

# Model .Derivative

Tree Transformation Illustrations

# Notations

- $x$  and  $y$  represent any variable nodes.
- **A** and **B** represent any subtrees.
- **Purple node** represents the argument node of the tree transformation function.
- **Orange node** comes from node's duplication, which requires a positioning sequence (argument node  $\rightarrow$  template node) as an item of the generation sequence.
- **Teal subtree** comes from subtree's duplication, which requires a Primer and a positioning sequence (argument node  $\rightarrow$  template subtree's root node) as two items of the generation sequence.
- The sequence of <sub>1</sub>s and <sub>2</sub>s at the bottom-right corner of the node(subtree) is its(its root node's) positioning sequence.
- The number at the bottom-left corner of the node(subtree) is its(its root node's) traversal order in depth-first search(DFS).

### Element.LeftIdentity

$$\begin{array}{c} | \\ + \\ / \backslash \\ 0_1 \quad \mathbf{A}_r \end{array} \longrightarrow \begin{array}{c} | \\ {}_1\mathbf{A} \end{array}$$

$$\begin{array}{c} | \\ \times \\ / \backslash \\ 1_1 \quad \mathbf{A}_r \end{array} \longrightarrow \begin{array}{c} | \\ {}_1\mathbf{A} \end{array}$$

# Element.RightIdentity

$$\begin{array}{c} | \\ + \\ / \quad \backslash \\ \mathbf{A}_1 \quad 0_r \end{array} \longrightarrow \begin{array}{c} | \\ {}_1\mathbf{A} \end{array}$$

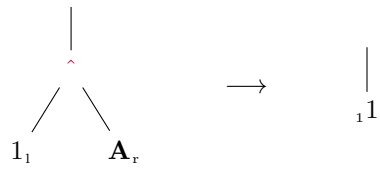
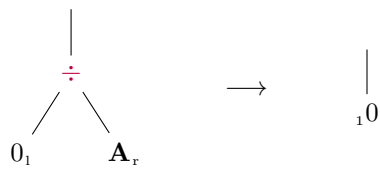
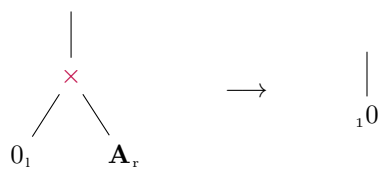
$$\begin{array}{c} | \\ - \\ / \quad \backslash \\ \mathbf{A}_1 \quad 0_r \end{array} \longrightarrow \begin{array}{c} | \\ {}_1\mathbf{A} \end{array}$$

$$\begin{array}{c} | \\ \times \\ / \quad \backslash \\ \mathbf{A}_1 \quad 1_r \end{array} \longrightarrow \begin{array}{c} | \\ {}_1\mathbf{A} \end{array}$$

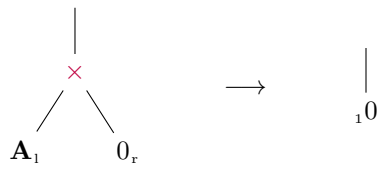
$$\begin{array}{c} | \\ \div \\ / \quad \backslash \\ \mathbf{A}_1 \quad 1_r \end{array} \longrightarrow \begin{array}{c} | \\ {}_1\mathbf{A} \end{array}$$

$$\begin{array}{c} | \\ \wedge \\ / \quad \backslash \\ \mathbf{A}_1 \quad 1_r \end{array} \longrightarrow \begin{array}{c} | \\ {}_1\mathbf{A} \end{array}$$

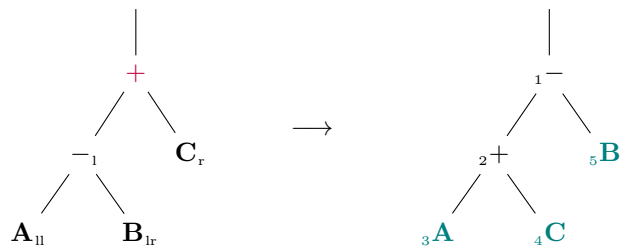
**Element.LeftZero**



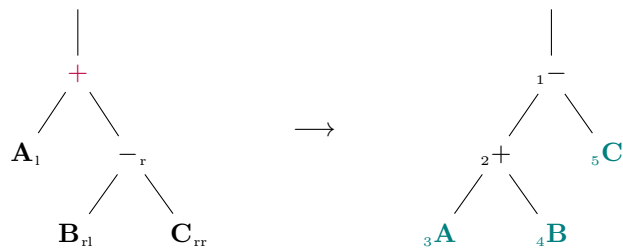
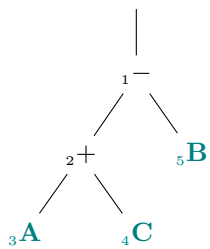
**Element.RightZero**



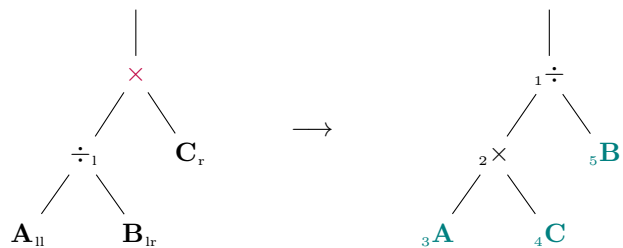
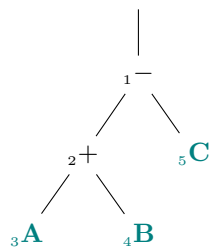
# Element.Merger



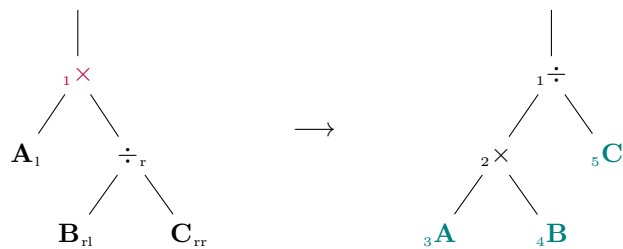
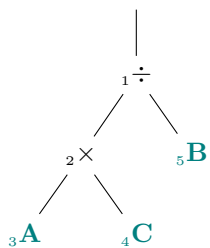
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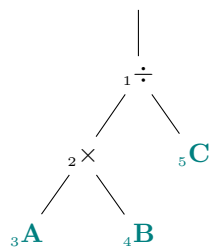
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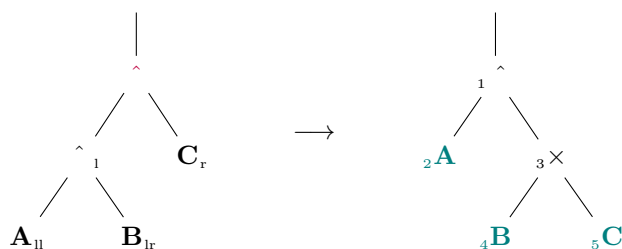
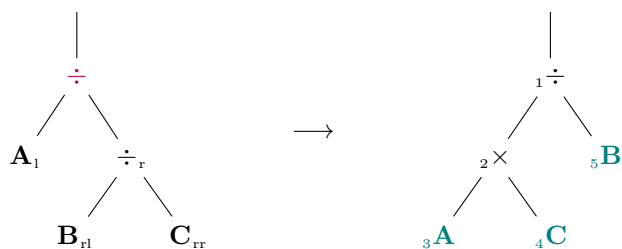
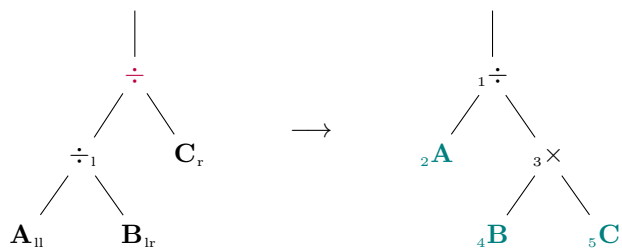
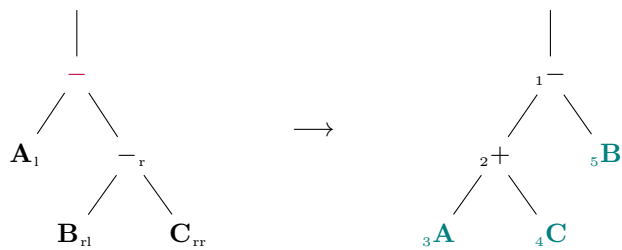
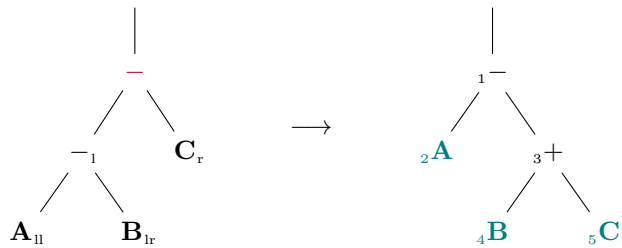
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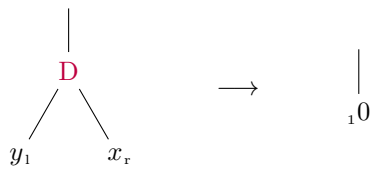
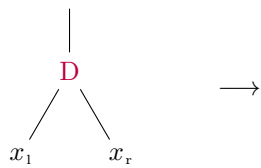


## Element.Absorption

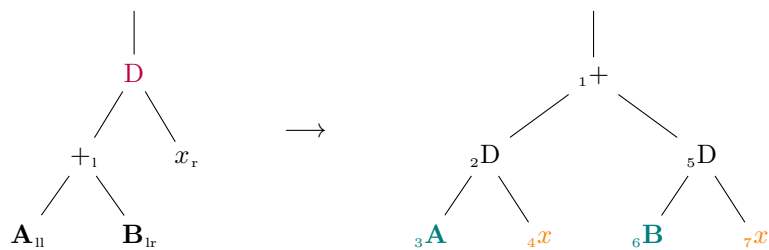




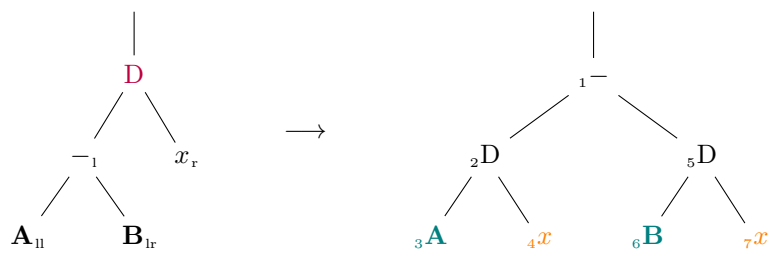
## Derivative.Element



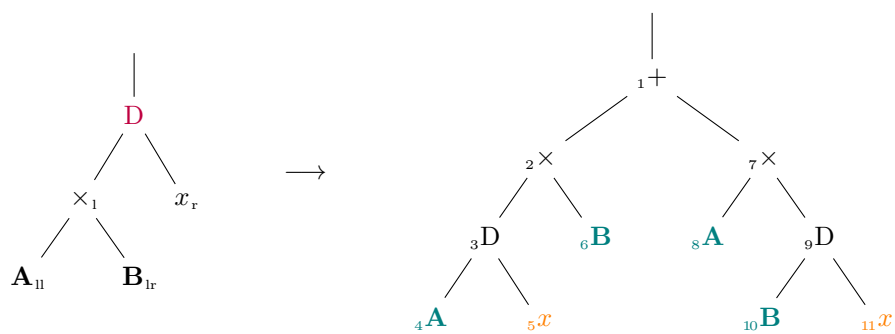
### Derivative.Addition



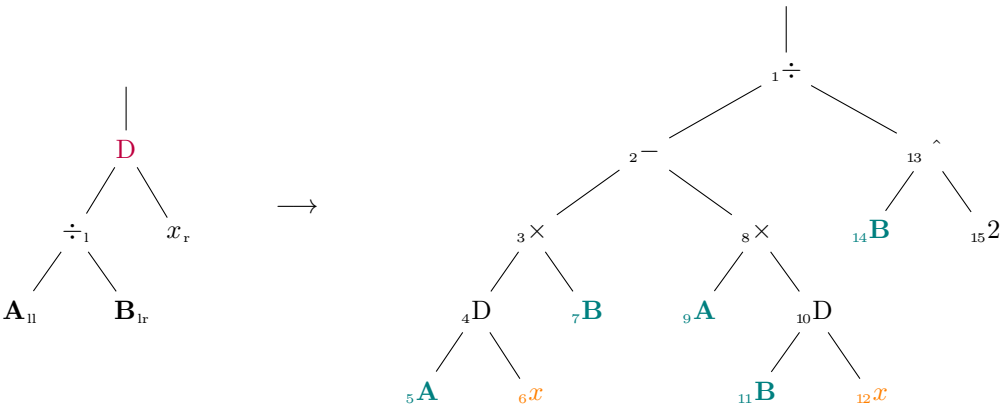
### Derivative.Subtraction



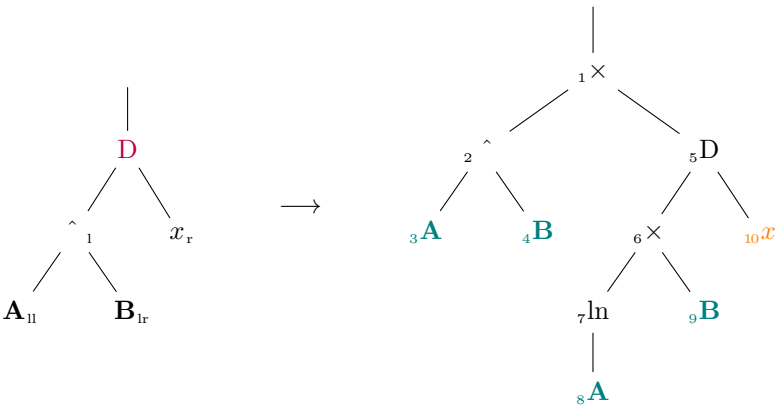
### Derivative.Multiplication



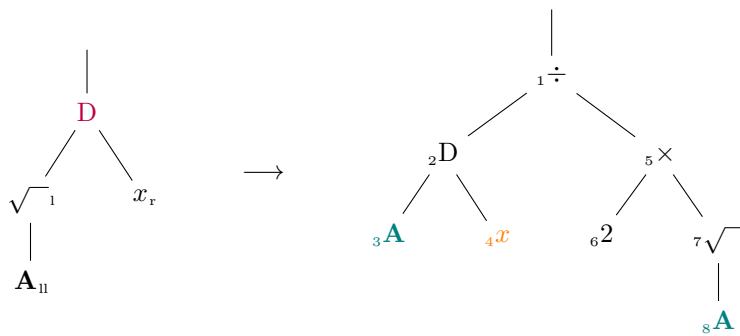
Derivative.Division



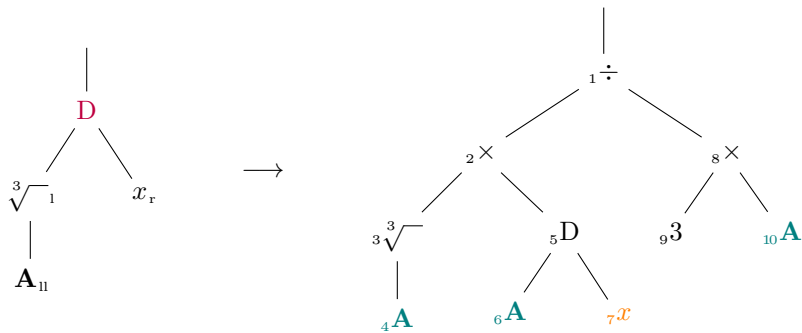
Derivative.Power



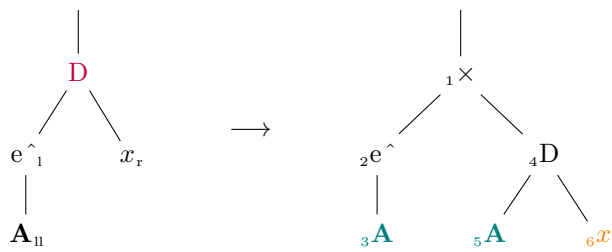
### Derivative.SquareRoot



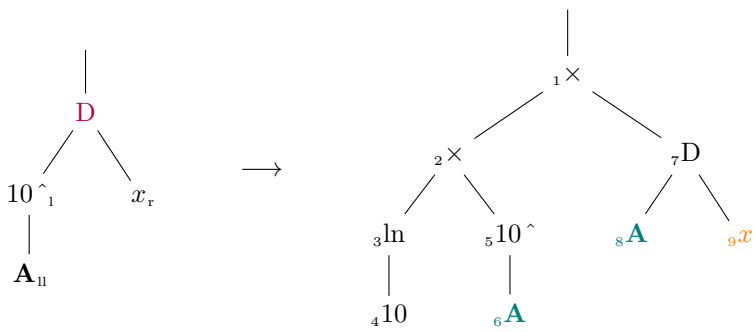
### Derivative.CubeRoot



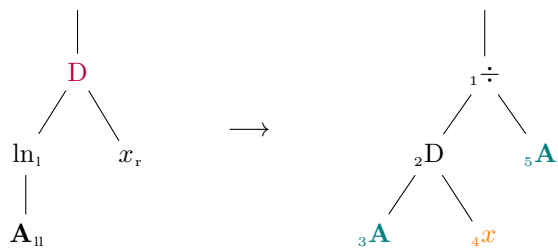
### Derivative.NaturalExponent



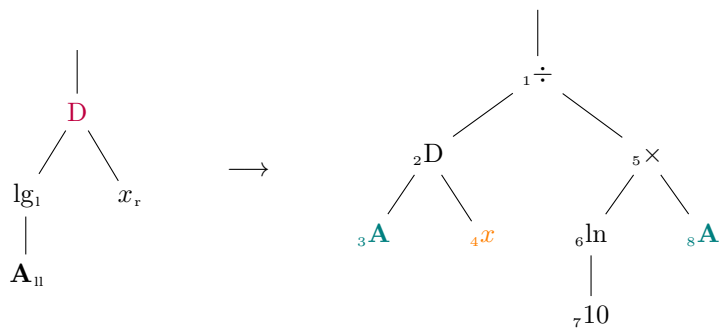
### Derivative.DecimalExponent



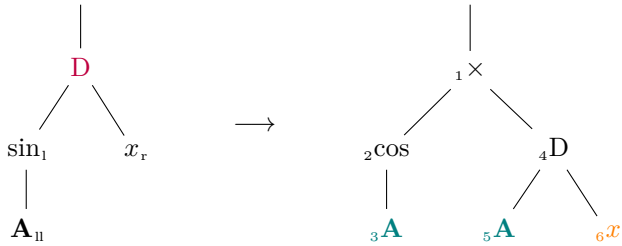
### Derivative.NaturalLogarithm



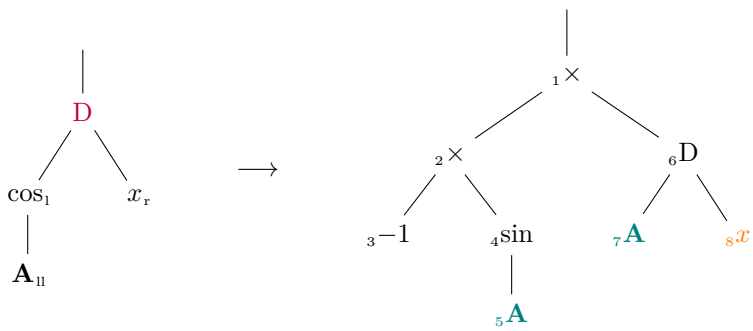
### Derivative.DecimalLogarithm



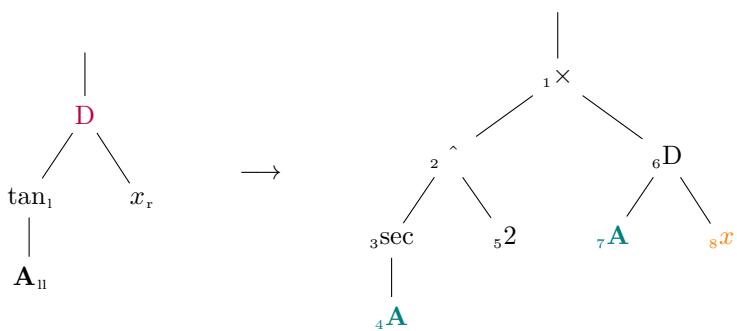
### Derivative.Sine



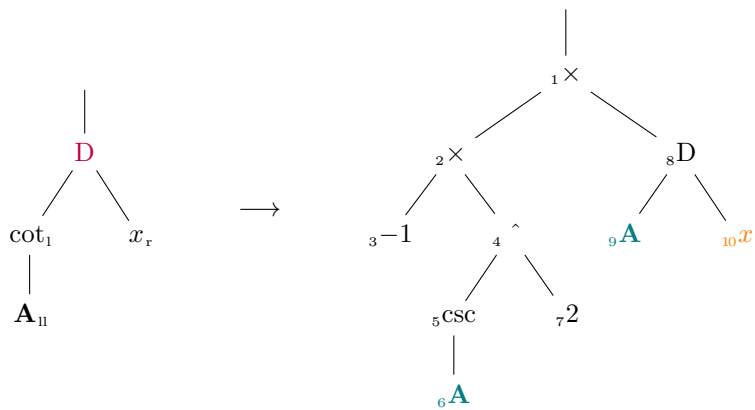
### Derivative.Cosine



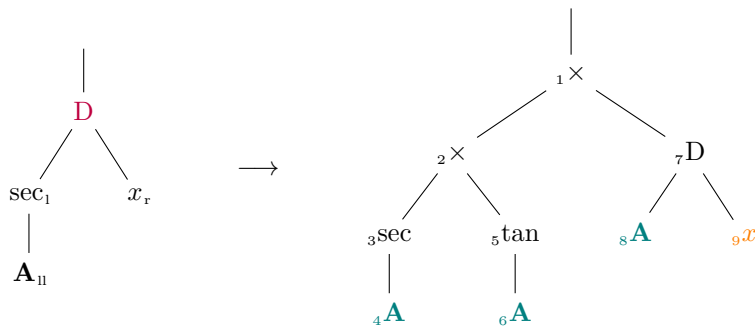
### Derivative.Tangent



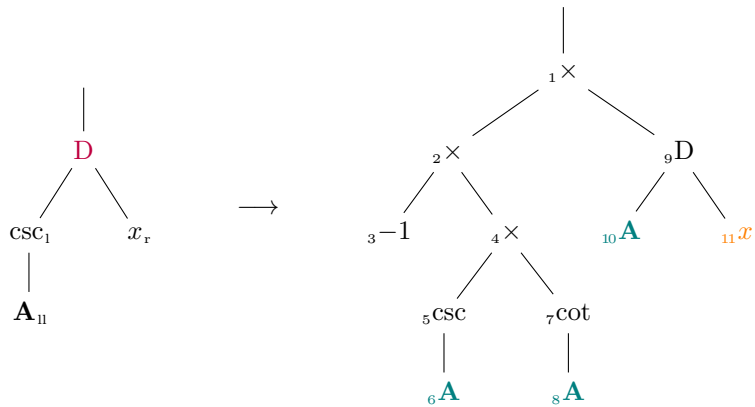
## Derivative.Cotangent



## Derivative.Secant

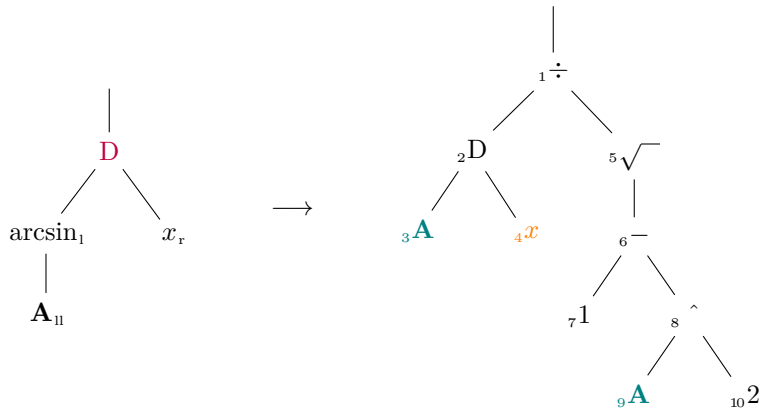


## Derivative.Cosecant

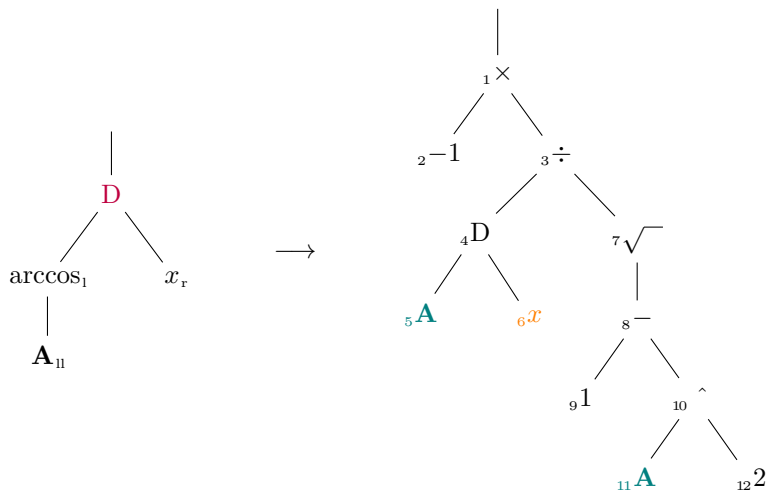




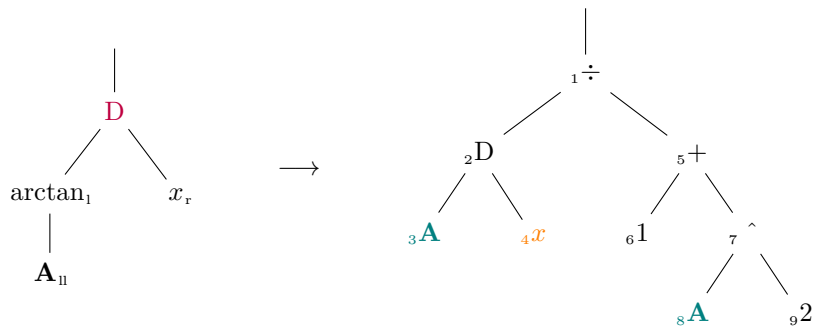
## Derivative.InverseSine



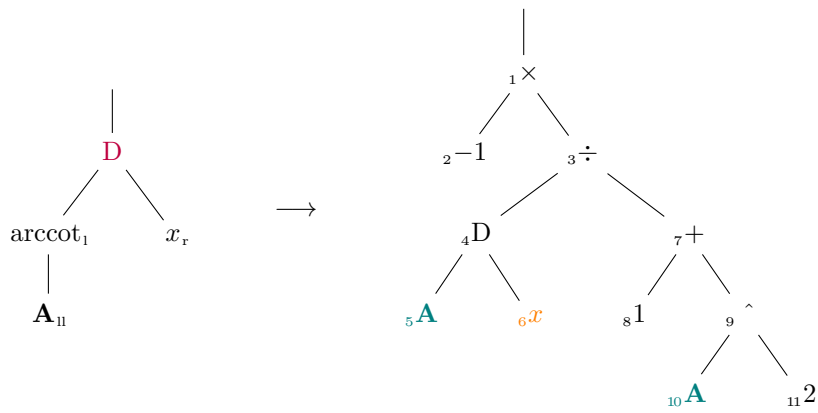
## Derivative.InverseCosine



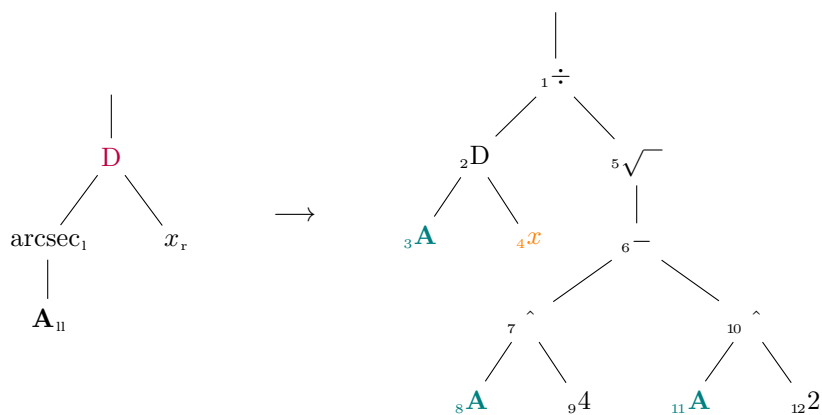
### Derivative.InverseTangent



### Derivative.InverseCotangent



## Derivative.InverseSecant



## Derivative.InverseCosecant

