2. ϵ -outage probability

The simulation consists of two parts:

(1) Generate theoretical curve

Generate the theoretical curve under different L and SNR by

$$C_{\epsilon,\text{theoretical}} = \log \left(1 + F^{-1} (1 - \epsilon) \text{SNR} \right)$$

where $F(x) = P(\|h\|^2 > x)$ and $\|h\|^2$ is chi-square distribution with 2L degrees of freedom.

(2) Generate Simulated curve

To generate the simulated curve, recall the definition of ϵ -outage probability:

$$\epsilon(C) = P\left(\log(1 + ||h||^2 \text{SNR}) < C\right)$$

Given ϵ , L, and SNR, we first generate a large number $(N = 2L \cdot 10^6)$ of channel realizations from $\mathcal{CN}(0,1)$. For every 2L realization, we obtain $||h||^2$ by

$$||h||^2 = \sum_{l=1}^{2L} x_l^2$$

Calculate $\log(1+\|h\|^2 \text{SNR})$ for each $\|h\|^2$ and sort them into nondecreasing order. Let $k = N\epsilon$, and pick the kth smallest value from the sorted data, which is then the simulated result.

The comparison between theoretical computation and simulation is shown below. Solid lines represent the theoretical result and marked points show the simulated result.

