

Report on Visualization Project

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1 Introduction

In this project, the data we tackle with are the user ratings of the movies, and we aim to create two-dimensional illustrations of the latent factors. The formulation of the problem is:

$$Y_{M \times N} = U_{K \times M}^T V_{K \times N}$$

where M is the number of users, N is the number of movies, Y is the sparse rating matrix, U and V are the latent factors.

We first solve for U and V using Bias-Stochastic Gradient Descent (BSGD) method, and then, visualize U and V through PCA. (...)

2 Algorithm

2.1 Optimization

To solve for the latent factors U and V , we solve the following optimization problem:

$$\operatorname{argmin}_{U, V, a, b} \frac{\lambda}{2} (\|U\|^2 + \|V\|^2 + \|a\|^2 + \|b\|^2) + \sum_{(i,j) \in S} (Q_{i,j})^2$$

where $Q_{i,j} = (u_i^T v_j + a_i + b_j + \mu - Y_{i,j})$. Then,

$$\frac{\partial J}{\partial U_l} = \lambda U_l + \sum_{(i,j) \in S} 2Q_{i,j} 1_{i=l} V_j$$

We call the first term in the gradient as “norm term”, and the second term “error term”. U_l is updated iteratively through gradient method:

$$U_l^{n+1} = U_l^n - \eta \frac{\partial J}{\partial U_l}$$

In BSGD, for each iteration, we randomly loop through all the data and update U_l with “error term” only in the loop, then after the loop, correct U_l with “norm term”. We can do V_k , a_l and b_k similarly.

2.2 Visualization

We project U and V to 2 dimensions and visualize them. First, we compute SVD of V :

$$V = A\Sigma B^T$$

The first two columns of A correspond to best 2-dimensional projection of movies V .

Then, we project every movie ($V_{1:N}$) and user ($U_{1:M}$) using $A_{1:2}$:

$$\begin{aligned}\tilde{V} &= A_{1:2}^T V \in R^{2 \times N} \\ \tilde{U} &= A_{1:2}^T U \in R^{2 \times N}\end{aligned}$$

3 Implementation

3.1 Find U & V (BSGD.m)

To solve the optimization problem with Bias-SGD, we simply divide the data by 5 fold, use 4 folds as training data and 1 fold as test data to find the optimal damping parameter λ and number of iteration. The step size η is chosen as 1e-2 and is decreased by 10% for each iteration. From the results shown below (Figure 1), we choose $\lambda = 25$. For $\lambda = 25$, the out-of-sample error is still decreasing at the 100th iteration (Figure 1), however, the improvement is minimal. Therefore, we choose the number of iteration as 100.

3.2 Projection

To visualize the movie factor V , we choose 101 movies which we are familiar with. We project them, and color them with their tags (category). Since there could be several tags for one movie in the original data, we re-tag them uniquely according to our own understanding. The result is shown in (Figure 2). As an example, we show the "Romance", "Sci-Fi" and "Crime" clusters in Figure 3. We also show several representative series ("Star Trek", "Free Willy", "Godfather", "Batman", "Terminator", and "Hepburn") in Figure 4.

The user factor is projected in ???. Because we do not have any information about the users, we cannot discuss it further.

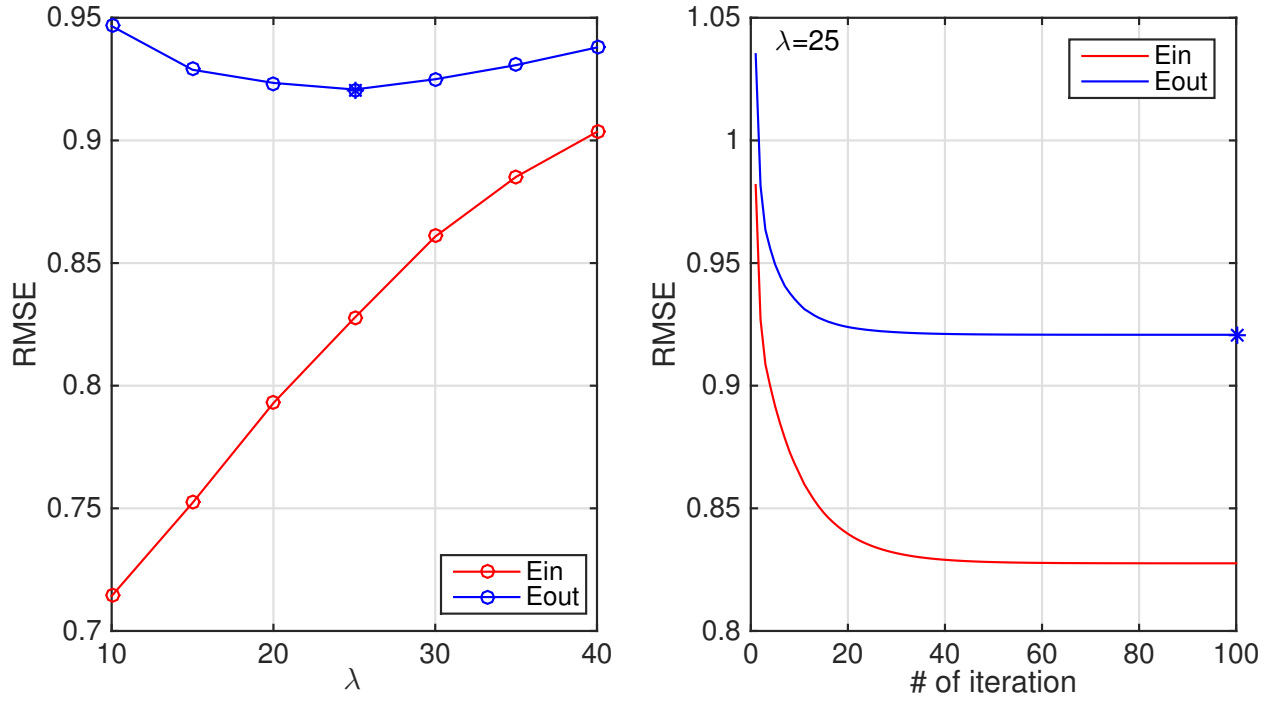


Figure 1: RMS error (RMSE) vs. Parameter. Left: For different λ , we plot the minimum RMSE in 100 iterations. We see that $\lambda = 25$ is the optimum choice. Right: For $\lambda = 25$, we plot the RMSEs in 100 iterations. We see that RMSE decays slowly after about 15 iterations. We simply choose the number of iteration as 100 for final run.

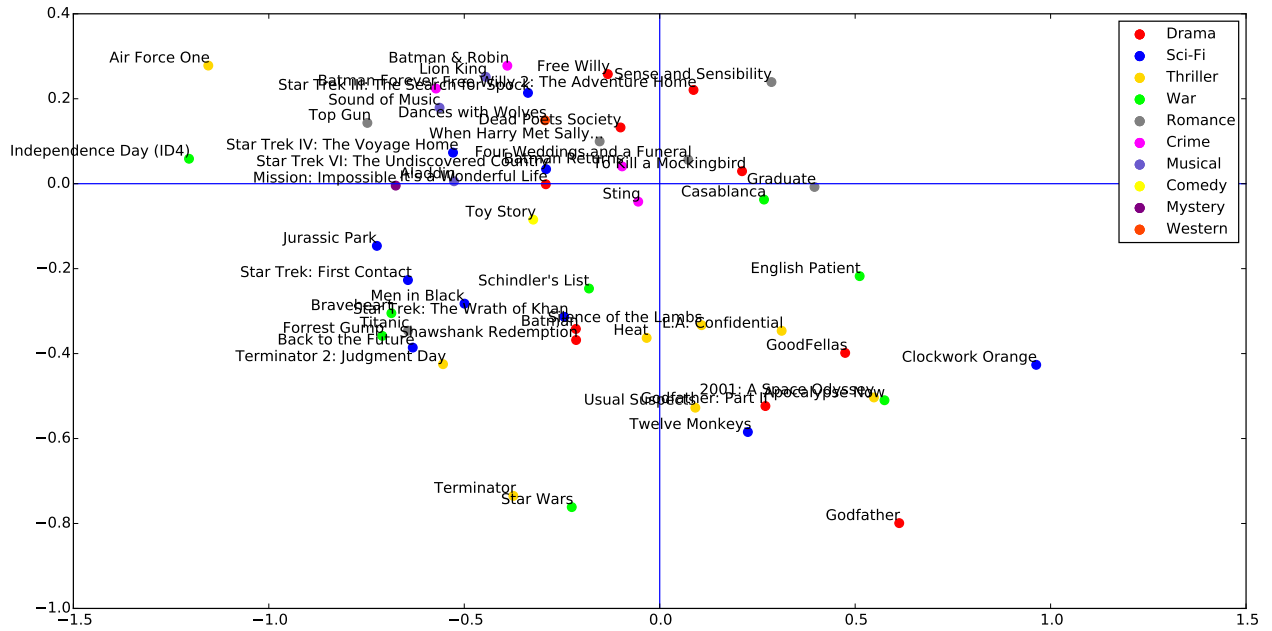


Figure 2: Projection of movie factor

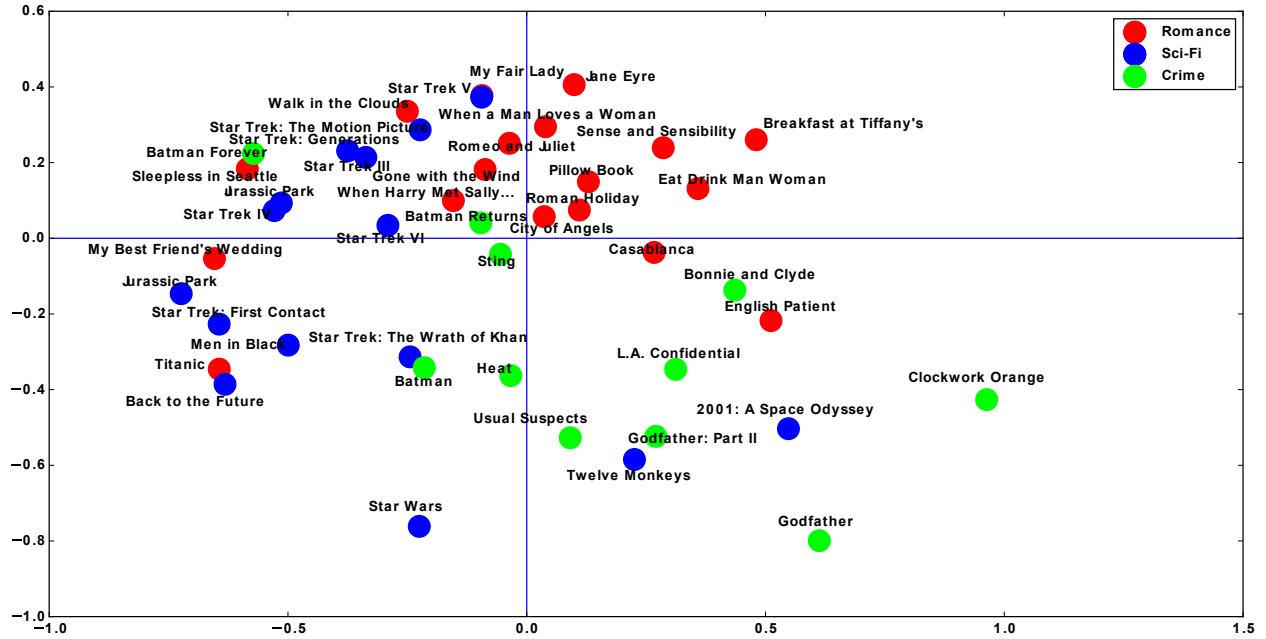


Figure 3: Projection of movie factor

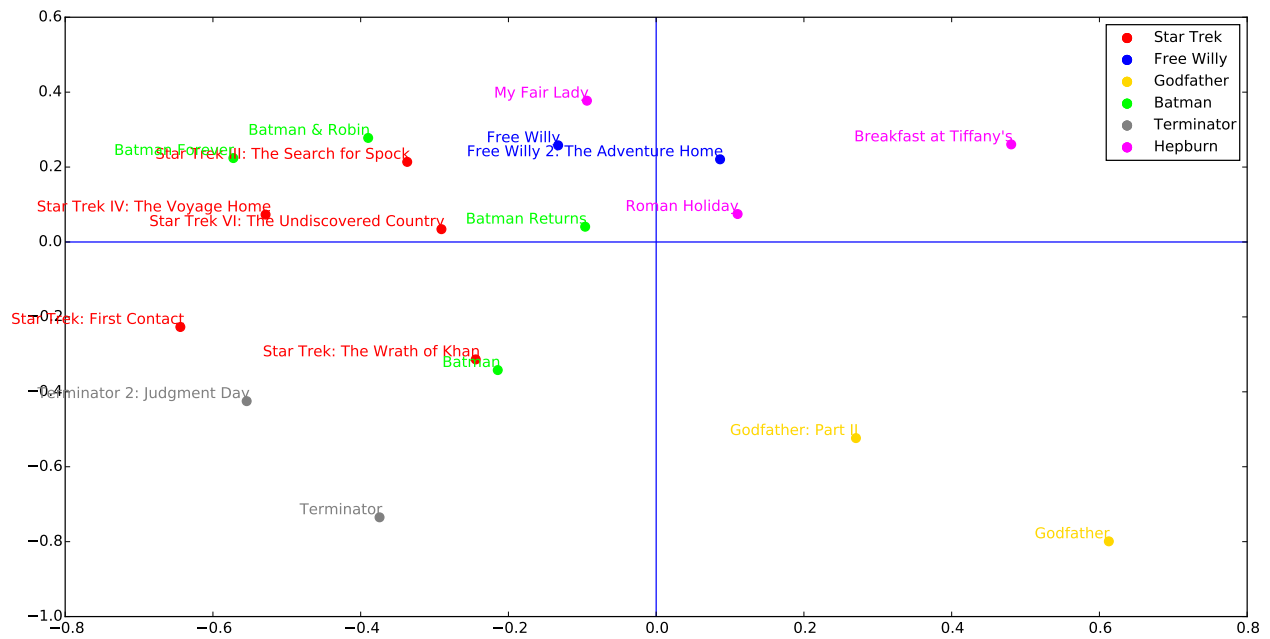


Figure 4: Projection of movie factor

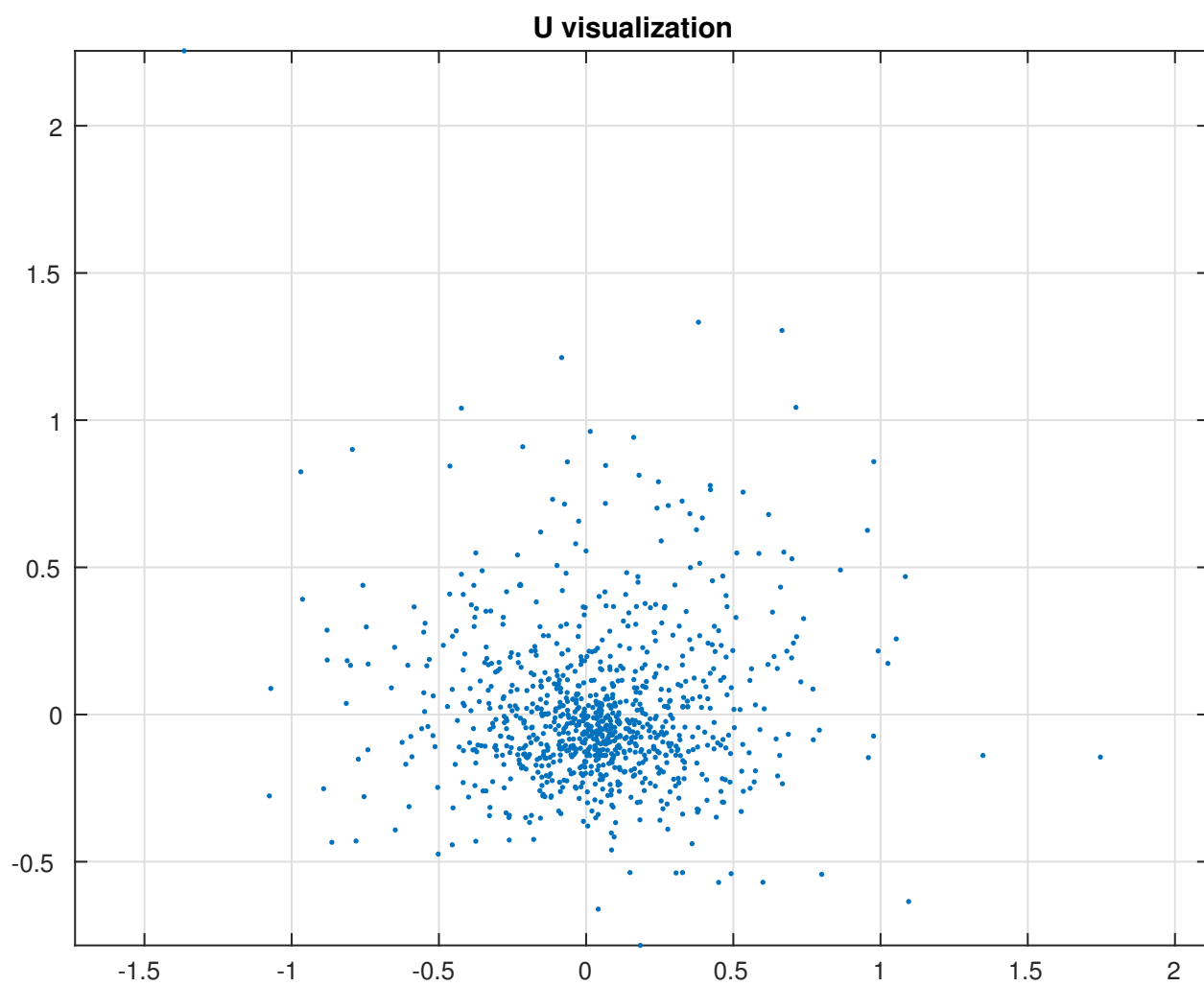


Figure 5: Projection of U

4 Discussions and Conclusions