

Block Ciphers

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CUNY - Hunter College

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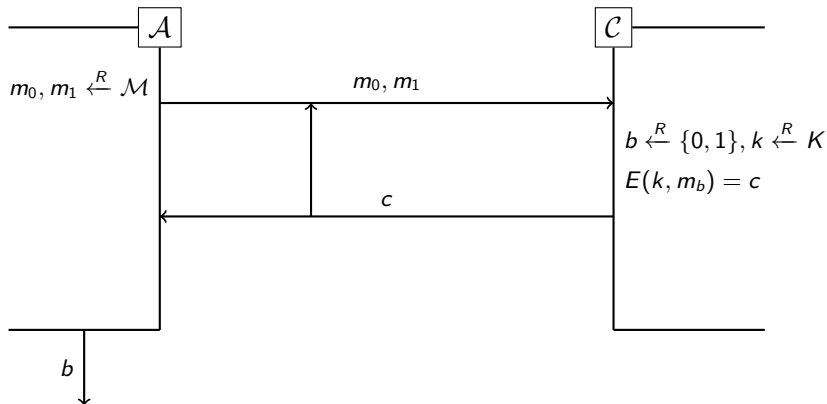
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One Time Pad Security Game: Chosen Plaintext Attack



Pseudo Random Functions (PRFs)

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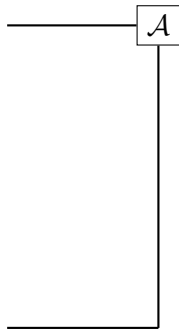
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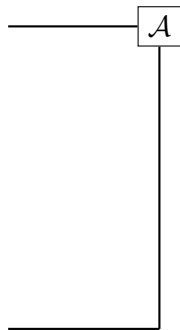
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PRF Security Game: Chosen Plaintext Attack

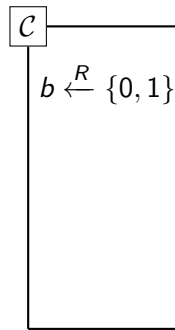
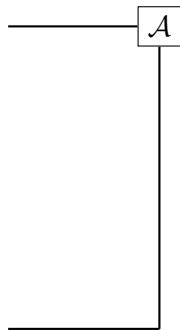
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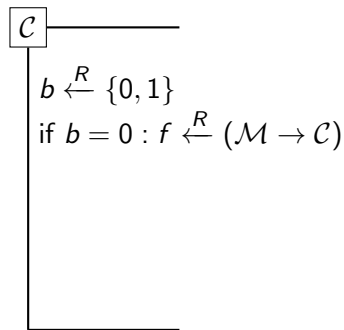
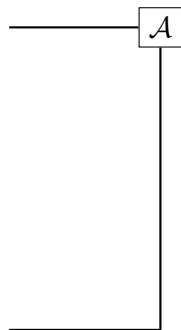
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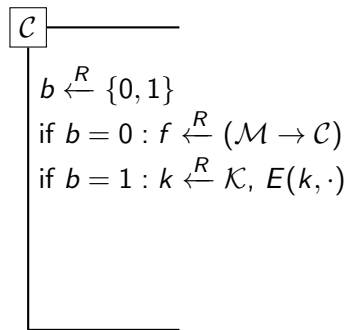
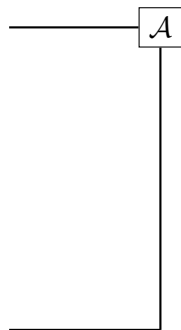
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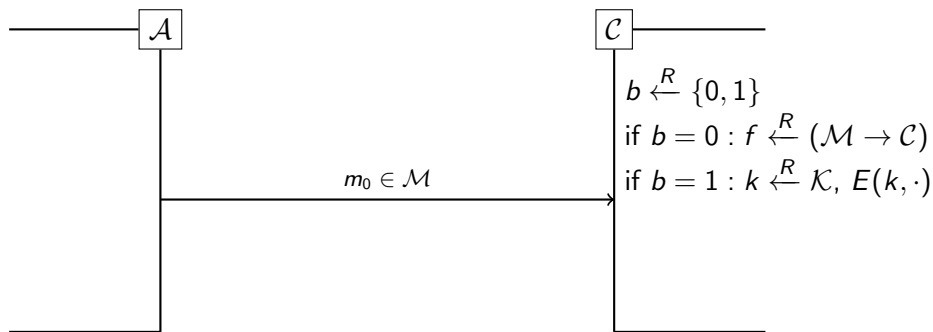
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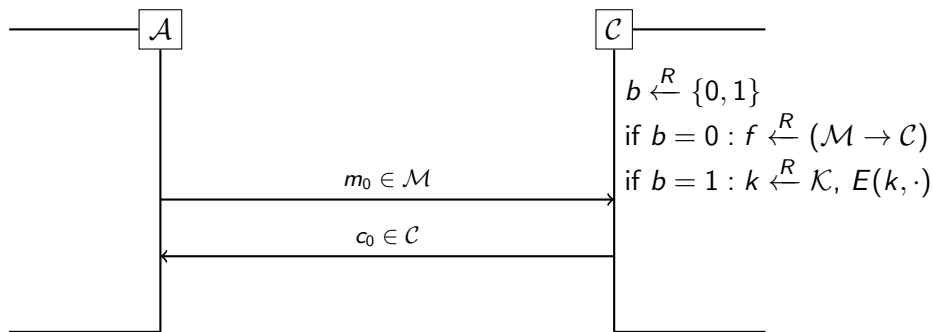
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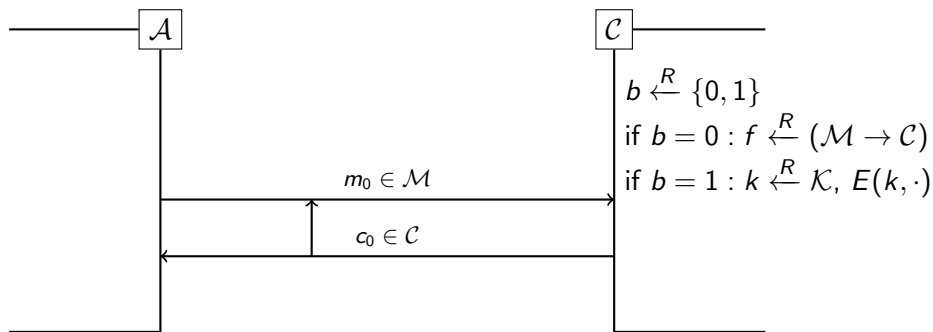
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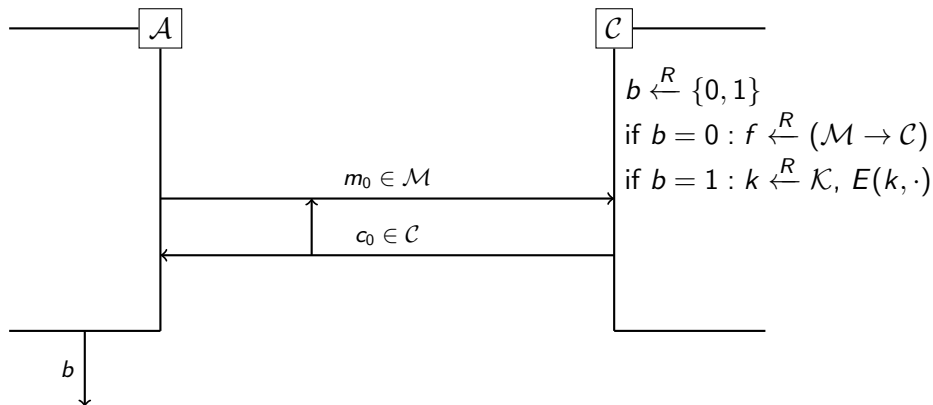
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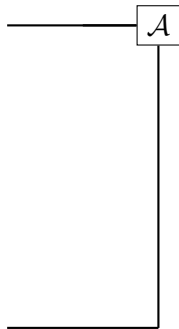


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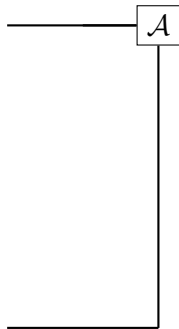


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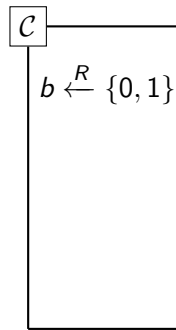
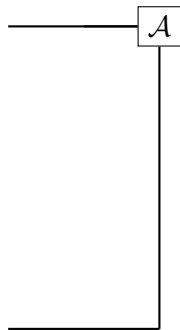
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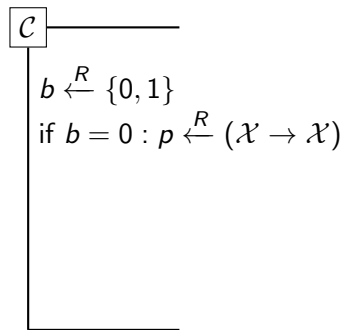
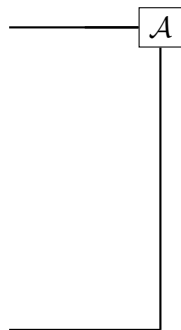
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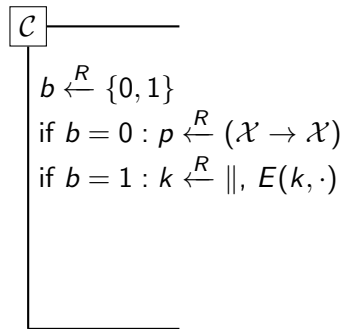
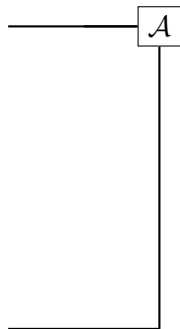
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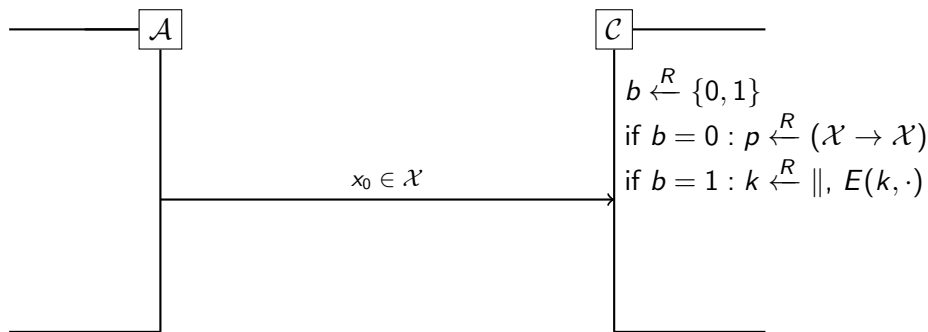
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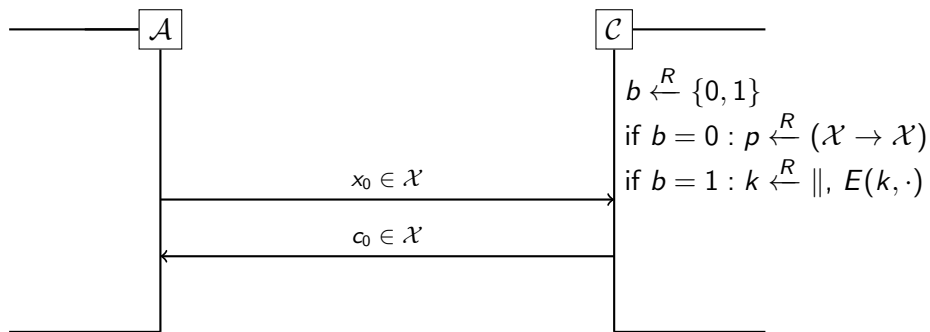
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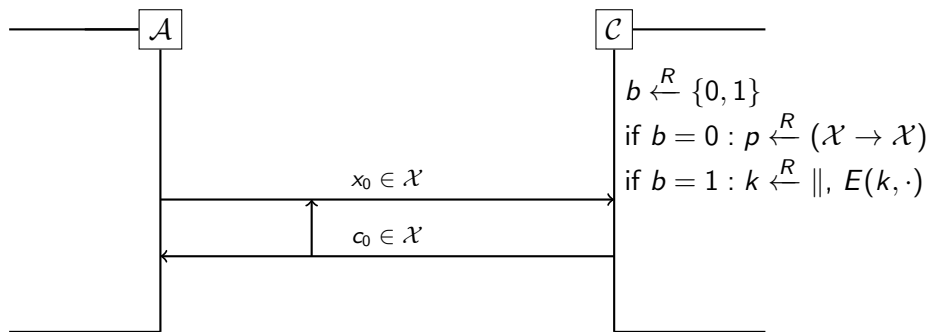
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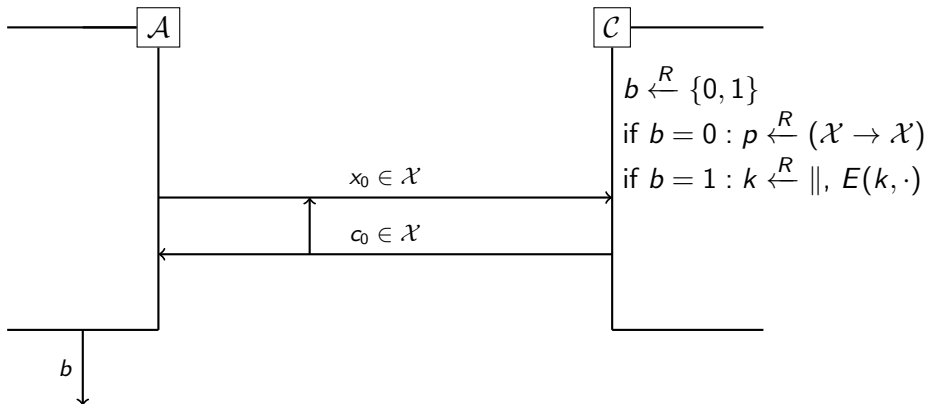
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Security Lemma

- a secure PRP is equivalent to a secure PRF

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- its message space and ciphertext space are the same: $\mathcal{M} = \mathcal{C}$
- Shares the correctness requirement with Shannon Ciphers
 $D(k, E(k, m)) = m$

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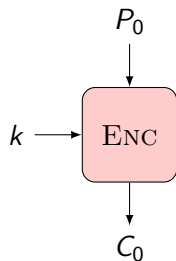


Image Credit: Diana Maimut

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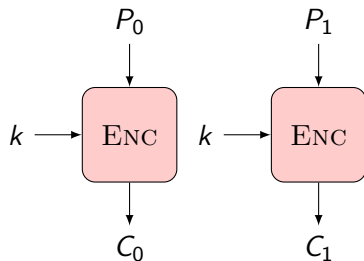


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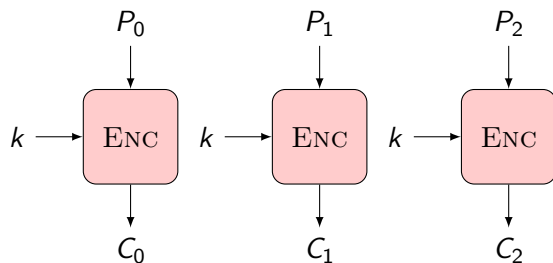


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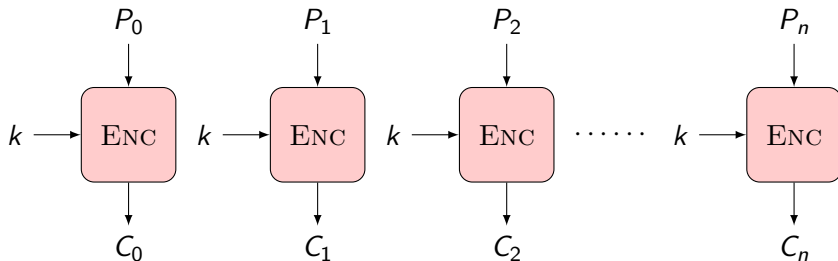


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Future HW: describe an attack to break CPA given ECB

Image Encryption using ECB

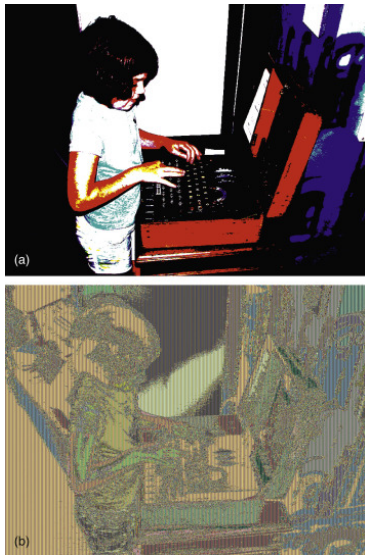
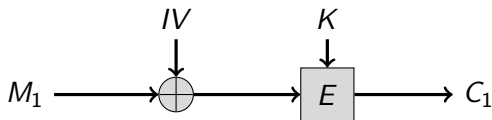


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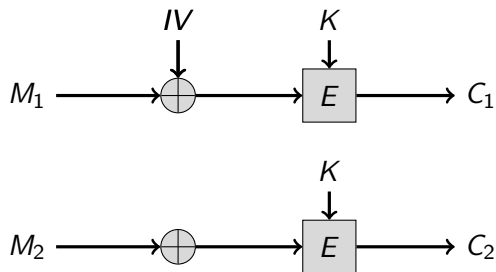
Cipher Block Chaining: CBC (not quite cryptocurrencies)

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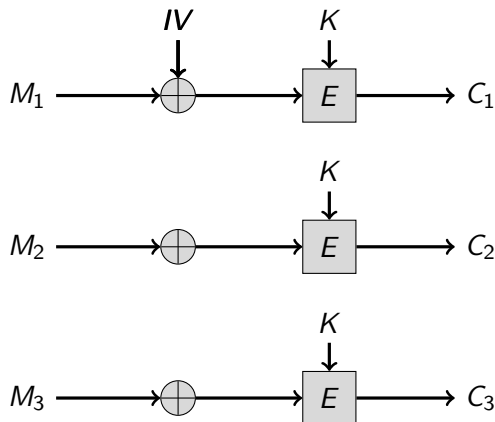
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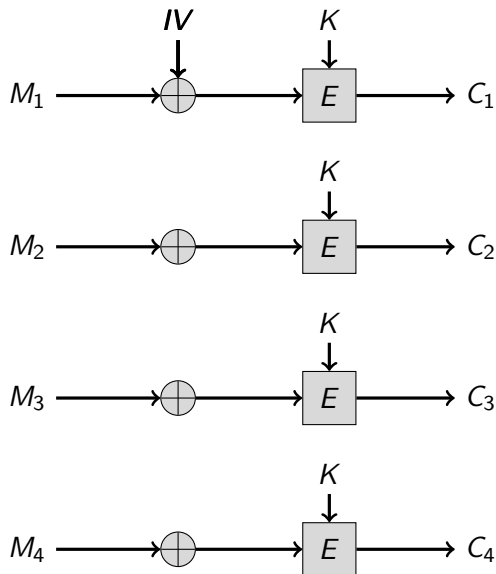
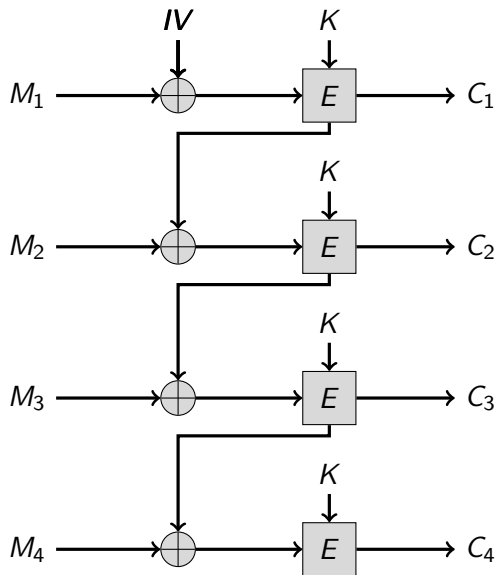


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- It is best to use a random IV every message and send it with the cipher text

Image Encryption using CBC vs ECB

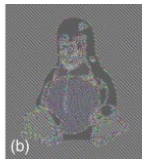


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