1. Differential In Single-Ended Out

(a)(b)

這題要做一個 Differential In Single-ended Out 的 Amplifier。這題的難度我認為不大,因為 spec 只要求 $A_V = 20$ dB 以及 BW = 5MHz。基本上只要讓所有的 MOS 偏壓在 Saturation 基本上就能 達到了。下面列出 A_V 和 BW 的公式幫助我們找方向

$$A_{v} \approx g_{mN}(r_{ON} \parallel r_{OP}) = \frac{2}{(\lambda_{N} + \lambda_{P})V_{ov}}$$

$$BW \approx \frac{1}{R_{out}C_{L}} = \frac{(\lambda_{N} + \lambda_{P})I_{D}}{C_{L}}$$

而我們可以調的參數分別是:

- 1. Differential pair 的 MOS 的 size -> 影響 λ, Vov
- 2. Current Source 的 MOS 的 size -> 影響 Vov, ID
- 3. V_b -> 影響 V_{ov}, I_D
- 4. V_{icm} -> 影響 operating point

可以看出 λ 在 Gain 和 BW 之間是反向的關係,而 I_D 和 V_{ov} 雖然是正向關係,但一個在分母一個在分子,因此這個會是我們 design 的一個限制,我們必須在兩者間作 tradeoff。但 λ 基本上只受 differential pair 的 size 中的 L 影響,所以我們可以不調整他們的 L,用其他來達成 spec。假設 C_L 固定,我的方向如下:**調高 ID** -> Vov 變大, V_{ov} 與小

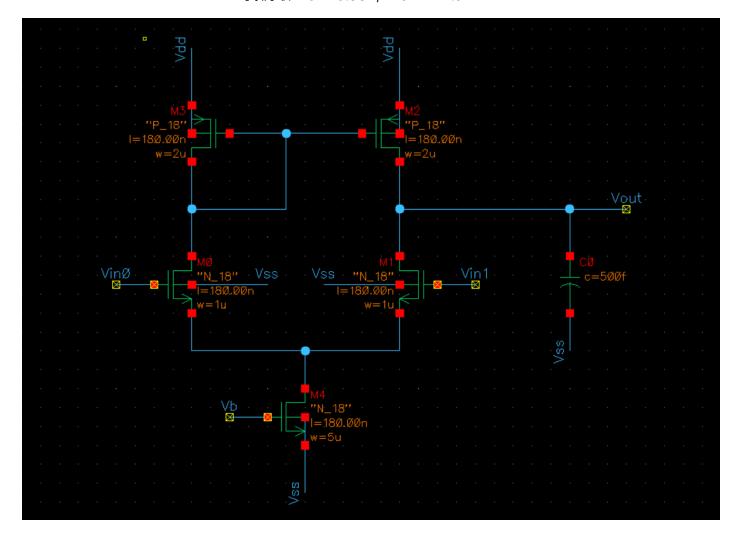
->調高 differential pair 的 W

->Vov 變小,gain 變大

事實上,我自己實作時只做完第一步就達成 spec 了。不過這個策略對後續的題目有幫助。

Schematic

我們取 Vb = 0.55V, Vicm = 1.3V



```
**** mosfets
subckt
element
         0:mm3
                    0:mm2
                               0:mm1
                                           0:mm0
                                                      0:mm4
model
                                           0:n 18.1
         0:p 18.1
                    0:p 18.1
                               0:n 18.1
                                                      0:n 18.1
region
         Saturation Saturation Saturation Saturation
                                 18.1314u
                                             18.1314u
 id
          -18.1314u -18.1314u
                                                        36.2628u
                                 -50.4203a
                                           -50.4203a -6.417e-21
 ibs
          2.478e-21
                     2.478e-21
                      88.2657a -118.7050a -118.7050a -149.6343a
 ibd
           88.2657a
         -671.7110m -671.7110m 648.2353m
                                           648.2353m
                                                       550.0000m
 vgs
         -671.7110m -671.7110m
                               476.5243m
                                           476.5243m
                                                       351.7647m
 vds
                       Θ.
                                -351.7647m -351.7647m
                                                         Θ.
 vbs
            Θ.
 vth
         -534.5841m -534.5841m
                               548.5272m
                                           548.5272m
                                                       512.5768m
                                142.3676m
                                           142.3676m
         -191.3452m -191.3452m
                                                       103.6204m
 vdsat
         -137.1269m -137.1269m
                                 99.7081m
                                             99.7081m
                                                        37.4232m
 vod
            1.1502m
                       1.1502m
                                  1.9991m
                                             1.9991m
                                                         9.9805m
                                                       507.4463m
 gam eff
          557.0845m
                     557.0845m
                                516.4853m
                                           516.4853m
          183.4018u
                     183.4018u
                                209.3913u
                                            209.3913u
                                                       564.9433u
 gm
            6.5198u
                       6.5198u
                                 11.2940u
                                             11.2940u
                                                        29.4075u
 gds
                                  23.5626u
           55.2108u
                      55.2108u
                                             23.5626u
                                                        84.3221u
 gmb
            2.4229f
                       2.4229f
                                  1.4042f
                                             1.4042f
                                                         7.1957f
 cdtot
            3.7584f
                       3.7584f
                                  1.8202f
                                              1.8202f
                                                         8.3931f
 cgtot
 cstot
            5.4364f
                       5.4364f
                                  2.5513f
                                              2.5513f
                                                        12.0865f
 cbtot
                       4.6917f
                                  2.4162f
                                              2.4162f
                                                        12.6990f
            4.6917f
            2.8008f
                       2.8008f
                                   1.3109f
                                              1.3109f
                                                         5.6226f
 cgs
          707.5300a
                     707.5300a
                                359.5321a
                                            359.5321a
                                                         1.8394f
 cgd
```

Hand Calculation : $A_v \approx g_{mN}(r_{ON} || r_{OP}) = 209.3913u * \frac{1}{11.2940u + 6.5198u} = 11.754 = 21.4dB$

Simulation: 21.2022dB

基本上差距也不大,跟模擬跟計算結果十分接近。

```
pole/zero analysis
  input = 0:vac
                           output = v(vout)
      poles (rad/sec)
                                       poles (hertz)
real
                imag
                                 real
                                                 imag
-34.3546x
                                 -5.46770x
                Θ.
                                                 Θ.
-19.3616g
                                 -3.08149g
                Θ.
                                                 Θ.
-42.9941g
                                 -6.84273g
                Θ.
                                                 Θ.
      zeros (rad/sec)
                                       zeros (hertz)
                imag
real
                                 real
                                                 imag
-35.3478g
                0.
                                 -5.62578q
                                                 0.
                0.
-48.4487g
                                 -7.71086g
                                                 Θ.
533.314g
                Θ.
                                 84.8796g
                                                 0.
```

```
capacitance table
  nodal
  node
                        node
                                              node
               cap
                                     cap
                                                           cap
                                = 11.3439f 0:net22
                                                         12.2984f
+0:in
                      0:net19
                                   20.2561f 0:vicm
+0:vb
              8.3931f 0:vdd
                                                         0.
              1.8202f 0:vin1
+0:vin0
                                    1.8202f 0:vout
                                                      = 503.8272f
+0:vss
          = 529.6180f
```



Hand Calculation:

1. Output Pole
$$\approx \frac{1}{R_{\text{out}}C_L} = \frac{1}{\frac{1}{11.2940u + 6.5198u} *503.8272f} = 35.357 \text{M(rad/s)}$$

2. Mirror Pole
$$\approx \frac{g_{mp}}{C_E} = \frac{183.4018u}{12.2984f} = 14.9G (rad / s)$$

3. First Zero
$$\approx 2\omega_{p2} = 29.8G(rad / s)$$

Simulation:

- **1. Ouput Pole** = 5.62578M * 2pi = 35.348M(rad / s)
- **2. Mirror Pole** = 7.71086G * 2pi = 15.422G(rad / s)
- **3. First Zero** = 5.62578G * 2pi = 35.348G(rad / s)

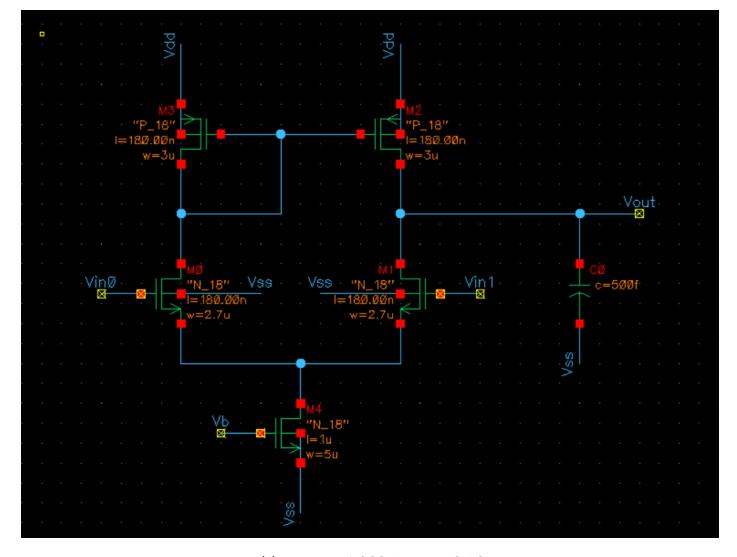
這題希望我們去 maximize FOM,這應該是這次作業最困難的部分。一樣我們先列個算式找方向

$$FOM = \frac{BW(MHz)}{Tail\ Current(uA)} = \frac{(\lambda_N + \lambda_P)I_D}{2I_DC_L} = \frac{(\lambda_N + \lambda_P)}{C_L}$$

可以看到基本上他只跟 λ 和 C_L 有關。 λ 跟 Differential pair 的 MOS 的 L 有關,而 C_L 則與 W*L 有關 (MOS 本身的寄生電容並聯 load capacitance)。 λ 跟 1/L 呈正比,但注意到我們在(a)中 L 已經是 0.18um(最小 L in CIC018)。在不做大修改之下 MOS 的寄生電容不太能影像 load capacitance,只能透過 V_{bias} 和 V_{icm} 進行微調來做精進。

另一種想法是,把 size 變大去影響 load capacitance,但是這要注意的地方是這個方法往往會大幅影響 gain,或者是掉出 saturation region。因此我最後是採取原先的架構進行微調,嘗試在 BW 不變的情況下去降低 Tail Current。

Schematic



With $V_{icm} = 1.303V$, $V_b = 0.56V$

```
**** mosfets
subckt
element
                    0:mm2
                                0:mm1
                                           0:mm0
         0:mm3
                                                       0:mm4
model
                    0:p 18.1
                                0:n 18.1
                                           0:n 18.1
                                                       0:n 18.1
         0:p 18.1
region
         Saturation Saturation Saturation Saturation
 id
          -11.9027u
                     -11.9027u
                                  11.9027u
                                             11.9027u
                                                         23.8053u
 ibs
          1.446e-21
                     1.446e-21 -180.9911a -180.9911a -4.213e-21
 ibd
          105.5285a 105.5285a -236.2364a -236.2364a -292.5164a
 vgs
         -602.4497m -602.4497m 615.3634m
                                           615.3634m
                                                        560.0000m
 vds
         -602.4497m -602.4497m
                                 209.9137m
                                            209.9137m
                                                        687.6366m
                       0.
                                -687.6366m -687.6366m
 vbs
            Θ.
                                                          Θ.
 vth
         -534.1576m -534.1576m
                                 607.1894m
                                           607.1894m
                                                        386.6257m
 vdsat
         -136.3237m -136.3237m
                                  93.0308m
                                             93.0308m
                                                        167.9130m
 vod
          -68.2921m
                     -68.2921m
                                   8.1740m
                                              8.1740m
                                                        173.3743m
            1.7990m
                        1.7990m
                                              5.4011m
                                                          1.5576m
 beta
                                   5.4011m
 gam eff
          557.0846m
                     557.0846m
                                 523.9725m
                                            523.9725m
                                                        507.4462m
                     167.5044u
          167.5044u
                                 204.2781u
                                            204.2781u
                                                        232.5681u
 gm
                                  14.9580u
 gds
            5.0874u
                       5.0874u
                                             14.9580u
                                                          2.8022u
 gmb
           49.5661u
                      49.5661u
                                  22.3644u
                                             22.3644u
                                                         46.0179u
                                   3.5658f
                                              3.5658f
                                                         6.7449f
 cdtot
            3.6082f
                       3.6082f
            5.3455f
                       5.3455f
                                   3.9996f
                                                         34.4447f
                                              3.9996f
 cgtot
                                                         38.7294f
            7.6037f
                       7.6037f
                                   5.2838f
                                              5.2838f
 cstot
 cbtot
            6.9071f
                       6.9071f
                                   5.7522f
                                              5.7522f
                                                         18.7259f
            3.8241f
                       3.8241f
                                   2.5477f
                                              2.5477f
                                                         30.0903f
 cgs
                                   1.0058f
            1.0629f
                       1.0629f
                                              1.0058f
                                                         1.7771f
 cgd
```

```
gaindb= 20.0031 at= 500.0000k
from= 500.0000k to= 12.5594g
band= 6.0514x
```

```
nodal
          capacitance table
  node
                cap
                         node
                                               node
                                 cap
                                                       cap
+0:in
                       0:net19
                                 = 17.8649f 0:net22
                                                           17.3126f
               Θ.
                                                       =
              34.4447f 0:vdd
                                                           0.
+0:vb
                                    29.0215f 0:vicm
                                                       =
           =
                                 = 1
+0:vin0
               3.9996f 0:vin1
                                 = 3.9996f 0:vout
                                                       = 507.1740f
          =
           = 568.9597f
+0:vss
```

Working item	Spec	Simulation	Calculation
Vdd	1.5V		
C _L	500fF		
Tail Current(uA)	Open 23.8053u		
Av(dB)	>20dB	20.0031	20.164
V _{icm}	>20dB	1.303V	
V_{ocm}	Open	23.8053uA	
V _b	Open	0.56V	
Size of NMOS	Open	$\frac{W}{L} = \frac{2.7u}{0.18u} m = 1$	
Size of PMOS	Open	$\frac{W}{L} = \frac{3u}{0.18u} m = 1$	
Size of Current Source	Open	$\frac{W}{L} = \frac{5u}{1u} m = 1$	
BW(MHz)	>5MHz	6.0514	6.29
FOM	BW / Tail Current	0.254	0.264

Hand Calculation

1.
$$A_v \approx g_{mN}(r_{ON} \mid\mid r_{OP}) = 204.2781u * \frac{1}{14.958u + 5.087u} = 10.191 = 20.164dB$$

2. BW
$$\approx \frac{1}{R_{\text{out}}C_{\text{L}}} = \frac{1}{\frac{1}{14.958u + 5.087u} * 507.174f} = 39.522 \text{M(rad/s)} = 6.29 \text{MHz}$$

3. FOM =
$$\frac{BW(MHz)}{Tail\ Current(uA)} = \frac{6.29}{23.8053} = 0.264$$

基本上都跟 simulation 差異不大,誤差基本上來自於數值誤差以及計算的公式本來就只是幫助我們 找方向而已。

2. Two Stage Amplifier

(a)

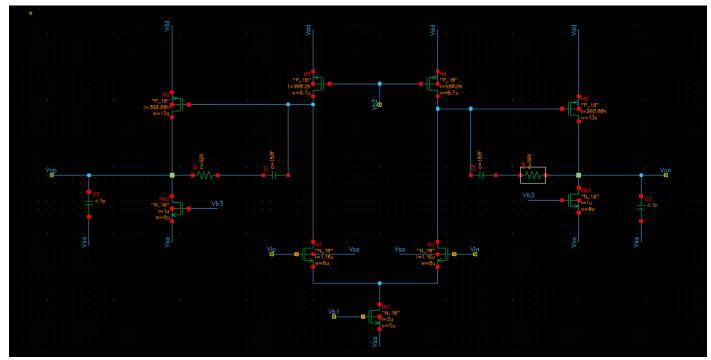
這題要做一個 Two Stage Amplifier。他有兩個 Gain Stage,而我們希望能達到 Gain > 60dB、
Unity Gain Frequency > 60MHz 以及 PM > 45°,後兩者我們可以靠 frequency compensation
來達成,但前提要是我們希望還沒做頻率補償前的 Unity Gain Frequency 能 > 60MHz 以及它是一個 stable system(negative phase at unity gain)。

Gain > 60dB(也就是 gain > 1000),基本上不難達成,因為它是一個 two stage Amplifier,而且兩個 stage 都有 high gain。所以我們應該把目標放在 Unity Gain Frequency,如果 first pole 太小,gain 會很快就 drop 到 unity gain。所以我們希望把 first pole 拉大。下面列出公式找方向: $A_v = g_{mn}(r_{o1} \parallel r_{o3}) \cdot g_{mp}(r_{o5} \parallel r_{omb2})$

要把 pole 調大就是要把 capacitance 調小,也就是 Second Stage W*L 要小,size 不能太大。我的方向如下:

- 1. 相較於 gain,更在意 pole 的位置
- 2. 將 pole 和 negative phase at unity gain 這兩個 spec 先達成
- 3. 最後再透過調整 first stage 的 size 來幫助達成 60dB, 並透過 bias 來讓所有 MOS 掉進 Saturation region。

Schematic



The information of the Circuit			
MOS	W/L	Bias	Voltage
M _{b1}	$\frac{5u}{2u}$	V _{b1}	0.45V
M _{b2}	$\frac{8u}{1u}$	V _{b2}	0.95V
M _{b3}	$\frac{8u}{1u}$	V _{b3}	0.48V
M _{1,2}	8 <i>u</i> 1.16 <i>u</i>	V_{icm}	1.29V
M _{3,4}	$\frac{8.7u}{0.9u}$	V_{ocm}	0.554V
M _{5,6}	$\frac{13u}{0.36u}$		

**** mosfets

subckt						
element	0:mm3	0:mm4	0:mm2	0:mm1	0:mm6	0:mmb3
model	0:p_18.1	0:p_18.1	0:n_18.1	0:n_18.1	0:p_18.1	0:n_18.1
region	Saturation	Saturation	Saturation	Saturation	Saturation	Saturation
id	-2.3220u	-2.3220u	2.3220u	2.3220u	-14.7403u	14.7403u
ibs	2.357e-22	2.357e-22	-492.9581a	-492.9581a	1.445e-21	-2.441e-21
ibd	246.4143a	246.4143a	-585.7830a	-585.7830a	579.7663a	-352.7806a
vgs	-550.0000m	-550.0000m	516.0774m	516.0774m	-580.3451m	480.0000m
vds	-580.3451m	-580.3451m	145.7323m	145.7323m	-946.1456m	553.8544m
vbs	Θ.	Θ.	-773.9226m	-773.9226m	Θ.	0.
vth	-496.1212m	-496.1212m	515.7103m	515.7103m	-510.4083m	386.1997m
vdsat	-94.0787m	-94.0787m	66.6708m	66.6708m	-114.6507m	113.4557m
vod	-53.8788m	-53.8788m	367.0445u	367.0445u	-69.9368m	93.8003m
beta	700.3310u	700.3310u	2.1587m	2.1587m	2.8229m	2.4890m
gam eff	557.0847m	557.0847m	525.7629m	525.7629m	557.0846m	507.4460m
gm	38.5668u	38.5668u	50.9119u	50.9119u	222.9552u	211.9540u
gds	148.0679n	148.0679n	1.2971u	1.2971u	1.7167u	2.4514u
gmb	11.5641u	11.5641u	7.3358u	7.3358u	65.7081u	43.0371u
cdtot	10.2389f	10.2389f	10.5130f	10.5130f	14.2914f	10.9838f
cgtot	45.8433f	45.8433f	40.0861f	40.0861f	32.1998f	54.0808f
cstot	52.2698f	52.2698f	38.0066f	38.0066f	41.1435f	60.5007f
cbtot	30.5267f	30.5267f	25.8339f	25.8339f	30.7396f	30.2449f
cgs	37.4762f	37.4762f	29.4700f	29.4700f	24.8505f	46.7345f
cgd	3.1270f	3.1270f	2.9757f	2.9757f	4.6648f	2.8497f

```
subckt
element
                     0:mmb2
                                 0:mmb1
         0:mm5
                                 0:n_18.1
model
         0:p_18.1
                     0:n_18.1
region
         Saturation Saturation Saturation
 id
          -14.7403u
                       14.7403u
                                    4.6440u
 ibs
          1.445e-21 -2.441e-21 -8.218e-22
 ibd
          579.7663a -352.7806a -329.2259a
         -580.3451m
                      480.0000m
                                  450.0000m
 vgs
         -946.1456m
                      553.8544m
                                  773.9226m
 vds
             Θ.
                        0.
                                    Θ.
 vbs
 vth
         -510.4083m
                      386.1997m
                                  350.3152m
                      113.4557m
         -114.6507m
                                  112.0485m
 vdsat
                       93.8003m
                                   99.6848m
 vod
           -69.9368m
 beta
             2.8229m
                        2.4890m
                                  759.2604u
 gam eff
          557.0846m
                      507.4460m
                                  507.4460m
          222.9552u
                      211.9540u
                                   65.5859u
 gds
             1.7167u
                        2.4514u
                                  542.3017n
           65.7081u
                       43.0371u
                                   13.2093u
 gmb
 cdtot
           14.2914f
                       10.9838f
                                    6.6403f
           32.1998f
                       54.0808f
                                   66.0516f
 cgtot
           41.1435f
                       60.5007f
 cstot
                                   70.3517f
           30.7396f
                       30.2449f
                                   27.4347f
 cbtot
                                   58.5407f
           24.8505f
                       46.7345f
 cgs
 cgd
            4.6648f
                        2.8497f
                                    1.7204f
```

Hand Calculation:

$$\begin{aligned} \mathbf{A_v} &= \ \mathbf{g_{mn}}(\mathbf{r_{o1}} \parallel \ \mathbf{r_{o3}}) \cdot \ \mathbf{g_{mp}}(\mathbf{r_{o5}} \parallel \ \mathbf{r_{omb2}}) \\ &= 50.9119u \cdot \frac{1}{1.2971u + 0.148u} \cdot 222.9552u \cdot \frac{1}{1.7167u + 2.4514u} = 1884 = 65.504dB \end{aligned}$$

基本上滿接近的,沒什麼誤差,而且也有滿足我們的 spec

- 1. 65.5038dB > 60dB
- 2. 73.0526MHz > 60MHz
- 3. -180° < Phase < 0° (在 unity gain 前兩個 pole)。

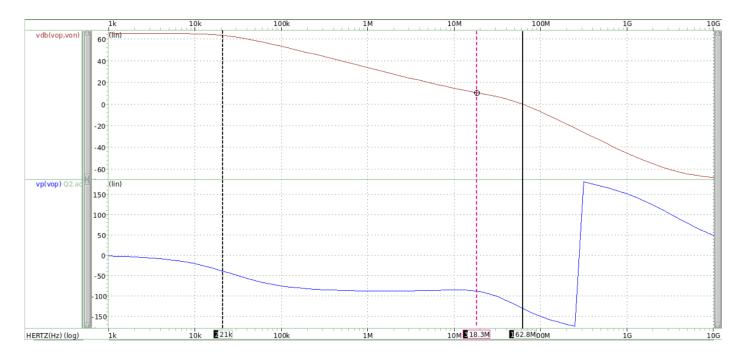
(b)

接著下面就開始做頻率補償啦!

以下是這個 design 用的 R_c 和 C_c · (e)的表格就先附在這裡了:

Performance Table			
Vdd	1.5V		
R _c , C _c	60kΩ 150fF		
V _{icm}	1.29V		
V_{ocm}	0.554		
Open-Loop Performance			
A _{DM} (> 60dB) 65.4974dB		74dB	
Unity Gain frequency(1pF load)(>60MHz)		61.5079MHz	
Phase Margin(> 45°) 49.5762°		762°	

下面是有做頻率補償的 bode plot



以下為 pole 和 zero 的位置:

- 1. First Pole 在 f = 21KHz = 131k(rad / s),可以看到從這點開始, gain 開始 drop
- 2. Zero 在 f = 18.3MHz = 115k(rad / s), 在這個點 gain drop 的幅度變小, 因為 zero 可以提供 +20dB/dec, 剛好抵銷掉前一個 Pole 的影響。
- 3. Second Pole 出現在 62.8MHz = 394.6M(rad/s),可以看到在這個點之後 gain 再次 drop。

```
pole/zero analysis
   input = 0:vac
                            output = v(vop, von)
                                        poles ( hertz)
      poles (rad/sec)
                 imag
real
                                                  imag
                                  real
-162.604k
                                 -25.8793k
-244.879x
                -125.997x
                                  -38.9737x
                                                   -20.0530x
-244.879x
                125.997x
                                 -38.9737x
                                                  20.0530x
      zeros (rad/sec)
                                        zeros (hertz)
                                  real
real
                imag
                                                  imag
-120.064x
                Θ.
                                  -19.1088x
                                                  0.
13.7786g
                Θ.
                                 2.19293q
                                                  Θ.
44.1062g
                0.
                                  7.01973g
                                                  0.
```

```
nodal capacitance table
  node
                         node
                cap
                                      cap
                                                node
                                                             cap
                       0:net15
                                 = 202.9517f 0:net3
                                                        = 150.0000f
+0:in
               Θ.
             82.6536f 0:net41
+0:net40
                                 = 202.9517f 0:net7
                                                        = 150.0000f
              66.0516f 0:vb2
+0:vb1
                                    91.6867f 0:vb3
                                                        = 108.1615f
           = 309.3594f 0:vicm
                                     0.
                                              0:vin
                                                          40.0861f
+0:vdd
                                                        =
              40.0861f 0:von
                                     1.0253p 0:vop
+0:vip
                                                            1.0253p
               2.3309p
+0:vss
```

$$A_{v2}=53.5$$
 , Rs = $r_{o1,2}\parallel r_{o3,4}=691961\,\Omega$, $R_L=r_{o5,6}\parallel r_{omb2}=239917\,\Omega$, $C_E=C_{gs}\approx 5 {
m fF}$

Simulation

- 1. First Pole = 162.604k(rad / s)
- 2. Second Pole = $(244.879^2 + 125.997^2)^{1/2} M(rad / s) = 275.4M(rad / s)$
- 3. Zero = -120.064M(rad / s)

Hand Calculation

$$\mathsf{Rs} = r_{o1,2} \parallel r_{o3,4} = 691961\Omega \ , \ R_L = r_{o5,6} \parallel r_{omb2} = 239917\Omega \ , \ C_E = C_{net41} \approx 53 \mathrm{fF}$$

$$\begin{split} \text{1. First Pole} &= \ \omega_{\text{p1}} \approx \frac{1}{R_{\text{S}} \left((1 + A_{\text{V2}}) \left(C_{\text{c}} + C_{\text{gd}} \right) + C_{\text{E}} \right) + R_{\text{L}} \left(C_{\text{c}} + C_{\text{gd}} + C_{\text{L}} \right)} \\ &= \frac{1}{691961* \left((1 + 53.49)*155*10^{-15} + 25*10^{-15} \right) + 239917*1.155*10^{-12}} = 162.902 \text{K(rad / s)} \end{split}$$

2. Second Pole =
$$\frac{g_{m5,6}}{c_E + c_L}$$
 = 274.395M(rad / s)

3. Zero =
$$\omega_z = \frac{1}{C_C(g_{m5.6}^{-1} - R_Z)} = -120M(rad / s)$$

基本上誤差都不大,second pole 的差距相對比較大。我認為誤差來自我們的計算公式是經過兩次簡化,本來誤差就會比較大。但確實能大致找到 pole 的位置。再加上 pole 有虛數,也就是會讓電路產生較不穩定的震盪,使其需要較久時間才可達到穩態

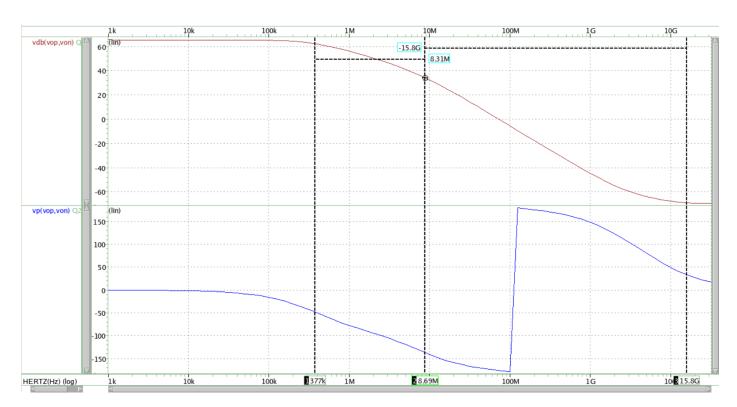
這題我們把 Compensate resistor and capacitor 拿掉,不做頻率補償,結果如下:

1. First Pole = 377kHz

3. Unity Gain frequency = 73.1MHz

2. Second Pole = 8.69MHz

4. Zero = 15.8GHz



```
pole/zero analysis
   input = 0:vac
                            output = v(vop, von)
      poles (rad/sec)
                                        poles (hertz)
real
                 imag
                                  real
                                                   imag
-2.30112x
                                  -366.234k
                                                   Θ.
-48.2326x
                                  -7.67645x
      zeros (rad/sec)
                                        zeros (hertz)
real
                                  real
                imag
                                                   imag
                                  2.19293g
13.7786g
                 0.
                                                   Θ.
47.6606g
                                  7.58542g
                                                   Θ.
```

```
y
gaindb= 65.5038 at= 1.0000k
from= 1.0000k to= 10.0000g
unit_gain= 73.0526x
phase_p=-176.0957
```

```
nodal capacitance table
  node
                        node
                                     cap
                                              node
                                                           cap
                      0:net15
                                = 52.9517f 0:net40
                                                         82.6536f
+0:in
                                                      = 1
          = 52.9517f 0:vb1
+0:net41
                                = 66.0516f 0:vb2
                                                         91.6867f
          = 108.1615f 0:vdd
                                = 309.3594f 0:vicm
          = 40.0861f 0:vip
                                  40.0861f 0:von
                                                          1.0253p
+0:vop
              1.0253p 0:vss
                                    2.3309p
```

Simulation

- 1. First Pole = 2.3M(rad / s)
- 2. Second Pole = 48.2326M(rad / s)
- 3. Zero = 13.7786G(rad / s)

Hand Calculation

$$A_{\rm v2}=53.5~,~{\rm Rs}=~r_{o1,2}\parallel~r_{o3,4}=691961~\Omega~,$$

$$R_L=~r_{o5,6}\parallel~r_{omb2}=239917~\Omega~,~C_E=~C_{gs}\approx25{\rm fF},~C_{gd}~\approx5{\rm fF}$$

1. First Pole =
$$\omega_{p1} \approx \frac{1}{R_S((1+A_{v2})Cgd+Cgs)}$$

= $\frac{1}{691961*((1+53.5)*5f+25f))}$ = 4.858 M (rad / s)

2. Second Pole =
$$\omega_{p2} \approx \frac{R_S((1+A_{v2})C_{gd}+C_E)+R_L(C_{gd}+C_L)}{R_SR_L(C_EC_{gd}+C_{gd}C_L+C_LC_E)} = 41.211M(rad/s)$$

3. Zero =
$$\omega_z = \frac{g_{m5,6}}{c_{gd}} = 44.6G(\text{rad/s})$$

可以看到我們的計算結果跟模擬有些差距。首先,first pole 和 second pole 的誤差都不大。但是我

們算出來的 zero 反而不是 RHP First Zero, 而是第二個 Zero。

頻率補償靠著額外加的電容,透過 miller effect 壓低 second pole 的位置,進而拉低 unity gain frequency,使 phase margin 拉大,讓這個電路變成 stable。原先的電路可能會因為有許多 pole,導致 phase 不斷變大,回授使其變成一個 unstable 的系統。但這個做法要付出的代價就是 BW 會降低,Unit Gain Bandwidth 提前到來的情況。而 Rc 在這個電路扮演的腳色在於控制又半平面的 pole,如果設計的好有機會與 pole 相消。

(e)

Performance Table			
Vdd	1.5V		
R _c , C _c	60kΩ 150fF		
V_{icm}	1.29V		
V_{ocm}	0.554		
Open-Loop Performance			
A _{DM} (> 60dB) 65.4974dB		74dB	
Unity Gain frequency(1pF load)(>60MHz)	61.5079MHz		
Phase Margin(> 45°)	49.5762°		