z = next(y);
16
```

```
if (y == begin()) {
17
               if (z == end()) return 0;
18
               return y->m == z->m && y->b <= z->b;
19
20
           iterator x = prev(y);
21
           if (z == end()) return y->m == x->m && y->b <= x->b;
22
           return (x-b - y-b)*(z-m - y-m) >= (y-b - z-b)*(y-m - x-m)
23
               );
       }
24
       iterator next(iterator y){return ++y;}
25
       iterator prev(iterator y){return --y;}
26
       void insert_line(ll m, ll b) {
27
           iterator y = insert((Line) { m, b });
28
           y->it=y;
           if (bad(y)) { erase(y); return; }
           while (next(y) != end() && bad(next(y))) erase(next(y));
           while (y != begin() && bad(prev(y))) erase(prev(y));
32
       }
33
       ll eval(ll x) {
34
           Line l = *lower_bound((Line) { x, is_query });
           return 1.m * x + 1.b;
36
       }
37
   }h;
38
   const Line *Line::succ(multiset<Line>::iterator it) const{
       return (++it==h.end()? NULL : &*it);}
```

2.16. Gain-Cost Set

```
1 //esta estructura mantiene pairs(beneficio, costo)
2 //de tal manera que en el set quedan ordenados
   //por beneficio Y COSTO creciente. (va borrando los que no son optimos)
   struct V{
4
     int gain, cost;
     bool operator<(const V &b)const{return gain<b.gain;}</pre>
   };
7
   set<V> s;
8
   void add(V x){
     set<V>::iterator p=s.lower_bound(x);//primer elemento mayor o igual
     if(p!=s.end() && p->cost <= x.cost) return;//ya hay uno mejor
11
     p=s.upper_bound(x);//primer elemento mayor
12
    if(p!=s.begin()){//borro todos los peores (<=beneficio y >=costo)
13
       --p;//ahora es ultimo elemento menor o igual
14
       while(p->cost >= x.cost){
15
```

9

```
if(p==s.begin()){s.erase(p); break;}
s.erase(p--);
}
s.insert(x);
int get(int gain){//minimo costo de obtener tal ganancia
set<V>::iterator p=s.lower_bound((V){gain, 0});
return p==s.end()? INF : p->cost;}
```

2.17. Set con búsqueda binaria

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
typedef tree<int,null_type,less<int>,//key,mapped type, comparator

rb_tree_tag,tree_order_statistics_node_update> set_t;
//find_by_order(i) devuelve iterador al i-esimo elemento
//order_of_key(k): devuelve la pos del lower bound de k
//Ej: 12, 100, 505, 1000, 10000.
//order_of_key(100) == 0, order_of_key(100) == 1,
//order_of_key(707) == 3, order_of_key(9999999) == 5
```

3. Algorítmos

3.1. Longest Increasing Subsecuence

```
//Para non-increasing, cambiar comparaciones y revisar busq binaria
   //Given an array, paint it in the least number of colors so that each
       color turns to a non-increasing subsequence.
  //Solution:Min number of colors=Length of the longest increasing
       subsequence
  int N, a[MAXN];//secuencia y su longitud
  ii d[MAXN+1];//d[i]=ultimo valor de la subsecuencia de tamanio i
   int p[MAXN];//padres
  vector<int> R;//respuesta
   void rec(int i){
    if(i==-1) return:
    R.push_back(a[i]);
10
    rec(p[i]);
11
12
  int lis(){//O(nlogn)
     d[0] = ii(-INF, -1); forn(i, N) d[i+1]=ii(INF, -1);
```

```
forn(i, N){
15
       int j = upper_bound(d, d+N+1, ii(a[i], INF))-d;
16
       if (d[j-1].first < a[i]&&a[i] < d[j].first){</pre>
17
         p[i]=d[j-1].second;
18
         d[j] = ii(a[i], i);
19
20
     }
21
     R.clear();
22
     dforn(i, N+1) if(d[i].first!=INF){
23
       rec(d[i].second);//reconstruir
       reverse(R.begin(), R.end());
25
       return i;//longitud
26
    }
27
     return 0;
28
29 }
                      3.2. Alpha-Beta prunning
1 | 11 alphabeta(State &s, bool player = true, int depth = 1e9, 11 alpha = -
       INF, 11 beta = INF) { //player = true -> Maximiza
       if(s.isFinal()) return s.score;
     //~ if (!depth) return s.heuristic();
3
       vector<State> children;
       s.expand(player, children);
5
       int n = children.size();
6
       forn(i, n) {
           ll v = alphabeta(children[i], !player, depth-1, alpha, beta);
8
           if(!player) alpha = max(alpha, v);
9
           else beta = min(beta, v);
10
           if(beta <= alpha) break;</pre>
11
12
       return !player ? alpha : beta;}
13
                          3.3. Mo's algorithm
int n,sq;
struct Qu{//queries [1, r]
       //intervalos cerrado abiertos !!! importante!!
       int 1, r, id;
   }qs[MAXN];
  int ans[MAXN], curans;//ans[i]=ans to ith query
   bool bymos(const Qu &a, const Qu &b){
       if(a.l/sq!=b.l/sq) return a.l<b.1;
```

return (a.l/sq)&1? a.r<b.r : a.r>b.r;

```
10 }
   void mos(){
11
       forn(i, t) qs[i].id=i;
12
       sort(qs, qs+t, bymos);
13
       int cl=0, cr=0;
14
       sq=sqrt(n);
15
       curans=0;
16
       forn(i, t){ //intervalos cerrado abiertos !!! importante!!
17
            Qu &q=qs[i];
18
            while(cl>q.1) add(--cl);
19
            while(cr<q.r) add(cr++);</pre>
20
            while(cl<q.1) remove(cl++);</pre>
21
            while(cr>q.r) remove(--cr);
22
            ans[q.id]=curans;
23
       }
24
25 }
```

4. Strings

4.1. Manacher

```
1 int d1[MAXN];//d1[i]=long del maximo palindromo impar con centro en i
1 int d2[MAXN];//d2[i]=analogo pero para longitud par
   //0 1 2 3 4
   //a a b c c <--d1[2]=3
   //a a b b <--d2[2]=2 (estan uno antes)
   void manacher(){
     int 1=0, r=-1, n=sz(s);
7
     forn(i, n){
       int k=(i>r? 1 : min(d1[l+r-i], r-i));
9
       while(i+k \le k i-k >= 0 \& s[i+k] == s[i-k]) ++k;
10
       d1[i] = k--;
11
       if(i+k > r) l=i-k, r=i+k;
12
     }
13
     1=0, r=-1;
14
     forn(i, n){
15
       int k=(i>r? 0 : min(d2[l+r-i+1], r-i+1))+1;
16
       while(i+k-1 \le k = 0 \ k \le [i+k-1] == s[i-k]) k++;
17
       d2[i] = --k;
18
       if(i+k-1 > r) l=i-k, r=i+k-1;
19
     }
20
```

4.2. KMP

```
string T;//cadena donde buscar(where)
string P;//cadena a buscar(what)
  int b[MAXLEN];//back table b[i] maximo borde de [0..i)
   void kmppre(){//by gabina with love
       int i =0, j=-1; b[0]=-1;
       while(i<sz(P)){</pre>
           while(j>=0 && P[i] != P[j]) j=b[j];
           i++, j++, b[i] = j;
8
       }
9
   }
10
   void kmp(){
11
       int i=0, j=0;
12
       while(i<sz(T)){</pre>
13
           while(j>=0 && T[i]!=P[j]) j=b[j];
           i++, j++;
15
           if(j==sz(P)) printf("Puisufounduatuindexu/duinuT\n", i-j), j=b[j
16
       }
17
   }
18
19
   int main(){
20
       cout << "T=";
21
       cin >> T;
22
       cout << "P=";
                                 4.3. Trie
1 | struct trie{
     map<char, trie> m;
     void add(const string &s, int p=0){
       if(s[p]) m[s[p]].add(s, p+1);
    }
5
     void dfs(){
6
       //Do stuff
       forall(it, m)
         it->second.dfs();
9
    }
10
11 | };
                   4.4. Suffix Array (largo, nlogn)
1 #define MAX_N 1000
#define rBOUND(x) (x<n? r[x] : 0)</pre>
3 //sa will hold the suffixes in order.
```

```
4 int sa[MAX_N], r[MAX_N], n;
   string s; //input string, n=sz(s)
   int f[MAX_N], tmpsa[MAX_N];
   void countingSort(int k){
     zero(f);
9
     forn(i, n) f[rBOUND(i+k)]++;
     int sum=0:
11
     forn(i, max(255, n)){
12
       int t=f[i]; f[i]=sum; sum+=t;}
13
     forn(i, n)
14
       tmpsa[f[rBOUND(sa[i]+k)]++]=sa[i];
15
     memcpy(sa, tmpsa, sizeof(sa));
16
17
   void constructsa(){\frac{1}{0} \text{ n}}
18
     n=sz(s);
19
     forn(i, n) sa[i]=i, r[i]=s[i];
20
     for(int k=1; k<n; k<<=1){</pre>
21
       countingSort(k), countingSort(0);
22
       int rank, tmpr[MAX_N];
23
       tmpr[sa[0]]=rank=0;
24
       forr(i, 1, n)
25
         tmpr[sa[i]] = r[sa[i-1]] & r[sa[i]+k] = r[sa[i-1]+k])?
26
             rank : ++rank;
       memcpy(r, tmpr, sizeof(r));
27
       if(r[sa[n-1]]==n-1) break;
28
29
30
   void print(){//for debug
31
     forn(i, n)
32
       cout << i << ''' <<
33
       s.substr(sa[i], s.find( '$', sa[i])-sa[i]) << endl;}
34
             4.5. String Matching With Suffix Array
   //returns (lowerbound, upperbound) of the search
  ii stringMatching(string P){ //O(sz(P)lgn)
     int lo=0, hi=n-1, mid=lo;
3
     while(lo<hi){
```

```
//returns (lowerbound, upperbound) of the search
ii stringMatching(string P){ //O(sz(P)lgn)}
int lo=0, hi=n-1, mid=lo;
while(lo<hi){
    mid=(lo+hi)/2;
    int res=s.compare(sa[mid], sz(P), P);
    if(res>=0) hi=mid;
else lo=mid+1;
```

```
9
     if(s.compare(sa[lo], sz(P), P)!=0) return ii(-1, -1);
10
     ii ans; ans.fst=lo;
11
     lo=0, hi=n-1, mid;
12
     while(lo<hi){</pre>
13
       mid=(lo+hi)/2;
       int res=s.compare(sa[mid], sz(P), P);
       if(res>0) hi=mid;
       else lo=mid+1;
18
     if(s.compare(sa[hi], sz(P), P)!=0) hi--;
19
     ans.snd=hi:
20
     return ans:
21
22 }
                4.6. LCP (Longest Common Prefix)
 1 //Calculates the LCP between consecutives suffixes in the Suffix Array.
   //LCP[i] is the length of the LCP between sa[i] and sa[i-1]
   int LCP[MAX_N], phi[MAX_N], PLCP[MAX_N];
   void computeLCP(){//0(n)}
     phi[sa[0]]=-1:
     forr(i, 1, n) phi[sa[i]]=sa[i-1];
     int L=0;
     forn(i, n){
8
       if(phi[i]==-1) {PLCP[i]=0; continue;}
9
       while(s[i+L]==s[phi[i]+L]) L++;
10
       PLCP[i]=L;
11
       L=max(L-1, 0);
12
13
     forn(i, n) LCP[i]=PLCP[sa[i]];
14
15 }
                              4.7. Corasick
1
   struct trie{
2
     map<char, trie> next;
     trie* tran[256];//transiciones del automata
     int idhoja, szhoja;//id de la hoja o 0 si no lo es
    //link lleva al sufijo mas largo, nxthoja lleva al mas largo pero que
```

es hoja

7

trie *padre, *link, *nxthoja;

char pch;//caracter que conecta con padre

```
trie(): tran(), idhoja(), padre(), link() {}
                                                                                  <sub>5</sub> };
9
     void insert(const string &s, int id=1, int p=0){//id>0!!!
                                                                                    const int MAXLEN = 10010;
10
       if(p \le z(s)){
                                                                                    state st[MAXLEN*2];
11
         trie &ch=next[s[p]];
                                                                                     int sz, last;
12
         tran[(int)s[p]]=&ch;
                                                                                     void sa_init() {
13
         ch.padre=this, ch.pch=s[p];
                                                                                      forn(i,sz) st[i].next.clear();
14
         ch.insert(s, id, p+1);
                                                                                     sz = last = 0;
15
                                                                                     st[0].len = 0;
16
       else idhoja=id, szhoja=sz(s);
                                                                                      st[0].link = -1;
17
                                                                                       ++sz;
                                                                                  14
18
     trie* get_link() {
                                                                                    | }
                                                                                  15
19
       if(!link){
                                                                                     // Es un DAG de una sola fuente y una sola hoja
20
                                                                                  17 // cantidad de endpos = cantidad de apariciones = cantidad de caminos de
         if(!padre) link=this;//es la raiz
21
         else if(!padre->padre) link=padre;//hijo de la raiz
                                                                                          la clase al nodo terminal
22
         else link=padre->get_link()->get_tran(pch);
                                                                                  18 // cantidad de miembros de la clase = st[v].len-st[st[v].link].len (v>0)
23
                                                                                          = caminos del inicio a la clase
24
       return link; }
                                                                                  19 // El arbol de los suffix links es el suffix tree de la cadena invertida
25
     trie* get_tran(int c) {
                                                                                         . La string de la arista link(v)->v son los caracteres que difieren
26
       if(!tran[c]) tran[c] = !padre? this : this->get_link()->get_tran(c);
                                                                                     void sa extend (char c) {
27
       return tran[c]; }
                                                                                      int cur = sz++;
28
     trie *get_nxthoja(){
                                                                                       st[cur].len = st[last].len + 1;
29
       if(!nxthoja) nxthoja = get_link()->idhoja? link : link->nxthoja;
                                                                                       // en cur agregamos la posicion que estamos extendiendo
30
       return nxthoja; }
                                                                                      //podria agregar tambien un identificador de las cadenas a las cuales
                                                                                 24
31
     void print(int p){
                                                                                           pertenece (si hay varias)
32
       if(idhoja) cout << "found" << idhoja << "___at_position_" << p-
                                                                                       int p;
                                                                                 25
33
           szhoja << endl;
                                                                                       for (p=last; p!=-1 && !st[p].next.count(c); p=st[p].link) // modificar
                                                                                  26
       if(get_nxthoja()) get_nxthoja()->print(p); }
                                                                                            esta linea para hacer separadores unicos entre varias cadenas (c
34
     void matching(const string &s, int p=0){
                                                                                           =='$')
35
       print(p); if(p<sz(s)) get_tran(s[p])->matching(s, p+1); }
                                                                                         st[p].next[c] = cur;
                                                                                 27
36
   }tri;
                                                                                       if (p == -1)
37
                                                                                         st[cur].link = 0;
                                                                                 29
38
                                                                                       else {
                                                                                  30
39
   int main(){
                                                                                         int q = st[p].next[c];
                                                                                 31
     tri=trie()://clear
                                                                                         if (st[p].len + 1 == st[q].len)
41
     tri.insert("ho", 1);
                                                                                           st[cur].link = q;
                                                                                 33
42
     tri.insert("hoho", 2);
                                                                                         else {
                                                                                  34
                                                                                           int clone = sz++:
                               Suffix Automaton
                                                                                           // no le ponemos la posicion actual a clone sino indirectamente
                                                                                               por el link de cur
                                                                                           st[clone].len = st[p].len + 1;
  struct state {
                                                                                           st[clone].next = st[q].next;
     int len, link;
2
                                                                                           st[clone].link = st[q].link;
     map<char,int> next;
                                                                                  39
                                                                                           for (; p!=-1 && st[p].next.count(c) && st[p].next[c]==q; p=st[p].
     state() { }
                                                                                 40
```

4.9. Z Function

```
char s[MAXN];
  int z[MAXN]; // z[i] = i==0 ? 0 : max k tq s[0,k) match with s[i,i+k)
   void z_function(char s[],int z[]) {
       int n = strlen(s);
4
       forn(i, n) z[i]=0;
5
      for (int i = 1, l = 0, r = 0; i < n; ++i) {
6
           if (i \le r) z[i] = min (r - i + 1, z[i - 1]);
           while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]]) ++z[i];
8
           if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
9
       }
10
  }
11
12
  int main() {
13
       ios::sync_with_stdio(0);
14
```

5. Geometría

5.1. Punto

```
struct pto{
     double x, y;
     pto(double x=0, double y=0):x(x),y(y){}
3
     pto operator+(pto a){return pto(x+a.x, y+a.y);}
4
     pto operator-(pto a){return pto(x-a.x, y-a.y);}
     pto operator+(double a){return pto(x+a, y+a);}
6
     pto operator*(double a){return pto(x*a, y*a);}
     pto operator/(double a){return pto(x/a, y/a);}
     //dot product, producto interno:
9
     double operator*(pto a){return x*a.x+y*a.y;}
10
     //module of the cross product or vectorial product:
11
     //if a is less than 180 clockwise from b, a^b>0
12
     double operator^(pto a){return x*a.y-y*a.x;}
13
     //returns true if this is at the left side of line gr
14
```

```
bool left(pto q, pto r){return ((q-*this)^(r-*this))>0;}
     bool operator<(const pto &a) const{return x<a.x-EPS || (abs(x-a.x)<EPS
16
          && y<a.y-EPS);}
   bool operator==(pto a){return abs(x-a.x)<EPS && abs(y-a.y)<EPS;}
     double norm(){return sqrt(x*x+y*y);}
     double norm_sq(){return x*x+y*y;}
19
20
   double dist(pto a, pto b){return (b-a).norm();}
   typedef pto vec;
   double angle(pto a, pto o, pto b){
    pto oa=a-o, ob=b-o;
     return atan2(oa^ob, oa*ob);}
26
27
   //rotate p by theta rads CCW w.r.t. origin (0,0)
   pto rotate(pto p, double theta){
    return pto(p.x*cos(theta)-p.y*sin(theta),
        p.x*sin(theta)+p.y*cos(theta));
31
32 }
```

5.2. Orden radial de puntos

```
struct Cmp{//orden total de puntos alrededor de un punto r
     pto r;
     Cmp(pto r):r(r) {}
     int cuad(const pto &a) const{
4
       if (a.x > 0 \&\& a.y >= 0) return 0;
5
       if(a.x <= 0 && a.y > 0)return 1;
6
       if(a.x < 0 \&\& a.y <= 0)return 2;
       if(a.x >= 0 \&\& a.y < 0)return 3;
       assert(a.x ==0 && a.y==0);
9
       return -1;
10
     }
11
     bool cmp(const pto&p1, const pto&p2)const{
12
       int c1 = cuad(p1), c2 = cuad(p2);
13
       if(c1==c2) return p1.y*p2.x<p1.x*p2.y;</pre>
14
           else return c1 < c2;
15
     }
16
       bool operator()(const pto&p1, const pto&p2) const{
17
       return cmp(pto(p1.x-r.x,p1.y-r.y),pto(p2.x-r.x,p2.y-r.y));
18
19
20 };
```

20

5.3. Line

```
int sgn(ll x){return x<0? -1 : !!x;}
   struct line{
     line() {}
3
     double a,b,c;//Ax+By=C
   //pto MUST store float coordinates!
     line(double a, double b, double c):a(a),b(b),c(c){}
    line(pto p, pto q): a(q.y-p.y), b(p.x-q.x), c(a*p.x+b*p.y) {}
     int side(pto p){return sgn(ll(a) * p.x + ll(b) * p.y - c);}
9
   bool parallels(line 11, line 12){return abs(11.a*12.b-12.a*11.b)<EPS;}
   pto inter(line 11, line 12){//intersection
     double det=11.a*12.b-12.a*11.b;
12
     if(abs(det) < EPS) return pto(INF, INF); //parallels</pre>
    return pto(12.b*11.c-11.b*12.c, 11.a*12.c-12.a*11.c)/det;
14
15 }
                              5.4. Segment
```

```
struct segm{
     pto s,f;
2
     segm(pto s, pto f):s(s), f(f) {}
     pto closest(pto p) {//use for dist to point
4
        double 12 = dist_sq(s, f);
        if(12==0.) return s;
6
        double t = ((p-s)*(f-s))/12;
        if (t<0.) return s;//not write if is a line
        else if(t>1.)return f;//not write if is a line
9
        return s+((f-s)*t);
10
    }
11
       bool inside(pto p){return abs(dist(s, p)+dist(p, f)-dist(s, f))<EPS</pre>
12
           ;}
13
   pto inter(segm s1, segm s2){
    pto r=inter(line(s1.s, s1.f), line(s2.s, s2.f));
       if(s1.inside(r) && s2.inside(r)) return r;
     return pto(INF, INF);
19 }
```

5.5. Rectangle

```
struct rect{
```

```
//lower-left and upper-right corners
     pto lw, up;
3
4
  |};
   //returns if there's an intersection and stores it in r
   bool inter(rect a, rect b, rect &r){
     r.lw=pto(max(a.lw.x, b.lw.x), max(a.lw.y, b.lw.y));
     r.up=pto(min(a.up.x, b.up.x), min(a.up.y, b.up.y));
   //check case when only a edge is common
     return r.lw.x<r.up.x && r.lw.y<r.up.y;</pre>
11 }
                          5.6. Polygon Area
double area(vector<pto> &p){//0(sz(p))
     double area=0;
    forn(i, sz(p)) area+=p[i]^p[(i+1) %z(p)];
     //if points are in clockwise order then area is negative
     return abs(area)/2;
5
   }
6
7 //Area ellipse = M_PI*a*b where a and b are the semi axis lengths
_{8} //Area triangle = sqrt(s*(s-a)(s-b)(s-c)) where s=(a+b+c)/2
                               5.7. Circle
vec perp(vec v){return vec(-v.y, v.x);}
  line bisector(pto x, pto y){
     line l=line(x, y); pto m=(x+y)/2;
     return line(-1.b, 1.a, -1.b*m.x+1.a*m.y);
   }
5
   struct Circle{
6
     pto o;
     double r;
     Circle(pto x, pto y, pto z){
9
       o=inter(bisector(x, y), bisector(y, z));
10
       r=dist(o, x);
11
     }
12
     pair<pto, pto> ptosTang(pto p){
13
       pto m=(p+o)/2;
14
       tipo d=dist(o, m);
15
       tipo a=r*r/(2*d);
16
       tipo h=sqrt(r*r-a*a);
17
       pto m2=o+(m-o)*a/d;
18
       vec per=perp(m-o)/d;
19
```

return make_pair(m2-per*h, m2+per*h);

```
}
21
   };
^{22}
   //finds the center of the circle containing p1 and p2 with radius r
    //as there may be two solutions swap p1, p2 to get the other
   bool circle2PtsRad(pto p1, pto p2, double r, pto &c){
           double d2=(p1-p2).norm_sq(), det=r*r/d2-0.25;
26
           if(det<0) return false;
27
           c=(p1+p2)/2+perp(p2-p1)*sqrt(det);
28
           return true;
29
30
   #define sqr(a) ((a)*(a))
   #define feq(a,b) (fabs((a)-(b))<EPS)</pre>
   pair<tipo, tipo> ecCuad(tipo a, tipo b, tipo c){//a*x*x+b*x+c=0
     tipo dx = sqrt(b*b-4.0*a*c);
     return make_pair((-b + dx)/(2.0*a), (-b - dx)/(2.0*a));
35
36
   pair<pto, pto> interCL(Circle c, line 1){
37
     bool sw=false;
38
     if((sw=feq(0,1.b))){
39
     swap(1.a, 1.b);
     swap(c.o.x, c.o.y);
41
42
     pair<tipo, tipo> rc = ecCuad(
43
     sgr(l.a)+sgr(l.b),
44
     2.0*1.a*1.b*c.o.y-2.0*(sgr(1.b)*c.o.x+1.c*1.a),
45
     sqr(1.b)*(sqr(c.o.x)+sqr(c.o.y)-sqr(c.r))+sqr(1.c)-2.0*1.c*1.b*c.o.y
46
     );
47
     pair<pto, pto> p( pto(rc.first, (l.c - l.a * rc.first) / l.b),
48
                pto(rc.second, (1.c - 1.a * rc.second) / 1.b) );
49
     if(sw){
50
     swap(p.first.x, p.first.y);
5.1
     swap(p.second.x, p.second.y);
52
53
     return p;
54
55
   pair<pto, pto> interCC(Circle c1, Circle c2){
     line 1:
57
     1.a = c1.o.x-c2.o.x:
58
     1.b = c1.o.y-c2.o.y;
     1.c = (sqr(c2.r) - sqr(c1.r) + sqr(c1.o.x) - sqr(c2.o.x) + sqr(c1.o.y)
     -sqr(c2.o.y))/2.0;
61
     return interCL(c1, 1);
63 }
```

5.8. Point in Poly

```
1 //checks if v is inside of P, using ray casting
   //works with convex and concave.
   //excludes boundaries, handle it separately using segment.inside()
   bool inPolygon(pto v, vector<pto>& P) {
     bool c = false;
    forn(i, sz(P)){
       int j=(i+1) \%z(P);
      if((P[j].y>v.y) != (P[i].y > v.y) &&
     (v.x < (P[i].x - P[j].x) * (v.y-P[j].y) / (P[i].y - P[j].y) + P[j].x))
         c = !c;
10
    }
11
     return c;
12
13 }
```

5.9. Point in Convex Poly log(n)

```
void normalize(vector<pto> &pt){//delete collinear points first!
     //this makes it clockwise:
       if(pt[2].left(pt[0], pt[1])) reverse(pt.begin(), pt.end());
     int n=sz(pt), pi=0;
4
     forn(i, n)
       if(pt[i].x<pt[pi].x || (pt[i].x==pt[pi].x && pt[i].y<pt[pi].y))</pre>
         pi=i;
     vector<pto> shift(n);//puts pi as first point
       forn(i, n) shift[i]=pt[(pi+i) %n];
9
       pt.swap(shift);
10
11
   bool inPolygon(pto p, const vector<pto> &pt){
     //call normalize first!
13
     if(p.left(pt[0], pt[1]) || p.left(pt[sz(pt)-1], pt[0])) return false;
14
     int a=1, b=sz(pt)-1;
15
     while(b-a>1){
       int c=(a+b)/2;
       if(!p.left(pt[0], pt[c])) a=c;
       else b=c;
19
20
     return !p.left(pt[a], pt[a+1]);
21
22 }
```

5.10. Convex Check CHECK

1 | bool isConvex(vector<int> &p){//O(N), delete collinear points!

```
int N=sz(p);
                                                                                  1 //plot a line approximation in a 2d map
2
                                                                                    void bresenham(pto a, pto b){
     if(N<3) return false;
3
     bool isLeft=p[0].left(p[1], p[2]);
                                                                                      pto d=b-a; d.x=abs(d.x), d.y=abs(d.y);
4
     forr(i, 1, N)
                                                                                      pto s(a.x<b.x? 1: -1, a.y<b.y? 1: -1);
       if(p[i].left(p[(i+1) \mathbb{N}], p[(i+2) \mathbb{N}])!=isLeft)
                                                                                      int err=d.x-d.v;
         return false;
                                                                                      while(1){
7
     return true; }
                                                                                        m[a.x][a.y]=1;//plot
                                                                                        if(a==b) break;
                           5.11. Convex Hull
                                                                                        int e2=err;
                                                                                       if(e2 >= 0) err-=2*d.y, a.x+=s.x;
   //stores convex hull of P in S, CCW order
                                                                                        if(e2 <= 0) err+= 2*d.x, a.y+= s.y;
                                                                                 11
   //left must return >=0 to delete collinear points!
                                                                                 12
   void CH(vector<pto>& P, vector<pto> &S){
                                                                                 13 }
     S.clear();
4
     sort(P.begin(), P.end());//first x, then y
                                                                                                           5.14. Rotate Matrix
5
     forn(i, sz(P)){//lower hull
6
       while(sz(S) \ge 2 \&\& S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back();
                                                                                  1 //rotates matrix t 90 degrees clockwise
       S.pb(P[i]);
                                                                                  //using auxiliary matrix t2(faster)
8
     }
                                                                                    void rotate(){
9
     S.pop_back();
                                                                                      forn(x, n) forn(y, n)
10
     int k=sz(S);
                                                                                        t2[n-y-1][x]=t[x][y];
                                                                                 5
11
     dforn(i, sz(P)){//upper hull
                                                                                      memcpy(t, t2, sizeof(t));
12
       while(sz(S) \ge k+2 \&\& S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back
13
           ();
                                                                                             5.15. Interseccion de Circulos en n3log(n)
       S.pb(P[i]);
14
15
                                                                                  1 struct event {
     S.pop_back();
16
                                                                                        double x; int t;
17
                                                                                        event(double xx, int tt) : x(xx), t(tt) {}
                          5.12. Cut Polygon
                                                                                        bool operator <(const event &o) const { return x < o.x; }</pre>
                                                                                  4
                                                                                    };
                                                                                  5
1 //cuts polygon Q along the line ab
                                                                                    typedef vector<Circle> VC;
   //stores the left side (swap a, b for the right one) in P
                                                                                    typedef vector<event> VE;
   void cutPolygon(pto a, pto b, vector<pto> Q, vector<pto> &P){
     P.clear();
                                                                                    double cuenta(VE &v, double A,double B) {
4
     forn(i, sz(Q)){
                                                                                        sort(v.begin(), v.end());
       double left1=(b-a)^(Q[i]-a), left2=(b-a)^(Q[(i+1) / z(Q)]-a);
                                                                                        double res = 0.0, lx = ((v.empty())?0.0:v[0].x);
                                                                                 11
       if(left1>=0) P.pb(Q[i]);
7
                                                                                        int contador = 0;
                                                                                 12
       if(left1*left2<0)</pre>
                                                                                 13
                                                                                        forn(i,sz(v)) {
         P.pb(inter(line(Q[i], Q[(i+1) \%z(Q)]), line(a, b)));
                                                                                            //interseccion de todos (contador == n), union de todos (
                                                                                 14
     }
                                                                                                contador > 0)
10
11 }
                                                                                            //conjunto de puntos cubierto por exacta k Circulos (contador ==
                                                                                 15
                            5.13. Bresenham
                                                                                            if (contador == n) res += v[i].x - lx;
                                                                                 16
```

```
contador += v[i].t. lx = v[i].x:
17
       }
18
       return res;
19
20
    // Primitiva de sgrt(r*r - x*x) como funcion double de una variable x.
21
   inline double primitiva(double x,double r) {
22
       if (x \ge r) return r*r*M_PI/4.0;
23
       if (x <= -r) return -r*r*M_PI/4.0;
24
       double raiz = sqrt(r*r-x*x);
25
       return 0.5 * (x * raiz + r*r*atan(x/raiz));
26
27
   double interCircle(VC &v) {
28
       vector<double> p; p.reserve(v.size() * (v.size() + 2));
29
       forn(i,sz(v)) p.push_back(v[i].c.x + v[i].r), p.push_back(v[i].c.x
30
           - v[i].r):
       forn(i,sz(v)) forn(j,i) {
31
           Circle &a = v[i], b = v[j];
32
           double d = (a.c - b.c).norm();
33
           if (fabs(a.r - b.r) < d \&\& d < a.r + b.r) {
34
               double alfa = acos((sgr(a.r) + sgr(d) - sgr(b.r)) / (2.0 * d)
35
                     * a.r));
               pto vec = (b.c - a.c) * (a.r / d);
36
               p.pb((a.c + rotate(vec, alfa)).x), p.pb((a.c + rotate(vec, -
37
                    alfa)).x);
38
39
       sort(p.begin(), p.end());
40
       double res = 0.0;
41
       forn(i,sz(p)-1) {
42
           const double A = p[i], B = p[i+1];
43
           VE ve; ve.reserve(2 * v.size());
44
           forn(j,sz(v)) {
45
               const Circle &c = v[j];
46
               double arco = primitiva(B-c.c.x,c.r) - primitiva(A-c.c.x,c.r
47
                    );
               double base = c.c.y * (B-A);
48
               ve.push_back(event(base + arco,-1));
49
               ve.push_back(event(base - arco, 1));
50
51
           res += cuenta(ve,A,B);
52
53
       return res;
54
55 |}
```

6. Matemática

6.1. Identidades

$$\sum_{i=0}^{n} {n \choose i} = 2^{n}$$

$$\sum_{i=0}^{n} i {n \choose i} = n * 2^{n-1}$$

$$\sum_{i=m}^{n} i = \frac{n(n+1)}{2} - \frac{m(m-1)}{2} = \frac{(n+1-m)(n+m)}{2}$$

$$\sum_{i=0}^{n} i = \sum_{i=1}^{n} i = \frac{n(n+1)}{2}$$

$$\sum_{i=0}^{n} i^{2} = \frac{n(n+1)(2n+1)}{2} = \frac{n^{3}}{3} + \frac{n^{2}}{2} + \frac{n}{6}$$

$$\sum_{i=0}^{n} i(i-1) = \frac{8}{6} (\frac{n}{2})(\frac{n}{2}+1)(n+1) \text{ (doubles)} \to \text{Sino ver caso impar y par}$$

$$\sum_{i=0}^{n} i^{3} = \left(\frac{n(n+1)}{2}\right)^{2} = \frac{n^{4}}{4} + \frac{n^{3}}{2} + \frac{n^{2}}{4} = \left[\sum_{i=1}^{n} i\right]^{2}$$

$$\sum_{i=0}^{n} i^{4} = \frac{n(n+1)(2n+1)(3n^{2}+3n-1)}{2n^{2}} = \frac{n^{5}}{5} + \frac{n^{4}}{2} + \frac{n^{3}}{3} - \frac{n}{30}$$

$$\sum_{i=0}^{n} i^{p} = \frac{(n+1)^{p+1}}{p+1} + \sum_{k=1}^{p} \frac{B_{k}}{p-k+1} {n \choose k} (n+1)^{p-k+1}$$

$$x = e - n + k + 1$$

Teorema de Pick: (Area, puntos interiores y puntos en el borde) $A = I + \tfrac{B}{2} - 1$

6.2. Ec. Característica

$$\begin{aligned} a_0T(n) + a_1T(n-1) + \ldots + a_kT(n-k) &= 0 \\ p(x) = a_0x^k + a_1x^{k-1} + \ldots + a_k \end{aligned}$$
 Sean r_1, r_2, \ldots, r_q las raíces distintas, de mult. m_1, m_2, \ldots, m_q
$$T(n) = \sum_{i=1}^q \sum_{j=0}^{m_i-1} c_{ij}n^jr_i^n$$
 Las constantes c_{ij} se determinan por los casos base.

6.3. Combinatorio

6.4. Exp. de Numeros Mod.

6.5. Exp. de Matrices y Fibonacci en log(n)

```
#define SIZE 350
int NN;
double tmp[SIZE][SIZE];
void mul(double a[SIZE] [SIZE], double b[SIZE] [SIZE]){ zero(tmp);
    forn(i, NN) forn(j, NN) forn(k, NN) res[i][j]+=a[i][k]*b[k][j];
    forn(i, NN) forn(j, NN) a[i][j]=res[i][j];
}
void powmat(double a[SIZE][SIZE], int n, double res[SIZE][SIZE]){
    forn(i, NN) forn(j, NN) res[i][j]=(i==j);
```

while(n){

10

```
if(n&1) mul(res, a), n--;
11
           else mul(a, a), n/=2;
12
       } }
13
                6.6. Matrices y determinante O(n^3)
  struct Mat {
1
       vector<vector<double> > vec;
2
       Mat(int n): vec(n, vector<double>(n) ) {}
3
       Mat(int n, int m): vec(n, vector<double>(m) ) {}
       vector<double> &operator[](int f){return vec[f];}
5
       const vector<double> &operator[](int f) const {return vec[f];}
6
       int size() const {return sz(vec);}
       Mat operator+(Mat &b) { ///this de n x m entonces b de n x m
8
           Mat m(sz(b), sz(b[0]));
           forn(i,sz(vec)) forn(j,sz(vec[0])) m[i][j] = vec[i][j] + b[i][j
10
               ];
           return m:
11
       Mat operator*(const Mat &b) { ///this de n x m entonces b de m x t
12
           int n = sz(vec), m = sz(vec[0]), t = sz(b[0]);
13
           Mat mat(n,t);
14
           forn(i,n) forn(j,t) forn(k,m) mat[i][j] += vec[i][k] * b[k][j];
15
           return mat:
16
       double determinant(){//sacado de e maxx ru
17
           double det = 1:
18
           int n = sz(vec);
19
           Mat m(*this);
20
           forn(i, n){//para cada columna
21
               int k = i;
22
               forr(j, i+1, n)//busco la fila con mayor val abs
23
                   if(abs(m[j][i])>abs(m[k][i])) k = j;
24
               if(abs(m[k][i])<1e-9) return 0;</pre>
25
               m[i].swap(m[k]);//la swapeo
26
               if(i!=k) det = -det;
27
               det *= m[i][i];
28
               forr(j, i+1, n) m[i][j] /= m[i][i];
29
               //hago 0 todas las otras filas
30
               forn(j, n) if (j!= i && abs(m[j][i])>1e-9)
31
                   forr(k, i+1, n) m[j][k]-=m[i][k]*m[j][i];
32
33
           return det;
34
       }
35
```

```
36 };
37
   int n;
38
   int main() {
   //DETERMINANTE:
   //https://uva.onlinejudge.org/index.php?option=com_onlinejudge&Itemid=8&
       page=show_problem&problem=625
     freopen("input.in", "r", stdin);
42
       ios::sync_with_stdio(0);
       while(cin >> n && n){
           Mat m(n);
45
           forn(i, n) forn(j, n) cin >> m[i][j];
           cout << (11)round(m.determinant()) << endl:</pre>
47
       }
       cout << "*" << endl:
49
     return 0;
51 }
```

6.7. Teorema Chino del Resto

$$y = \sum_{j=1}^{n} (x_j * (\prod_{i=1, i \neq j}^{n} m_i)_{m_j}^{-1} * \prod_{i=1, i \neq j}^{n} m_i)$$

6.8. Criba

6.9. Funciones de primos

Sea $n = \prod p_i^{k_i}$, fact(n) genera un map donde a cada p_i le asocia su k_i

```
1 //factoriza bien numeros hasta MAXP^2
  map<ll,ll> fact(ll n){ //0 (cant primos)
     map<ll,ll> ret;
     forall(p, primos){
       while(!(n %*p)){
         ret[*p]++;//divisor found
6
         n/=*p;
8
9
     if(n>1) ret[n]++;
10
     return ret;
11
12
  //factoriza bien numeros hasta MAXP
```

```
56 }
14 map<11,11> fact2(11 n){ //0 (lg n)
     map<ll,ll> ret;
                                                                                     57
15
     while (criba[n]){
                                                                                        int main() {
16
       ret[criba[n]]++;
                                                                                          buscarprimos();
17
                                                                                          forr (x,1, 500000){
       n/=criba[n];
18
                                                                                    60
                                                                                            cout << "x, =, " << x << endl;
19
                                                                                            cout << "Numero_de_factores_primos:_" << numPrimeFactors(x) << endl;</pre>
     if(n>1) ret[n]++;
                                                                                     62
                                                                                            cout << "Numero_de_distintos_factores_primos:_" <<
     return ret;
21
                                                                                     63
                                                                                                numDiffPrimeFactors(x) << endl;</pre>
^{22}
    //Usar asi: divisores(fac, divs, fac.begin()); NO ESTA ORDENADO
                                                                                            cout << "Suma de factores primos: " << sumPrimeFactors(x) << endl;
   void divisores(const map<11,11> &f, vector<11> &divs, map<11,11>::
                                                                                            cout << "Numero de divisores:" << numDiv(x) << endl;</pre>
                                                                                     65
       iterator it, ll n=1){
                                                                                            cout << "Suma, de, divisores:,," << sumDiv(x) << endl;</pre>
                                                                                            cout << "Phi,de,Euler:" << eulerPhi(x) << endl;</pre>
       if(it==f.begin()) divs.clear();
25
       if(it==f.end()) { divs.pb(n); return; }
                                                                                         }
                                                                                     68
26
       ll p=it->fst, k=it->snd; ++it;
                                                                                          return 0;
                                                                                     69
                                                                                     70 |}
       forn(_, k+1) divisores(f, divs, it, n), n*=p;
28
29
   11 sumDiv (11 n){
                                                                                                         6.10. Phollard's Rho (rolando)
     ll rta = 1:
31
     map<ll,ll> f=fact(n);
32
     forall(it, f) {
                                                                                     1 | ll gcd(ll a, ll b){return a?gcd(b %a, a):b;}
33
     11 \text{ pot} = 1, \text{ aux} = 0;
34
     forn(i, it->snd+1) aux += pot, pot *= it->fst;
                                                                                        11 mulmod (11 a, 11 b, 11 c) { //returns (a*b) %, and minimize overfloor
35
     rta*=aux;
                                                                                         11 x = 0, y = a\%;
36
     }
                                                                                         while (b > 0){
37
     return rta;
                                                                                           if (b \% 2 == 1) x = (x+y) \% c;
38
                                                                                            y = (y*2) \% c;
39
   ll eulerPhi (ll n){ // con criba: O(lg n)
                                                                                            b /= 2;
                                                                                     8
     11 \text{ rta} = n;
41
     map<ll,ll> f=fact(n);
42
                                                                                          return x % c;
                                                                                     10
     forall(it, f) rta -= rta / it->first;
                                                                                    11
     return rta:
                                                                                     12
45
                                                                                        ll expmod (ll b, ll e, ll m){\frac{1}{0}} \log b
   11 eulerPhi2 (11 n){ // 0 (sqrt n)
                                                                                          if(!e) return 1;
                                                                                    14
     11 r = n:
                                                                                          11 q= expmod(b,e/2,m); q=mulmod(q,q,m);
47
                                                                                    15
     forr (i,2,n+1){
                                                                                          return e %2? mulmod(b,q,m) : q;
48
                                                                                     16
       if ((11)i*i > n) break;
49
                                                                                     17
       if (n \% i == 0){
50
                                                                                     18
         while (n\% == 0) n/=i;
                                                                                        bool es_primo_prob (ll n, int a)
51
         r = r/i; }
52
                                                                                    20
                                                                                          if (n == a) return true;
53
                                                                                    21
     if (n != 1) r= r/n;
                                                                                          11 s = 0, d = n-1;
     return r;
                                                                                          while (d \% 2 == 0) s++, d/=2;
```

```
factRho(factor):
24
     11 x = expmod(a,d,n);
                                                                                      factRho(n/factor);
                                                                                 68
25
     if ((x == 1) \mid | (x+1 == n)) return true;
                                                                                 69 }
26
27
                                                                                                                6.11. GCD
     forn (i, s-1){
28
      x = mulmod(x, x, n);
29
                                                                                 tipo gcd(tipo a, tipo b){return a?gcd(b %a, a):b;}
       if (x == 1) return false;
30
       if (x+1 == n) return true;
31
                                                                                                         6.12. Extended Euclid
     }
32
     return false;
33
                                                                                 void extendedEuclid (ll a, ll b) \{ //a * x + b * y = d \}
34
                                                                                     if (!b) { x = 1; y = 0; d = a; return;}
35
                                                                                     extendedEuclid (b, a%);
   bool rabin (ll n){ //devuelve true si n es primo
                                                                                     11 x1 = v;
     if (n == 1) return false:
37
                                                                                     11 y1 = x - (a/b) * y;
     const int ar[] = \{2,3,5,7,11,13,17,19,23\};
38
                                                                                     x = x1; y = y1;
     forn (j,9)
39
                                                                                 7 }
       if (!es_primo_prob(n,ar[j]))
40
         return false;
41
                                                                                                                6.13. LCM
     return true:
42
43
                                                                                 1 | tipo lcm(tipo a, tipo b){return a / gcd(a,b) * b;}
44
   11 rho(11 n){
                                                                                                              6.14. Inversos
       if( (n & 1) == 0 ) return 2;
46
       11 x = 2 , y = 2 , d = 1;
47
                                                                                 1 #define MAXMOD 15485867
       11 c = rand() % n + 1;
48
                                                                                   11 inv[MAXMOD];//inv[i]*i=1 mod MOD
       while(d == 1){
49
                                                                                    void calc(int p){\frac{}{0}}
           x = (mulmod(x, x, n) + c) n;
50
                                                                                      inv[1]=1;
           y = (mulmod(y, y, n) + c) %n;
51
                                                                                      forr(i, 2, p) inv[i] = p-((p/i)*inv[p%i])%p;
           y = (mulmod(y, y, n) + c) n;
52
                                                                                 6
           if(x - y \ge 0) d = gcd(x - y, n);
53
                                                                                    int inverso(int x){\frac{1}{0}(\log x)}
                                                                                 7
           else d = gcd(y - x, n);
54
                                                                                      return expmod(x, eulerphi(MOD)-2);//si mod no es primo(sacar a mano)
55
                                                                                     return expmod(x, MOD-2);//si mod es primo
       return d==n? rho(n):d:
56
                                                                                 10 }
57
                                                                                                              6.15. Simpson
58
   map<ll,ll> prim;
   void factRho (ll n){ //O (lg n)^3. un solo numero
                                                                                    double integral(double a, double b, int n=10000) {//O(n), n=cantdiv
     if (n == 1) return:
                                                                                      double area=0, h=(b-a)/n, fa=f(a), fb;
61
     if (rabin(n)){
                                                                                     forn(i, n){
62
      prim[n]++;
                                                                                        fb=f(a+h*(i+1));
63
       return;
                                                                                        area+=fa+ 4*f(a+h*(i+0.5)) +fb, fa=fb;
64
                                                                                 5
65
                                                                                 6
    11 factor = rho(n);
                                                                                      return area*h/6.;}
```

6.16. Fraction

```
tipo mcd(tipo a, tipo b){return a?mcd(b%a, a):b;}
   struct frac{
     tipo p,q;
     frac(tipo p=0, tipo q=1):p(p),q(q) {norm();}
     void norm(){
       tipo a = mcd(p,q);
       if(a) p/=a, q/=a;
7
       else q=1;
 8
       if (q<0) q=-q, p=-p;}
     frac operator+(const frac& o){
       tipo a = mcd(q, o.q);
       return frac(p*(o.q/a)+o.p*(q/a), q*(o.q/a));}
     frac operator-(const frac& o){
13
       tipo a = mcd(q, o.q);
14
       return frac(p*(o.q/a)-o.p*(q/a), q*(o.q/a));}
15
     frac operator*(frac o){
16
       tipo a = mcd(q,o.p), b = mcd(o.q,p);
17
       return frac((p/b)*(o.p/a), (q/a)*(o.q/b));}
18
     frac operator/(frac o){
19
       tipo a = mcd(q,o.q), b = mcd(o.p,p);
20
       return frac((p/b)*(o.q/a),(q/a)*(o.p/b));}
21
     bool operator<(const frac &o) const{return p*o.q < o.p*q;}</pre>
22
     bool operator==(frac o){return p==o.p&kq==o.q;}
23
24 | };
```

6.17. Polinomio

```
int m = sz(c), n = sz(o.c);
1
          vector<tipo> res(max(m,n));
2
          forn(i, m) res[i] += c[i];
          forn(i, n) res[i] += o.c[i];
          return poly(res); }
      poly operator*(const tipo cons) const {
6
       vector<tipo> res(sz(c));
          forn(i, sz(c)) res[i]=c[i]*cons;
8
          return poly(res);
9
      poly operator*(const poly &o) const {
10
           int m = sz(c), n = sz(o.c);
11
          vector<tipo> res(m+n-1);
12
          forn(i, m) forn(j, n) res[i+j]+=c[i]*o.c[j];
13
          return poly(res);
14
```

```
tipo eval(tipo v) {
       tipo sum = 0;
16
       dforn(i, sz(c)) sum=sum*v + c[i];
17
       return sum; }
      //poly contains only a vector<int> c (the coeficients)
19
     //the following function generates the roots of the polynomial
   //it can be easily modified to return float roots
     set<tipo> roots(){
       set<tipo> roots;
23
       tipo a0 = abs(c[0]), an = abs(c[sz(c)-1]);
       vector<tipo> ps,qs;
25
       forr(p,1,sqrt(a0)+1) if (a0 \% == 0) ps.pb(p),ps.pb(a0/p);
26
       forr(q,1,sqrt(an)+1) if (an)(q=0) qs.pb(q),qs.pb(an/q);
       forall(pt,ps)
28
         forall(qt,qs) if ( (*pt) % (*qt)==0 ) {
29
           tipo root = abs((*pt) / (*qt));
           if (eval(root)==0) roots.insert(root);
31
32
       return roots; }
33
34
   pair<poly,tipo> ruffini(const poly p, tipo r) {
     int n = sz(p.c) - 1;
     vector<tipo> b(n);
37
    b[n-1] = p.c[n];
38
     dforn(k,n-1) b[k] = p.c[k+1] + r*b[k+1];
39
     tipo resto = p.c[0] + r*b[0];
40
     poly result(b);
41
     return make_pair(result,resto);
42
43
   poly interpolate(const vector<tipo>& x,const vector<tipo>& y) {
       poly A; A.c.pb(1);
45
       forn(i,sz(x)) { poly aux; aux.c.pb(-x[i]), aux.c.pb(1), A = A * aux;
46
    poly S; S.c.pb(0);
    forn(i,sz(x)) { poly Li;
       Li = ruffini(A,x[i]).fst;
      Li = Li * (1.0 / Li.eval(x[i])); // here put a multiple of the
50
           coefficients instead of 1.0 to avoid using double
       S = S + Li * y[i]; }
    return S;
   }
53
55 | int main(){
```

```
return 0;
57 }
                           6.18. Ec. Lineales
bool resolver_ev(Mat a, Vec y, Vec &x, Mat &ev){
     int n = a.size(), m = n?a[0].size():0, rw = min(n, m);
     vector<int> p; forn(i,m) p.push_back(i);
     forn(i, rw) {
       int uc=i. uf=i:
5
       forr(f, i, n) forr(c, i, m) if(fabs(a[f][c])>fabs(a[uf][uc])) {uf=f;
       if (feq(a[uf][uc], 0)) { rw = i; break; }
7
       forn(j, n) swap(a[j][i], a[j][uc]);
8
       swap(a[i], a[uf]); swap(y[i], y[uf]); swap(p[i], p[uc]);
9
       tipo inv = 1 / a[i][i]; //aca divide
10
       forr(j, i+1, n) {
11
         tipo v = a[j][i] * inv;
12
        forr(k, i, m) a[j][k]-=v * a[i][k];
13
        y[j] -= v*y[i];
14
15
     } // rw = rango(a), aca la matriz esta triangulada
16
     forr(i, rw, n) if (!feq(y[i],0)) return false; // checkeo de
17
         compatibilidad
     x = \text{vector} < \text{tipo} > (m, 0);
18
     dforn(i, rw){
19
       tipo s = v[i]:
20
       forr(j, i+1, rw) s -= a[i][j]*x[p[i]];
21
       x[p[i]] = s / a[i][i]; //aca divide
22
23
     ev = Mat(m-rw, Vec(m, 0)); // Esta parte va SOLO si se necesita el ev
24
     forn(k, m-rw) {
25
       ev[k][p[k+rw]] = 1:
26
       dforn(i, rw){
27
         tipo s = -a[i][k+rw];
28
         forr(j, i+1, rw) s -= a[i][j]*ev[k][p[j]];
29
         ev[k][p[i]] = s / a[i][i]; //aca divide
30
       }
31
     }
32
     return true;
33
34 | }
                                6.19. FFT
```

```
1 //~ typedef complex<double> base; //menos codigo, pero mas lento
//elegir si usar complejos de c (lento) o estos
3 struct base{
       double r,i;
       base(double r=0, double i=0):r(r), i(i){}
       double real()const{return r;}
       void operator/=(const int c){r/=c, i/=c;}
   };
8
   base operator*(const base &a, const base &b){
       return base(a.r*b.r-a.i*b.i, a.r*b.i+a.i*b.r);}
   base operator+(const base &a, const base &b){
       return base(a.r+b.r, a.i+b.i);}
   base operator-(const base &a, const base &b){
13
       return base(a.r-b.r, a.i-b.i);}
   vector<int> rev; vector<base> wlen_pw;
   inline static void fft(base a[], int n, bool invert) {
       forn(i, n) if(i<rev[i]) swap(a[i], a[rev[i]]);</pre>
     for (int len=2; len<=n; len<<=1) {
       double ang = 2*M_PI/len * (invert?-1:+1);
19
       int len2 = len >> 1;
       base wlen (cos(ang), sin(ang));
21
       wlen_pw[0] = base(1, 0);
           forr(i, 1, len2) wlen_pw[i] = wlen_pw[i-1] * wlen;
23
       for (int i=0; i<n; i+=len) {
         base t, *pu = a+i, *pv = a+i+len2, *pu_end = a+i+len2, *pw = &
25
             wlen_pw[0];
         for (; pu!=pu_end; ++pu, ++pv, ++pw)
           t = *pv * *pw, *pv = *pu - t,*pu = *pu + t;
27
       }
28
    }
     if (invert) forn(i, n) a[i]/= n;}
   inline static void calc_rev(int n){//precalculo: llamar antes de fft!!
       wlen_pw.resize(n), rev.resize(n);
32
       int lg=31-__builtin_clz(n);
33
      forn(i, n){
       rev[i] = 0:
           forn(k, lg) if(i\&(1<< k)) rev[i]|=1<<(lg-1-k);
       }}
   inline static void multiply(const vector<int> &a, const vector<int> &b,
       vector<int> &res) {
     vector<base> fa (a.begin(), a.end()), fb (b.begin(), b.end());
       int n=1; while(n < \max(sz(a), sz(b))) n <<= 1; n <<= 1;
       calc_rev(n);
41
```

```
fa.resize (n). fb.resize (n):
     fft (&fa[0], n, false), fft (&fb[0], n, false);
43
     forn(i, n) fa[i] = fa[i] * fb[i];
44
    fft (&fa[0], n, true);
45
     res.resize(n);
46
       forn(i, n) res[i] = int (fa[i].real() + 0.5); }
47
   void toPoly(const string &s, vector<int> &P){//convierte un numero a
       polinomio
       P.clear();
49
       dforn(i, sz(s)) P.pb(s[i]-'0');}
```

6.20. Tablas y cotas (Primos, Divisores, Factoriales, etc)

```
Factoriales
0! = 1
                  11! = 39.916.800
1! = 1
                  12! = 479.001.600 \ (\in int)
2! = 2
                  13! = 6.227.020.800
3! = 6
                  14! = 87.178.291.200
4! = 24
                  15! = 1.307.674.368.000
5! = 120
                  16! = 20.922.789.888.000
6! = 720
                  17! = 355.687.428.096.000
7! = 5.040
                  18! = 6.402.373.705.728.000
8! = 40.320
                  19! = 121.645.100.408.832.000
9! = 362.880
                  20! = 2.432.902.008.176.640.000 (\in tint)
10! = 3.628.800 \mid 21! = 51.090.942.171.709.400.000
       \max \text{ signed tint} = 9.223.372.036.854.775.807
     max unsigned tint = 18.446.744.073.709.551.615
```

Primos

 $\begin{array}{c} 2\ 3\ 5\ 7\ 11\ 13\ 17\ 19\ 23\ 29\ 31\ 37\ 41\ 43\ 47\ 53\ 59\ 61\ 67\ 71\ 73\ 79\ 83\ 89\ 97\ 101\ 103\ 107\ 109\\ 113\ 127\ 131\ 137\ 139\ 149\ 151\ 157\ 163\ 167\ 173\ 179\ 181\ 191\ 193\ 197\ 199\ 211\ 223\ 227\\ 229\ 233\ 239\ 241\ 251\ 257\ 263\ 269\ 271\ 277\ 281\ 283\ 293\ 307\ 311\ 313\ 317\ 331\ 337\ 347\\ 349\ 353\ 359\ 367\ 373\ 379\ 383\ 389\ 397\ 401\ 409\ 419\ 421\ 431\ 433\ 439\ 443\ 449\ 457\ 461\\ 463\ 467\ 479\ 487\ 491\ 499\ 503\ 509\ 521\ 523\ 541\ 547\ 557\ 563\ 569\ 571\ 577\ 587\ 593\ 599\\ 601\ 607\ 613\ 617\ 619\ 631\ 641\ 643\ 647\ 653\ 659\ 661\ 673\ 677\ 683\ 691\ 701\ 709\ 719\ 727\\ 733\ 739\ 743\ 751\ 757\ 761\ 769\ 773\ 787\ 797\ 809\ 811\ 821\ 823\ 827\ 829\ 839\ 853\ 857\ 859\\ 863\ 877\ 881\ 883\ 887\ 907\ 911\ 919\ 929\ 937\ 941\ 947\ 953\ 967\ 971\ 977\ 983\ 991\ 997\ 1009\\ 1013\ 1019\ 1021\ 1031\ 1033\ 1039\ 1049\ 1051\ 1061\ 1063\ 1069\ 1087\ 1091\ 1093\ 1097\ 1103\\ 1109\ 1117\ 1123\ 1129\ 1151\ 1153\ 1163\ 1171\ 1181\ 1187\ 1193\ 1201\ 1213\ 1217\ 1223\ 1229\\ 1231\ 1237\ 1249\ 1259\ 1277\ 1279\ 1283\ 1289\ 1291\ 1297\ 1301\ 1303\ 1307\ 1319\ 1321\ 1327\\ 1361\ 1367\ 1373\ 1381\ 1399\ 1409\ 1423\ 1427\ 1429\ 1433\ 1439\ 1447\ 1451\ 1453\ 1459\ 1471\\ 1481\ 1483\ 1487\ 1489\ 1493\ 1499\ 1511\ 1523\ 1531\ 1543\ 1549\ 1553\ 1559\ 1567\ 1571\ 1579\\ 1583\ 1597\ 1601\ 1607\ 1609\ 1613\ 1619\ 1621\ 1627\ 1637\ 1657\ 1663\ 1667\ 1669\ 1693\ 1697\\ 1699\ 1709\ 1721\ 1723\ 1733\ 1741\ 1747\ 1753\ 1759\ 1777\ 1783\ 1787\ 1789\ 1801\ 1811\ 1823\\ \end{array}$

1831 1847 1861 1867 1871 1873 1877 1879 1889 1901 1907 1913 1931 1933 1949 1951 1973 1979 1987 1993 1997 1999 2003 2011 2017 2027 2029 2039 2053 2063 2069 2081

Primos cercanos a 10^n

9941 9949 9967 9973 10007 10009 10037 10039 10061 10067 10069 10079 99961 99971 99989 99991 100003 100019 100043 100049 100057 100069 999959 999961 999979 999983 1000003 1000033 1000037 1000039 9999943 9999971 99999991 10000019 10000079 10000103 10000121 99999941 9999959 9999971 99999989 100000007 100000037 100000039 100000049 99999893 99999929 99999937 1000000007 1000000009 1000000021 1000000033

Cantidad de primos menores que 10^n

```
\pi(10^1) = 4; \pi(10^2) = 25; \pi(10^3) = 168; \pi(10^4) = 1229; \pi(10^5) = 9592

\pi(10^6) = 78.498; \pi(10^7) = 664.579; \pi(10^8) = 5.761.455; \pi(10^9) = 50.847.534

\pi(10^{10}) = 455.052,511; \pi(10^{11}) = 4.118.054.813; \pi(10^{12}) = 37.607.912.018
```

Divisores

```
Cantidad de divisores (\sigma_0) para algunos n/\neg \exists n' < n, \sigma_0(n') \geqslant \sigma_0(n)
       \sigma_0(60) = 12; \sigma_0(120) = 16; \sigma_0(180) = 18; \sigma_0(240) = 20; \sigma_0(360) = 24
    \sigma_0(720) = 30; \sigma_0(840) = 32; \sigma_0(1260) = 36; \sigma_0(1680) = 40; \sigma_0(10080) = 72
        \sigma_0(15120) = 80; \sigma_0(50400) = 108; \sigma_0(83160) = 128; \sigma_0(110880) = 144
   \sigma_0(498960) = 200; \sigma_0(554400) = 216; \sigma_0(1081080) = 256; \sigma_0(1441440) = 288
                            \sigma_0(4324320) = 384 : \sigma_0(8648640) = 448
            Suma de divisores (\sigma_1) para algunos n/\neg \exists n' < n, \sigma_1(n') \geqslant \sigma_1(n)
    \sigma_1(96) = 252; \sigma_1(108) = 280; \sigma_1(120) = 360; \sigma_1(144) = 403; \sigma_1(168) = 480
        \sigma_1(960) = 3048; \sigma_1(1008) = 3224; \sigma_1(1080) = 3600; \sigma_1(1200) = 3844
     \sigma_1(4620) = 16128; \sigma_1(4680) = 16380; \sigma_1(5040) = 19344; \sigma_1(5760) = 19890
    \sigma_1(8820) = 31122; \sigma_1(9240) = 34560; \sigma_1(10080) = 39312; \sigma_1(10920) = 40320
\sigma_1(32760) = 131040; \sigma_1(35280) = 137826; \sigma_1(36960) = 145152; \sigma_1(37800) = 148800
\sigma_1(60480) = 243840; \sigma_1(64680) = 246240; \sigma_1(65520) = 270816; \sigma_1(70560) = 280098
            \sigma_1(95760) = 386880; \sigma_1(98280) = 403200; \sigma_1(100800) = 409448
        \sigma_1(491400) = 2083200; \sigma_1(498960) = 2160576; \sigma_1(514080) = 2177280
        \sigma_1(982800) = 4305280; \sigma_1(997920) = 4390848; \sigma_1(1048320) = 4464096
     \sigma_1(4979520) = 22189440; \sigma_1(4989600) = 22686048; \sigma_1(5045040) = 23154768
    \sigma_1(9896040) = 44323200; \sigma_1(9959040) = 44553600; \sigma_1(9979200) = 45732192
```

7. Grafos

7.1. Dijkstra

```
#define INF 1e9 int N;
```

```
3 | #define MAX_V 250001
                                                                                  3 int G[MAX_N][MAX_N];
   vector<ii> G[MAX_V];
                                                                                    void floyd(){\frac{}{0(N^3)}}
   //To add an edge use
                                                                                    forn(k, N) forn(i, N) if(G[i][k]!=INF) forn(j, N) if(G[k][j]!=INF)
   #define add(a, b, w) G[a].pb(make_pair(w, b))
                                                                                      G[i][j]=min(G[i][j], G[i][k]+G[k][j]);
   ll dijkstra(int s, int t){\frac{1}{0}(|E| \log |V|)}
                                                                                    }
                                                                                  7
     priority_queue<ii, vector<ii>, greater<ii> > Q;
                                                                                     bool inNegCycle(int v){
                                                                                      return G[v][v]<0;}
     vector<ll> dist(N, INF); vector<int> dad(N, -1);
     Q.push(make_pair(0, s)); dist[s] = 0;
                                                                                     //checks if there's a neg. cycle in path from a to b
10
     while(sz(Q)){
                                                                                     bool hasNegCycle(int a, int b){
11
                                                                                      forn(i, N) if(G[a][i]!=INF && G[i][i]<0 && G[i][b]!=INF)
       ii p = Q.top(); Q.pop();
12
       if(p.snd == t) break;
                                                                                         return true;
13
                                                                                 13
       forall(it, G[p.snd])
                                                                                      return false;
14
                                                                                 14
         if(dist[p.snd]+it->first < dist[it->snd]){
                                                                                 15 }
15
           dist[it->snd] = dist[p.snd] + it->fst;
16
                                                                                                                7.4. Kruskal
           dad[it->snd] = p.snd;
17
           Q.push(make_pair(dist[it->snd], it->snd)); }
18
                                                                                  struct Ar{int a,b,w;};
     }
19
                                                                                  bool operator<(const Ar& a, const Ar &b){return a.w<b.w;}</pre>
     return dist[t];
20
                                                                                    vector<Ar> E:
     if(dist[t]<INF)//path generator</pre>
21
                                                                                    ll kruskal(){
       for(int i=t; i!=-1; i=dad[i])
22
                                                                                         11 cost=0;
         printf("%1%", i, (i==s?'\n':'\_'));}
23
                                                                                         sort(E.begin(), E.end());//ordenar aristas de menor a mayor
                                                                                  6
                           7.2. Bellman-Ford
                                                                                         uf.init(n);
                                                                                         forall(it, E){
                                                                                  8
                                                                                             if(uf.comp(it->a)!=uf.comp(it->b)){//si no estan conectados
  vector<ii> G[MAX_N];//ady. list with pairs (weight, dst)
                                                                                  9
                                                                                                 uf.unir(it->a, it->b);//conectar
  int dist[MAX_N];
                                                                                 10
   void bford(int src){//O(VE)
                                                                                                 cost+=it->w;
                                                                                 11
     dist[src]=0;
                                                                                             }
                                                                                 12
4
                                                                                         }
     forn(i, N-1) forn(j, N) if(dist[j]!=INF) forall(it, G[j])
                                                                                 13
       dist[it->snd]=min(dist[it->snd], dist[j]+it->fst);
                                                                                         return cost;
6
                                                                                 14
                                                                                 15 }
7
8
                                                                                                                  7.5. Prim
   bool hasNegCycle(){
     forn(j, N) if(dist[j]!=INF) forall(it, G[j])
                                                                                    bool taken[MAXN];
       if(dist[it->snd]>dist[j]+it->fst) return true;
                                                                                    priority_queue<ii, vector<ii>, greater<ii> > pq;//min heap
     //inside if: all points reachable from it->snd will have -INF distance
                                                                                    void process(int v){
         (do bfs)
                                                                                         taken[v]=true;
                                                                                  4
     return false;
                                                                                         forall(e, G[v])
                                                                                  5
14 }
                                                                                             if(!taken[e->second]) pq.push(*e);
                                                                                  6
                          7.3. Floyd-Warshall
                                                                                    }
                                                                                  7
1 |//G[i][j] contains weight of edge (i, j) or INF
                                                                                    ll prim(){
2 //G[i][i]=0
                                                                                         zero(taken);
```

```
process(0);
ll cost=0;
while(sz(pq)){
    ii e=pq.top(); pq.pop();
    if(!taken[e.second]) cost+=e.first, process(e.second);
}
return cost;
}
```

7.6. 2-SAT + Tarjan SCC

```
//We have a vertex representing a var and other for his negation.
   //Every edge stored in G represents an implication. To add an equation
       of the form allb, use addor(a, b)
   //MAX=max cant var, n=cant var
   #define addor(a, b) (G[neg(a)].pb(b), G[neg(b)].pb(a))
   vector<int> G[MAX*2];
   //idx[i]=index assigned in the dfs
   //lw[i]=lowest index(closer from the root) reachable from i
   int lw[MAX*2], idx[MAX*2], qidx;
   stack<int> q;
   int qcmp, cmp[MAX*2];
   //verdad[cmp[i]]=valor de la variable i
   bool verdad[MAX*2+1];
13
   int neg(int x) { return x>=n? x-n : x+n;}
   void tin(int v){
15
     lw[v]=idx[v]=++qidx;
16
     q.push(v), cmp[v]=-2;
17
     forall(it, G[v]){
18
       if(!idx[*it] || cmp[*it]==-2){
19
         if(!idx[*it]) tjn(*it);
20
         lw[v]=min(lw[v], lw[*it]);
21
       }
^{22}
     }
23
     if(lw[v]==idx[v]){
24
       int x;
^{25}
       do{x=q.top(); q.pop(); cmp[x]=qcmp;}while(x!=v);
26
       verdad[qcmp] = (cmp[neg(v)] < 0);</pre>
27
       qcmp++;
28
     }
29
30
   //remember to CLEAR G!!!
```

```
bool satisf(){//0(n)
  memset(idx, 0, sizeof(idx)), qidx=0;
  memset(cmp, -1, sizeof(cmp)), qcmp=0;
  forn(i, n){
    if(!idx[i]) tjn(i);
    if(!idx[neg(i)]) tjn(neg(i));
  }
  forn(i, n) if(cmp[i]==cmp[neg(i)]) return false;
  return true;
}
```

7.7. Articulation Points

```
1 int N;
   vector<int> G[1000000];
   //V[i]=node number(if visited), L[i]= lowest V[i] reachable from i
   int qV, V[1000000], L[1000000], P[1000000];
   void dfs(int v, int f){
     L[v]=V[v]=++qV;
     forall(it, G[v])
       if(!V[*it]){
         dfs(*it, v);
9
         L[v] = min(L[v], L[*it]);
         P[v] += L[*it] >= V[v];
11
12
       else if(*it!=f)
13
         L[v]=min(L[v], V[*it]);
14
   }
15
   int cantart(){ //O(n)
     qV=0;
17
     zero(V), zero(P);
     dfs(1, 0); P[1]--;
     int q=0;
     forn(i, N) if(P[i]) q++;
   return q;
22
23 }
```

7.8. Comp. Biconexas y Puentes

```
struct edge {
int u,v, comp;
bool bridge;
};
vector<edge> e;
```

```
6 | void addEdge(int u, int v) {
     G[u].pb(sz(e)), G[v].pb(sz(e));
     e.pb((edge)\{u,v,-1,false\});
9
                                                                                     const int MAXN=100001;
   //d[i]=id de la dfs
                                                                                       const int LOGN=20;
   //b[i]=lowest id reachable from i
                                                                                       //f[v][k] holds the 2<sup>k</sup> father of v
   int d[MAXN], b[MAXN], t;
                                                                                       //L[v] holds the level of v
   int nbc;//cant componentes
                                                                                       int N, f[MAXN][LOGN], L[MAXN];
   int comp[MAXN];//comp[i]=cant comp biconexas a la cual pertenece i
                                                                                       //call before build:
   void initDfs(int n) {
15
     zero(G), zero(comp);
                                                                                         f[v][0]=fa, L[v]=lvl;
     e.clear();
     forn(i,n) d[i]=-1;
     nbc = t = 0:
19
20
   stack<int> st;
                                                                                       int climb(int a, int d){\frac{1}{0(lgn)}}
   void dfs(int u, int pe) \{//0(n + m)\}
                                                                                         if(!d) return a;
                                                                                    14
     b[u] = d[u] = t++;
23
                                                                                    15
     comp[u] = (pe != -1);
24
                                                                                           return a:}
                                                                                    16
     forall(ne, G[u]) if (*ne != pe){
25
                                                                                       int lca(int a, int b){\frac{1}{0}}
       int v = e[*ne].u ^ e[*ne].v ^ u;
26
                                                                                         if(L[a]<L[b]) swap(a, b);
                                                                                    18
       if (d[v] == -1) {
27
                                                                                         a=climb(a, L[a]-L[b]);
                                                                                    19
         st.push(*ne);
28
                                                                                         if(a==b) return a;
                                                                                    20
         dfs(v,*ne);
29
                                                                                    21
         if (b[v] > d[u]){
30
                                                                                         return f[a][0]; }
                                                                                    22
           e[*ne].bridge = true; // bridge
31
         }
32
                                                                                         return L[a]+L[b]-2*L[lca(a, b)];}
         if (b[v] >= d[u]) \{ // art \}
33
           int last;
34
           do {
35
             last = st.top(); st.pop();
36
              e[last].comp = nbc;
37
                                                                                       int dad[MAXN];//dad[v]=padre del nodo v
           } while (last != *ne);
                                                                                       void dfs1(int v, int p=-1){//pre-dfs
38
           nbc++:
                                                                                         dad[v]=p;
39
           comp[u]++;
                                                                                         treesz[v]=1;
40
                                                                                         forall(it, G[v]) if(*it!=p){
41
                                                                                     6
         b[u] = min(b[u], b[v]);
42
                                                                                           dfs1(*it, v);
       }
                                                                                            treesz[v]+=treesz[*it]:
43
                                                                                     8
       else if (d[v] < d[u]) \{ // back edge
                                                                                         }
44
                                                                                    9
         st.push(*ne);
45
                                                                                    10
         b[u] = min(b[u], d[v]);
                                                                                       //PONER Q EN O !!!!!
46
47
     }
48
                                                                                    13 //Las cadenas aparecen continuas en el recorrido!
```

```
49 }
                         7.9. LCA + Climb
  void dfs(int v, int fa=-1, int lvl=0){//generate required data
    forall(it, G[v])if(*it!=fa) dfs(*it, v, lvl+1); }
   void build(){//f[i][0] must be filled previously, O(nlgn)
    forn(k, LOGN-1) forn(i, N) f[i][k+1]=f[f[i][k]][k];}
  #define lg(x) (31-_builtin_clz(x))//=floor(log2(x))
    dforn(i, lg(L[a])+1) if(1<<i<=d) a=f[a][i], d-=1<<i;
    dforn(i, lg(L[a])+1) if(f[a][i]!=f[b][i]) a=f[a][i], b=f[b][i];
   int dist(int a, int b) {//returns distance between nodes
                7.10. Heavy Light Decomposition
  int treesz[MAXN];//cantidad de nodos en el subarbol del nodo v
  int pos[MAXN], q;//pos[v]=posicion del nodo v en el recorrido de la dfs
```

```
14 | int cantcad;
   int homecad [MAXN];//dada una cadena devuelve su nodo inicial
   int cad[MAXN];//cad[v]=cadena a la que pertenece el nodo
   void heavylight(int v, int cur=-1){
     if(cur==-1) homecad[cur=cantcad++]=v;
18
     pos[v]=q++;
19
     cad[v]=cur;
20
     int mx=-1;
21
     forn(i, sz(G[v])) if(G[v][i]!=dad[v])
22
       if(mx==-1 || treesz[G[v][mx]]<treesz[G[v][i]]) mx=i;</pre>
23
     if(mx!=-1) heavylight(G[v][mx], cur);
24
     forn(i, sz(G[v])) if(i!=mx && G[v][i]!=dad[v])
25
       heavylight(G[v][i], -1);
27
   //ejemplo de obtener el maximo numero en el camino entre dos nodos
   //RTA: max(query(low, u), query(low, v)), con low=lca(u, v)
   //esta funcion va trepando por las cadenas
   int query(int an, int v){//O(logn)
     //si estan en la misma cadena:
32
     if(cad[an] == cad[v]) return rmq.get(pos[an], pos[v]+1);
33
     return max(query(an, dad[homecad[cad[v]]]),
34
            rmq.get(pos[homecad[cad[v]]], pos[v]+1));
35
36 }
```

7.11. Centroid Decomposition

```
1 | int n;
   vector<int> G[MAXN];
   bool taken[MAXN];//poner todos en FALSE al principio!!
   int padre[MAXN];//padre de cada nodo en el centroid tree
5
   int szt[MAXN];
   void calcsz(int v, int p) {
     szt[v] = 1;
8
    forall(it,G[v]) if (*it!=p && !taken[*it])
9
       calcsz(*it,v), szt[v]+=szt[*it];
10
11
   void centroid(int v=0, int f=-1, int lvl=0, int tam=-1) {//0(nlogn)
12
     if(tam==-1) calcsz(v, -1), tam=szt[v];
13
     forall(it, G[v]) if(!taken[*it] && szt[*it]>=tam/2)
14
       {szt[v]=0; centroid(*it, f, lvl, tam); return;}
15
     taken[v]=true;
16
     padre[v]=f;
17
```

```
forall(it, G[v]) if(!taken[*it])
       centroid(*it, v, lvl+1, -1);
19
20 }
                           7.12. Euler Cycle
int n,m,ars[MAXE], eq;
  vector<int> G[MAXN];//fill G,n,m,ars,eq
   list<int> path;
   int used[MAXN];
   bool usede[MAXE];
   queue<list<int>::iterator> q;
   int get(int v){
     while(used[v]<sz(G[v]) && usede[ G[v][used[v]] ]) used[v]++;</pre>
     return used[v];
9
10
   void explore(int v, int r, list<int>::iterator it){
11
     int ar=G[v][get(v)]; int u=v^ars[ar];
12
     usede[ar]=true:
13
     list<int>::iterator it2=path.insert(it, u);
14
     if(u!=r) explore(u, r, it2);
15
     if(get(v)<sz(G[v])) q.push(it);</pre>
16
17
   void euler(){
18
     zero(used), zero(usede);
19
     path.clear();
20
     q=queue<list<int>::iterator>();
21
     path.push_back(0); q.push(path.begin());
22
     while(sz(q)){
23
       list<int>::iterator it=q.front(); q.pop();
24
       if(used[*it]<sz(G[*it])) explore(*it, *it, it);</pre>
25
     }
26
     reverse(path.begin(), path.end());
27
28
   void addEdge(int u, int v){
29
     G[u].pb(eq), G[v].pb(eq);
30
     ars[eq++]=u^v;
31
32 }
                         7.13. Diametro árbol
vector<int> G[MAXN]; int n,m,p[MAXN],d[MAXN],d2[MAXN];
int bfs(int r, int *d) {
     queue<int> q;
```

11

```
d[r]=0; q.push(r);
                                                                                             while (comp[v].size() > 0) {
4
                                                                                  12
                                                                                               no[comp[v].back()] = s;
     int v;
5
                                                                                  13
     while(sz(q)) { v=q.front(); q.pop();
                                                                                                comp[s].push_back(comp[v].back());
                                                                                  14
6
       forall(it,G[v]) if (d[*it]==-1)
                                                                                                comp[v].pop_back();
                                                                                  15
         d[*it]=d[v]+1, p[*it]=v, q.push(*it);
                                                                                  16
9
                                                                                  17
     return v;//ultimo nodo visitado
                                                                                         } while (v != s);
                                                                                  18
10
                                                                                         forall(j,comp[s]) if (*j != r) forall(e,h[*j])
11
                                                                                  19
   vector<int> diams; vector<ii> centros;
                                                                                           if (no[e->src] != s) e->w -= mcost[ temp[*i] ];
                                                                                  20
   void diametros(){
                                                                                  21
     memset(d,-1,sizeof(d));
                                                                                       mark[v] = true:
                                                                                  22
14
                                                                                       forall(i,next[v]) if (no[*i] != no[v] && prev[no[*i]] == v)
     memset(d2,-1,sizeof(d2));
                                                                                  23
                                                                                         if (!mark[no[*i]] || *i == s)
     diams.clear(), centros.clear();
                                                                                  24
     forn(i, n) if(d[i]==-1){
                                                                                           visit(h, *i, s, r, no, comp, prev, next, mcost, mark, cost, found)
                                                                                  25
17
       int v,c;
18
       c=v=bfs(bfs(i, d2), d);
                                                                                  26
19
       forn(_,d[v]/2) c=p[c];
                                                                                     weight minimumSpanningArborescence(const graph &g, int r) {
20
       diams.pb(d[v]);
                                                                                         const int n=sz(g);
21
       if(d[v]&1) centros.pb(ii(c, p[c]));
                                                                                       graph h(n):
22
       else centros.pb(ii(c, c));
                                                                                       forn(u,n) forall(e,g[u]) h[e->dst].pb(*e);
23
                                                                                       vector<int> no(n);
                                                                                  31
24
                                                                                       vector<vector<int> > comp(n);
25
                                                                                       forn(u, n) comp[u].pb(no[u] = u);
                                                                                  33
26
   int main() {
                                                                                       for (weight cost = 0; ;) {
27
     freopen("in", "r", stdin);
                                                                                         vector<int> prev(n, -1);
                                                                                  35
28
     while(cin >> n >> m){}
                                                                                         vector<weight> mcost(n, INF);
                                                                                  36
29
                                                                                         forn(j,n) if (j != r) forall(e,h[j])
       forn(i,m) { int a,b; cin >> a >> b; a--, b--;
                                                                                  37
30
         G[a].pb(b);
                                                                                           if (no[e->src] != no[i])
31
         G[b].pb(a);
                                                                                             if (e->w < mcost[ no[j] ])</pre>
32
                                                                                  39
                                                                                                mcost[ no[i] ] = e->w, prev[ no[i] ] = no[e->src];
                                                                                  40
                              7.14. Chu-liu
                                                                                         vector< vector<int> > next(n);
                                                                                  41
                                                                                         forn(u,n) if (prev[u] >= 0)
                                                                                           next[ prev[u] ].push_back(u);
   void visit(graph &h, int v, int s, int r,
                                                                                  43
                                                                                         bool stop = true;
     vector<int> &no, vector< vector<int> > &comp,
                                                                                  44
2
                                                                                         vector<int> mark(n);
     vector<int> &prev, vector< vector<int> > &next, vector<weight> &mcost,
                                                                                  45
3
                                                                                         forn(u,n) if (u != r && !mark[u] && !comp[u].empty()) {
                                                                                  46
     vector<int> &mark, weight &cost, bool &found) {
4
                                                                                           bool found = false:
                                                                                  47
     if (mark[v]) {
5
                                                                                           visit(h, u, u, r, no, comp, prev, next, mcost, mark, cost, found);
       vector<int> temp = no;
6
                                                                                           if (found) stop = false;
       found = true:
                                                                                  49
                                                                                         }
       do {
                                                                                         if (stop) {
         cost += mcost[v];
9
                                                                                           forn(u,n) if (prev[u] >= 0) cost += mcost[u];
         v = prev[v];
                                                                                  52
         if (v != s) {
                                                                                           return cost;
```

53

```
}
     }
55
56 }
                            7.15. Hungarian
1 //Dado un grafo bipartito completo con costos no negativos, encuentra el
        matching perfecto de minimo costo.
2 tipo cost[N][N], lx[N], ly[N], slack[N]; //llenar: cost=matriz de
       advacencia
  int n, max_match, xy[N], yx[N], slackx[N], prev2[N]; //n=cantidad de nodos
   bool S[N], T[N]; //sets S and T in algorithm
   void add_to_tree(int x, int prevx) {
     S[x] = true, prev2[x] = prevx;
     forn(y, n) if (lx[x] + ly[y] - cost[x][y] < slack[y] - EPS)
       slack[y] = lx[x] + ly[y] - cost[x][y], slackx[y] = x;
8
9
   void update_labels(){
10
     tipo delta = INF;
     forn (y, n) if (!T[y]) delta = min(delta, slack[y]);
     form (x, n) if (S[x]) lx[x] -= delta;
     forn (y, n) if (T[y]) ly[y] += delta; else slack[y] -= delta;
14
15
   void init labels(){
16
     zero(lx), zero(ly);
17
     forn (x,n) forn(y,n) lx[x] = max(lx[x], cost[x][y]);
18
19
   void augment() {
20
     if (max_match == n) return;
21
     int x, y, root, q[N], wr = 0, rd = 0;
22
     memset(S, false, sizeof(S)), memset(T, false, sizeof(T));
23
     memset(prev2, -1, sizeof(prev2));
24
     forn (x, n) if (xy[x] == -1){
25
       q[wr++] = root = x, prev2[x] = -2;
26
       S[x] = true; break; }
27
     form (y, n) slack[y] = lx[root] + ly[y] - cost[root][y], slack[y] = lx[root]
28
         root;
     while (true){
29
       while (rd < wr){
30
         x = a[rd++]:
31
         for (y = 0; y < n; y++) if (cost[x][y] == lx[x] + ly[y] && !T[y]){
32
           if (yx[y] == -1) break; T[y] = true;
33
```

 $q[wr++] = yx[y], add_to_tree(yx[y], x);$

34

```
if (y < n) break; }</pre>
35
       if (v < n) break;
36
       update_labels(), wr = rd = 0;
       for (y = 0; y < n; y++) if (!T[y] && slack[y] == 0){
         if (yx[y] == -1)\{x = slackx[y]; break;\}
39
         else{
40
           T[v] = true;
41
           if (!S[yx[y]]) q[wr++] = yx[y], add_to_tree(yx[y], slackx[y]);
42
         }}
43
       if (v < n) break; }
     if (y < n){
45
       max_match++;
       for (int cx = x, cy = y, ty; cx != -2; cx = prev2[cx], cy = ty)
47
         ty = xy[cx], yx[cy] = cx, xy[cx] = cy;
       augment(); }
49
50
   tipo hungarian(){
51
     tipo ret = 0; max_match = 0, memset(xy, -1, sizeof(xy));
     memset(yx, -1, sizeof(yx)), init_labels(), augment(); //steps 1-3
     forn (x,n) ret += cost[x][xy[x]]; return ret;
55 }
```

7.16. Dynamic Conectivity

```
struct UnionFind {
       int n, comp;
       vector<int> pre,si,c;
3
       UnionFind(int n=0):n(n), comp(n), pre(n), si(n, 1) {
4
           forn(i,n) pre[i] = i; }
5
       int find(int u){return u==pre[u]?u:find(pre[u]);}
6
       bool merge(int u, int v) {
7
           if((u=find(u))==(v=find(v))) return false;
8
           if(si[u]<si[v]) swap(u, v);</pre>
9
           si[u]+=si[v], pre[v]=u, comp--, c.pb(v);
10
           return true;
11
12
       int snap(){return sz(c);}
13
       void rollback(int snap){
14
           while(sz(c)>snap){
15
               int v = c.back(); c.pop_back();
16
               si[pre[v]] = si[v], pre[v] = v, comp++;
17
           }
18
       }
19
```

```
20 };
   enum {ADD,DEL,QUERY};
   struct Query {int type,u,v;};
   struct DynCon {
       vector<Query> q;
24
       UnionFind dsu;
25
       vector<int> match,res;
26
       map<ii,int> last;//se puede no usar cuando hay identificador para
27
           cada arista (mejora poco)
       DynCon(int n=0):dsu(n){}
28
       void add(int u, int v) {
29
           if(u>v) swap(u,v);
30
           q.pb((Query){ADD, u, v}), match.pb(-1);
31
           last[ii(u,v)] = sz(q)-1;
32
       }
33
       void remove(int u, int v) {
34
           if(u>v) swap(u,v);
35
           q.pb((Query){DEL, u, v});
36
           int prev = last[ii(u,v)];
37
           match[prev] = sz(q)-1;
38
           match.pb(prev);
39
       }
40
       void query() {//podria pasarle un puntero donde guardar la respuesta
41
           q.pb((Query){QUERY, -1, -1}), match.pb(-1);}
42
       void process() {
43
           forn(i,sz(q)) if (q[i].type == ADD && match[i] == -1) match[i] =
44
                sz(q);
           go(0,sz(q));
45
       }
46
       void go(int 1, int r) {
47
           if(l+1==r){
48
               if (q[1].type == QUERY)//Aqui responder la query usando el
49
                    res.pb(dsu.comp);//aqui query=cantidad de componentes
50
                        conexas
               return;
51
52
           int s=dsu.snap(), m = (l+r) / 2;
53
           forr(i,m,r) if(match[i]!=-1 && match[i]<1) dsu.merge(q[i].u, q[i</pre>
54
               ].v);
           go(1,m);
55
           dsu.rollback(s);
56
           s = dsu.snap();
57
```

8. Flujo

8.1. Dinic

```
2 const int MAX = 300;
3 // Corte minimo: vertices con dist[v]>=0 (del lado de src) VS. dist[v
       ]==-1 (del lado del dst)
4 // Para el caso de la red de Bipartite Matching (Sean V1 y V2 los
       conjuntos mas proximos a src y dst respectivamente):
5 // Reconstruir matching: para todo v1 en V1 ver las aristas a vertices
       de V2 con it->f>0, es arista del Matching
6 // Min Vertex Cover: vertices de V1 con dist[v] ==-1 + vertices de V2 con
        dist[v]>0
7 // Max Independent Set: tomar los vertices NO tomados por el Min Vertex
       Cover
8 // Max Clique: construir la red de G complemento (debe ser bipartito!) y
        encontrar un Max Independet Set
9 // Min Edge Cover: tomar las aristas del matching + para todo vertices
       no cubierto hasta el momento, tomar cualquier arista de el
  int nodes, src, dst;
   int dist[MAX], q[MAX], work[MAX];
   struct Edge {
       int to, rev;
13
       ll f, cap;
14
       Edge(int to, int rev, ll f, ll cap) : to(to), rev(rev), f(f), cap(
15
           cap) {}
   };
16
   vector<Edge> G[MAX];
   void addEdge(int s, int t, ll cap){
       G[s].pb(Edge(t, sz(G[t]), 0, cap)), G[t].pb(Edge(s, sz(G[s])-1, 0,
19
           0));}
20 bool dinic bfs(){
       fill(dist, dist+nodes, -1), dist[src]=0;
21
       int qt=0; q[qt++]=src;
22
       for(int qh=0; qh<qt; qh++){</pre>
23
```

```
int u =q[qh];
24
           forall(e, G[u]){
^{25}
                int v=e->to;
26
                if(dist[v]<0 && e->f < e->cap)
27
                    dist[v]=dist[u]+1, q[qt++]=v;
28
           }
29
       }
30
       return dist[dst]>=0;
31
32
   11 dinic_dfs(int u, ll f){
33
       if(u==dst) return f;
34
       for(int &i=work[u]; i<sz(G[u]); i++){</pre>
35
           Edge &e = G[u][i];
36
           if(e.cap<=e.f) continue;</pre>
37
            int v=e.to;
38
           if(dist[v]==dist[u]+1){
39
                    11 df=dinic_dfs(v, min(f, e.cap-e.f));
40
                    if(df>0){
41
                             e.f+=df, G[v][e.rev].f-= df;
42
                             return df; }
43
           }
44
       }
45
       return 0;
46
47
   ll maxFlow(int _src, int _dst){
48
       src=_src, dst=_dst;
49
       11 result=0;
50
       while(dinic_bfs()){
51
           fill(work, work+nodes, 0);
52
            while(ll delta=dinic_dfs(src,INF))
53
                result+=delta;
54
       }
55
       // todos los nodos con dist[v]!=-1 vs los que tienen dist[v]==-1
56
            forman el min-cut
       return result; }
57
```

8.2. Konig

```
1 // asume que el dinic YA ESTA tirado
 // asume que nodes-1 y nodes-2 son la fuente y destino
 int match[maxnodes]; // match[v]=u si u-v esta en el matching, -1 si v
      no esta matcheado
4 int s[maxnodes]; // numero de la bfs del koning
```

```
5 | queue<int> kq;
6 // s[e] %2==1 o si e esta en V1 y s[e] ==-1-> lo agarras
   void koning() \{//0(n)
     forn(v,nodes-2) s[v] = match[v] = -1;
     forn(v,nodes-2) forall(it,g[v]) if (it->to < nodes-2 && it->f>0)
       { match[v]=it->to; match[it->to]=v;}
     forn(v,nodes-2) if (match[v]==-1) {s[v]=0;kq.push(v);}
11
     while(!kq.empty()) {
12
       int e = kq.front(); kq.pop();
13
       if (s[e] %2==1) {
         s[match[e]] = s[e]+1;
15
         kq.push(match[e]);
16
       } else {
17
18
         forall(it,g[e]) if (it->to < nodes-2 && s[it->to]==-1) {
19
           s[it->to] = s[e]+1;
20
           kq.push(it->to);
21
         }
22
       }
23
     }
24
25 }
```

8.3. Edmonds Karp's

```
1 #define MAX V 1000
  #define INF 1e9
   //special nodes
   #define SRC 0
   #define SNK 1
   map<int, int> G[MAX_V];//limpiar esto
   //To add an edge use
   #define add(a, b, w) G[a][b]=w
   int f, p[MAX_V];
   void augment(int v, int minE){
    if(v==SRC) f=minE;
11
    else if(p[v]!=-1){
12
       augment(p[v], min(minE, G[p[v]][v]));
13
       G[p[v]][v]=f, G[v][p[v]]+=f;
14
    }
15
16
   ll maxflow(){//0(VE^2)
18
     11 Mf=0;
     do{
19
```

forn(v, N){

if (height[v] < k) continue;</pre>

count[height[v]]--;

23

24

25

```
f=0:
                                                                                           height[v] = max(height[v], N+1);
20
                                                                                   26
       char used[MAX_V]; queue<int> q; q.push(SRC);
                                                                                           count[height[v]]++;
                                                                                   27
^{21}
       zero(used), memset(p, -1, sizeof(p));
                                                                                           enqueue(v);
^{22}
                                                                                   28
       while(sz(q)){
                                                                                        }
23
                                                                                   29
         int u=q.front(); q.pop();
                                                                                   30
24
         if(u==SNK) break;
                                                                                      void relabel(int v) {
25
         forall(it, G[u])
                                                                                         count[height[v]]--;
26
                                                                                   32
           if(it->snd>0 && !used[it->fst])
                                                                                        height[v] = 2*N;
27
                                                                                   33
             used[it->fst]=true, q.push(it->fst), p[it->fst]=u;
                                                                                        forall(it, G[v])
28
                                                                                   34
       }
                                                                                          if(it->snd)
29
                                                                                   35
       augment(SNK, INF);
                                                                                            height[v] = min(height[v], height[it->fst] + 1);
30
                                                                                   36
                                                                                         count[height[v]]++;
       Mf+=f;
31
                                                                                   37
                                                                                         enqueue(v);
     }while(f):
32
                                                                                   38
     return Mf;
                                                                                   39
33
34 }
                                                                                      11 \max flow() {\frac{}{\sqrt{0}(V^3)}}
                                                                                         zero(height), zero(active), zero(count), zero(excess);
                       8.4. Push-Relabel O(N3)
                                                                                         count[0] = N-1;
                                                                                         count[N] = 1;
                                                                                        height[SRC] = N:
1 #define MAX V 1000
                                                                                   44
                                                                                        active[SRC] = active[SNK] = true;
  int N://valid nodes are [0...N-1]
                                                                                        forall(it, G[SRC]){
   #define INF 1e9
                                                                                   46
                                                                                          excess[SRC] += it->snd;
   //special nodes
                                                                                          push(SRC, it->fst);
   #define SRC 0
                                                                                   48
   #define SNK 1
                                                                                   49
                                                                                        while(sz(Q)) {
   map<int, int> G[MAX_V];
                                                                                   50
                                                                                          int v = Q.front(); Q.pop();
   //To add an edge use
                                                                                   51
                                                                                          active[v]=false;
   #define add(a, b, w) G[a][b]=w
                                                                                   52
                                                                                        forall(it, G[v]) push(v, it->fst);
   11 excess[MAX_V];
                                                                                   53
                                                                                        if(excess[v] > 0)
   int height[MAX_V], active[MAX_V], count[2*MAX_V+1];
                                                                                   54
                                                                                           count[height[v]] == 1? gap(height[v]):relabel(v);
                                                                                   55
   queue<int> Q;
12
                                                                                        }
   void enqueue(int v) {
                                                                                   56
13
     if (!active[v] && excess[v] > 0) active[v]=true, Q.push(v); }
                                                                                        ll mf=0:
                                                                                   57
14
                                                                                        forall(it, G[SRC]) mf+=G[it->fst][SRC];
   void push(int a, int b) {
                                                                                   58
15
                                                                                        return mf:
     int amt = min(excess[a], ll(G[a][b]));
                                                                                   59
16
                                                                                   60 }
     if(height[a] <= height[b] || amt == 0) return;</pre>
17
     G[a][b]-=amt, G[b][a]+=amt;
18
                                                                                                            8.5. Min-cost Max-flow
     excess[b] += amt, excess[a] -= amt;
19
     enqueue(b);
20
                                                                                    const int MAXN=10000:
21
   void gap(int k) {
                                                                                    2 typedef ll tf;
22
```

typedef 11 tc;

const tf INFFLUJO = 1e14;

5 | const tc INFCOSTO = 1e14;

```
6 struct edge {
     int u, v;
     tf cap, flow;
     tc cost;
9
     tf rem() { return cap - flow; }
11
   int nodes; //numero de nodos
   vector<int> G[MAXN]; // limpiar!
   vector<edge> e; // limpiar!
   void addEdge(int u, int v, tf cap, tc cost) {
     G[u].pb(sz(e)); e.pb((edge)\{u,v,cap,0,cost\});
     G[v].pb(sz(e)); e.pb((edge)\{v,u,0,0,-cost\});
18
   tc dist[MAXN], mnCost;
   int pre[MAXN];
   tf cap[MAXN], mxFlow;
   bool in_queue[MAXN];
   void flow(int s, int t) {
     zero(in_queue);
24
     mxFlow=mnCost=0;
25
     while(1){
26
       fill(dist, dist+nodes, INFCOSTO); dist[s] = 0;
27
       memset(pre, -1, sizeof(pre)); pre[s]=0;
28
       zero(cap); cap[s] = INFFLUJO;
29
       queue<int> q; q.push(s); in_queue[s]=1;
30
       while(sz(q)){
31
         int u=q.front(); q.pop(); in_queue[u]=0;
32
         for(auto it:G[u]) {
33
           edge &E = e[it];
34
           if(E.rem() \&\& dist[E.v] > dist[u] + E.cost + 1e-9){ // ojo EPS}
35
             dist[E.v]=dist[u]+E.cost;
36
             pre[E.v] = it;
37
             cap[E.v] = min(cap[u], E.rem());
38
             if(!in_queue[E.v]) q.push(E.v), in_queue[E.v]=1;
39
           }
40
         }
41
       }
42
       if (pre[t] == -1) break:
43
       mxFlow +=cap[t];
44
       mnCost +=cap[t]*dist[t];
^{45}
       for (int v = t; v != s; v = e[pre[v]].u) {
46
         e[pre[v]].flow += cap[t];
47
         e[pre[v]^1].flow -= cap[t];
48
```

```
49 | }
50 | }
51 | }
```

9. Plantilla

```
#include <bits/stdc++.h>
   using namespace std;
   #define forr(i, a, b) for(int i = (a); i < (int) (b); i++)
   #define forn(i, n) forr(i, 0, n)
   #define forall(it, v) for(auto it = v.begin(); it != v.end(); ++it)
   #define dforn(i, n) for(int i = ((int) n) - 1; i \ge 0; i--)
   #define db(v) cerr << #v << " = " << v << endl
   #define pb push_back
   typedef long long 11;
   const int MAXN = -1;
11
12 | int main() {
13
     return 0;
14
15 }
```

10. Ayudamemoria

Cant. decimales

```
#include <iomanip>
cout << setprecision(2) << fixed;</pre>
```

Rellenar con espacios(para justificar)

```
#include <iomanip>
cout << setfill('u') << setw(3) << 2 << endl;</pre>
```

Aleatorios

```
#define RAND(a, b) (rand()%(b-a+1)+a)
rand(time(NULL));
random_shuffle(A, A + n);
```

Comparación de Doubles

```
const double EPS = 1e-9;
x == y <=> fabs(x-y) < EPS
```

```
_3 | x > y <=> x > y + EPS
_4 | x >= y <=> x > y - EPS
                                Limites
  #include <limits>
  numeric_limits<T>
    ::max()
    ::min()
4
    ::epsilon()
                               Muahaha
 #include <signal.h>
  void divzero(int p){
    while(true);}
  void segm(int p){
    exit(0);}
   //in main
  signal(SIGFPE, divzero);
8 signal(SIGSEGV, segm);
                          Mejorar velocidad
i lios::sync_with_stdio(false);
                         Mejorar velocidad 2
   //Solo para enteros positivos
  inline void Scanf(int& a){
    char c = 0;
    while(c<33) c = getc(stdin);</pre>
    a = 0:
5
    while(c>33) a = a*10 + c - '0', c = getc(stdin);
6
7 | }
                             Expandir pila
#include <sys/resource.h>
2 | rlimit rl;
  getrlimit(RLIMIT_STACK, &rl);
 rl.rlim_cur=1024L*1024L*256L;//256mb
5 setrlimit(RLIMIT_STACK, &rl);
                                C++11
```

```
Leer del teclado

Leer del teclado

treopen("/dev/tty", "a", stdin);

Iterar subconjunto

for(int sbm=bm; sbm; sbm=(sbm-1)&bm)

File setup

// tambien se pueden usar comas: {a, x, m, 1}

touch {a..l}.in; tee {a..l}.cpp < template.cpp

Releer String

string s; int n;
getline(cin, s);
stringstream leer(s);
while(leer >> n){
    // do something ...
}
```