Report on Visualization Project

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1 Introduction

2 Algorithm

2.1 Optimization

In the code (BSGD.m), we solve the following optimization problem:

$$\underset{U,V,a,b}{\operatorname{argmin}} \frac{\lambda}{2} \left(\|U\|^2 + \|V\|^2 + \|a\|^2 + \|b\|^2 \right) + \sum_{(i,j)\in S} \left(Q_{i,j} \right)^2$$

where $Q_{i,j} = (u_i^T v_j + a_i + b_j + \mu - Y_{i,j})$. Then,

$$\frac{\partial J}{\partial U_l} = \lambda U_l + \sum_{(i,j)\in S} 2Q_{i,j} 1_{i=l} V_j$$

2.2 Visualization

3 Implementation

3.1 Find U & V

To solve the optimization problem with Bias-SGD, we simply divide the data by 5 fold, use 4 folds as training data and 1 fold as test data to find the optimal damping parameter λ and number of iteration. The step size η is chosen as 1e-2 and is decreased by 10% for each iteration. From the results shown below (Fig. 1), we choose $\lambda = 25$. For $\lambda = 25$, the out-of-sample error is still decreasing at the 100th iteration (Fig. 1), however, the improvement is minimal. Therefore, we choose the number of iteration as 100.

3.2 Projection

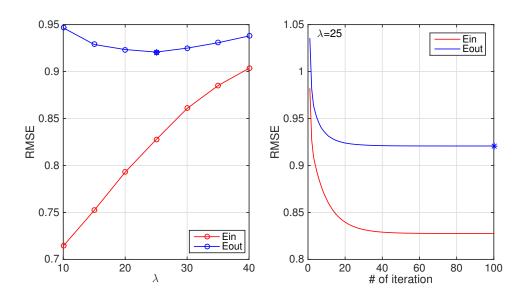


Figure 1: RMS error vs. Parameter