

UNIVERSITY OF CALIFORNIA
RIVERSIDE

MEASUREMENT OF THE LONGTIDUDIANL SINGLE SPIN ASYMMETRY,
 A_L , FOR POLARIZED PROTON-PROTON COLLISIONS IN THE $W \rightarrow \mu$
DECAY CHANNEL

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of the requirements for the degree of

Doctor of Philosophy

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by

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In no particular order now, but say something nice about each person.

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Some say that it takes a village to raise a child. The same can be said of raising a graduate student up to earning a PhD. This thesis is dedicated to the multitude who have helped me become the man I am today, and to students who struggle, and their mentors who do not give up on them.

ABSTRACT OF THE DISSERTATION

MEASUREMENT OF THE LONGITUDINAL SINGLE SPIN ASYMMETRY, A_L , FOR POLARIZED PROTON-PROTON COLLISIONS IN THE $W \rightarrow \mu$ DECAY CHANNEL

by

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University of California, Riverside, August 2016
Professor Kenneth Barish, Chairperson

This thesis discusses the process of extracting information about the spin structure of protons, specifically, spin contributions from the sea of quarks and antiquarks, which are kinematically distinct from the 'valence quarks'. We have known since the 'proton-spin crisis' [3] of the 1990s that proton spin does not entirely reside in the valence quarks, so the thrust of experimental efforts since then have been designed to determine both how to probe the proton spin structure, and how to validate models for proton spin structure. Here, I discuss one particular approach to understanding the sea-quark spin contribution, which utilizes the production of real W -bosons, and the W coupling with polarized spin structure in the proton sea, as produced from polarized proton collisions. Only one of the colliding protons is longitudinally spin polarized, in this analysis, and they are collided at an energy of 500GeV . The experimental observable used is referred to as " A_L " which is expressed mathematically as a ratio of sums and differences of various helicity combinations of singly polarized interactions between two protons, i.e. $p + p^{\Rightarrow} \rightarrow W \rightarrow \mu + \nu$. Once A_L has been experimentally measured, it can then be used to determine appropriate polarizations of proton sea-quarks, within a given uncertainty, if we write the cross-sections used in the calculation of A_L in terms of polarized parton distribution functions. Finally, this thesis will also include a discussion of my work experimentally determining the absolute luminosity of collisions at RHIC, which is needed as a normalization on any cross section used in the analysis. In particular, studying the cross section of the W interaction can help to validate our models for assigning a signal-to-background ratio to the $W \rightarrow \mu$ events.

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Chapter 1

Introduction

1.1 A Brief History of the Proton

The angular momentum of the proton has been a subject of study for the last 20 years[CITATION NEEDED]. One of the challenges of particle physics is to create a framework which can accurately describe matter, as well as predict the behavior of matter at all energy scales. The proton is a baryon which makes up the majority of the mass in the visible universe, yet fully understanding the origins of its properties - such as its mass and spin, still eludes us. However, through the applicaiton of the scientific method over many generations of physicists, we have magnificently described this important particle, and understood much of its properties. However, one property which still defies our descriptions is its fundamental angular momentum, spin.

Our understanding of the proton has evolved and sharpened since the first experiments in deep inelastic scattering showed that the proton is not a fundamental particle [5]. Gell-Mann later planted the seeds of a theoretical framework which could in part describe some of the structure of baryons, a class of hadrons which we may naively describe as composed of three 'valence quarks'[CITATION NEEDED]. We can apply well known spin-sum rules to the indivdual spins of the valence quarks which compose the proton in our naive valence-model to produce a correct prediction for the protons' spin $\frac{1}{2}$. When experimenters set out to measure the contribution of these valence quarks in 1988 at the EMC experiment [3], they were flabbergasted to find that the valence quarks carry only a small fraction of the proton's spin. Although recent papers [11] suggest that this 'spin crisis' is

simple due to misattribution of spin, most literature to date has focused on understanding how to model the proton with parton distribution functions. These parton distribution functions come in many varieties, and probe different degrees of freedom within the proton, in both the case of unpolarized parton distribution functions, and polarized parton distribution functions.

1.2 Scope and Objectives of This Work

This thesis will describe the research I carried out between May of 2010 through August of 2016. I will often quote work that was carried out in active collaboration with Ralf Seidel, Francesca Giordano, Daniel Jumper, Sanghwa Park, Abraham Meles and Chong Kim. Daniel, Abraham, Ralf, Francesca, and myself all worked on the 2013 polarized proton data set taken at RHIC with PHENIX. This analysis comprises the body of work devoted to calculating A_L for the $W \rightarrow \mu$ decay. Since 2013, the five of us collaborated closely on all aspects of the work, which provided invaluable cross-checks at nearly every stage. Many of the figures in this document were produced by our collective efforts, and I will do my best to cite when possible, if one analyzer played a particularly large role in generating the data or visualization, however after several years of working together, I will certainly fail to attribute, or misattribute at times.

The other portion of this thesis will discuss the Vernier Analysis, which is instrumental for every single-cross-section calculation taken with RHIC data. The thrust of the Vernier Analysis is to determine the beam luminosity at PHENIX's interaction point, so as to normalize these cross-section calculations. This is done with a series of specialized Vernier-Scans, where beams are scanned across one-another in order to measure beam geometry. The luminosity can then be calculated from first principals, and compared to the advertised machine luminosity published by RHIC's collider-accelerator department. I began working with the Vernier Analysis under the tutelage of K. Oleg Eyser, but eventually moved to work independantly on the analysis, producing an entire software framework for handling data cleaning, analysis, visualization and simulation.

Chapter 2

Physics Background

2.1 The Phenomena of Spin

Spin is a fundamental quantity possessed by all elementary particles. We use the word 'spin' to describe the property, because particles which possess spin, behave as though they have some kind of intrinsic, hidden rotation, as if they were 'spinning'. The dimension of spin, therefore is angular momentum. What is somewhat bizarre about spin, is that we do not observe anything physically spinning - although there are some phenomena (such as orbital angular momenta) which can be naively thought of as a 'spinning system' (but this description escapes classical analogy, due to its quantum, probabilistic nature). The role of Spin in Physics is of foundational importance, and yet, we have not successfully produced a model which can accurately predict the spin of hadrons.

The presence of spin in relativistic particles creates the phenomena of chirality, which has huge implications for how elementary particles can generate structure in matter itself **[CITATION NEEDED]**. In the case of the weak interaction, the presence of spin, which creates Chiral spinors breaks the left-right symmetry of weak coupling in matter (a fact which will be exploited in this thesis to probe the spin of the proton sea).

The phenomena of spin also changes the rules for how ensembles of particles may exist in a potential. Particles with spin are fermions, and because these particles must obey fermi statistics, we can observe structure in matter in the universe **[CITATION NEEDED]**. Without spin, the world as we know would collapse on itself, making any kind of extended non-exotic structures which currently exist by virtue of the Pauli exclusion principle, impossible.

2.2 A Brief History of Proton Spin

The study of Spin is really just an outgrowth of the general study of matter. Our models for matter, and the underlying structure of matter (in the modern sense), represents over a hundred years of experimental and theoretical efforts. The fundamental tool for this study is scattering. Scattering offers a very powerful method where one uses a well known initial state of matter (typically in the form of a beam), allows this beam to interact with an unknown configuration of matter, and measures the scattered beam. By carefully studying the kinematics of the scattered beam, we can create models which allow us to understand the structure of the target matter. We may also use these models to understand the interaction between the beam, and the target.

Although Gell-Mann's simple quark model of baryons [CITATION NEEDED] predicts the correct quantity for the spin of the proton, the work of Ashman et al (1988) [CITATION NEEDED] at the European Muon Collaboration directly measured a portion of the proton structure function g_1 and found that a rather small fraction of the proton spin comes from quarks - and most of the spin is carried by the gluons (Figure 2.1).



Figure 2.1: [FIGURE NEEDED] [CAPTION NEEDED]. Results of EMC experiment showing that the structure function g_1 , tells us a thing about proton spin.

2.3 Proton Spin Crisis

2.4 How to Model Proton Spin

- structure functions
- proton spin decomposition
- unpolarized parton distribution functions
- polarized parton distribution functions
- that sweet table from Delia hasch
- discussion \bar{q} , q , L_q , g
- DSSV figures

2.5 How to Measure Proton Spin

- physics probes for proton spin
- W cross section
- derivation of Asymmetry
- kinematic extremes of Asymmetry

2.5.1 Past Experimental Efforts

- summary of data on structure functions
- fixed target experiments
- collider experiments

2.6 World Efforts to Measure Proton Spin

2.6.1 CERN

ZEUS

HERA

HERMES

COMPASS

EMC

2.6.2 SLAC

2.6.3 JLAB

2.7 How to Measure Beam Luminosity in Collider Experiments

- vernier analysis note intro, equations
- summarize the papers on Luminosity

Chapter 3

Experimental Apparatus

3.1 The Relativistic Heavy Ion Collider

3.1.1 Overview

3.1.2 The RHIC Spin Program

3.1.3 Production of Polarized Proton Beams

3.2 The Pioneering High Energy Nuclear Interaction Experiment

3.2.1 Subsystem Overview

3.2.2 Luminosity

3.2.3 Beam Polarization

3.3 The Forward Upgrade

3.3.1 The Muon Tracker + Muon Trigger Subsystems

3.3.2 Resistive Plate Chambers

Design

Construction

Testing

Performance

3.3.3 The DAQ

2013 Data Set Triggers

Chapter 4

The Data Set

4.1 Overview

Now that we have discussed the various apparatuses provided by the PHENIX experiment, we can go into more depth with the process of engineering features. For this analysis, we consider only events which are identified by the Muon Arms subsystem as being muons. The raw data provided by PHENIX is quite complex, and at the hardware level is generally not too useful for physics analysis.

In this chapter, we will discuss the process of cleaning our data set, the goal of which is to get rid of background data, while keeping any event that could possibly contribute to the $W \rightarrow \mu$ signal. This cleaning is done in three stages. The first stage concerns applying a simple basic cut to our data set to remove events which are kinematically forbidden from having W boson parent particles, this is called the "Basic Cut".

After this, we label data with W_{ness} , which is an event's likelihood for coming from a W boson decay. Although this is part of data cleaning, since W_{ness} is an important parameter in the analysis, it is discussed in Section ??.

Finally, we must estimate the overall yield of μ resulting from the various proton helicity combinations, and the signal to background ratio characterizing that yield. Again, since this is also an important part of the physics, it is discussed in Section 5.2.6.

4.2 Analysis Variables and the Basic Cut

A brief summary of the kinematic variables used later in the analysis is given in Table 4.2. In addition four sets of RPC cluster variables exist which are being used as main RPC variables. These variables contain projections from either vertex, Station 1, 3 or the MuID road to the corresponding z positions of the RPCs based on the tracks in the PHMuoTracksOut node and are directly taken over from the RpcMuoTracks node in the dsts:

- newsngmuons→Branch("RpcMatchVtx",0,"Rpc3dca[_RecoTracks]/F:
Rpc3time[_RecoTracks]/F:Rpc3x[_RecoTracks]/F:Rpc3y[_RecoTracks]/F:
Rpc1dca[_RecoTracks]/F:Rpc1time[_RecoTracks]/F:Rpc1x[_RecoTracks]/F:
Rpc1y[_RecoTracks]/F");
- newsngmuons→Branch("RpcMatchSt1",0,"Rpc3dca[_RecoTracks]/F:
Rpc3time[_RecoTracks]/F:Rpc3x[_RecoTracks]/F:Rpc3y[_RecoTracks]/F:
Rpc1dca[_RecoTracks]/F:Rpc1time[_RecoTracks]/F:Rpc1x[_RecoTracks]/F:
Rpc1y[_RecoTracks]/F");
- newsngmuons→Branch("RpcMatchSt3",0,"Rpc3dca[_RecoTracks]/F:
Rpc3time[_RecoTracks]/F:Rpc3x[_RecoTracks]/F:Rpc3y[_RecoTracks]/F:
Rpc1dca[_RecoTracks]/F:Rpc1time[_RecoTracks]/F:Rpc1x[_RecoTracks]/F:
Rpc1y[_RecoTracks]/F");
- newsngmuons→Branch("RpcMatchMuID",0,"Rpc3dca[_RecoTracks]/F:
Rpc3time[_RecoTracks]/F:Rpc3x[_RecoTracks]/F:Rpc3y[_RecoTracks]/F:
Rpc1dca[_RecoTracks]/F:Rpc1time[_RecoTracks]/F:Rpc1x[_RecoTracks]/F:
Rpc1y[_RecoTracks]/F");

For the moment the timing and DCA distributions we use are those matching from station 1 for RPC1 and from station3 for RPC3. In addition, in order to improve the background rejection in the FVTX acceptance, for this analysis several new variables are added in relation to the FVTX-MuTr matching which were directly taken over from the corresponding methods in the PHMuoTracksOut node. Those are fvtx_dr, fvtx_dφ and fvtx_dθ which compare the FVTX tracklets radial position, azimuthal and polar angles with

Variable	Definition
η	Pseudorapidity, used in secondary likelihood cuts
χ_{track}^2	Standard chi2 of μ track Kalman fitter
$DG0, DDG0$	Roads generated in MUID+MuTr planes. $DG0$ is distance between first gap road and track. $DDG0$ is opening angle between road and track.
DCA_r, DCA_z	Distance of closest approach between μ track and beam axis (DCA_r). DCA_z is the distance between the track's intersection with PHENIX's z-axis and the event vertex.
$RpcDca_{1,3}$	Distance between extrapolated track at RPC 1 or 3, and hit cluster at RPC 1 or 3.
dw_{23}	Reduced azimuthal bending angle of track. $dw_{23} = p_T \sin(\theta)(\phi_2 - \phi_3)$
$fvtx_d\theta$	
$fvtx_d\phi$	FVTX matched track matching residuals for ϕ, θ, dr .
$fvtx_dr$	

Table 4.1: Summary of engineered features from the data set used in this analysis.

those of the MuTr as an extrapolated z position between the two. Another FVTX related addition is the FVTX hit multiplicity within a cone of **INPUT RANGE HERE** around the projected track. This variable will henceforth be called FVTX_cone.

The "Basic Cut" is defined:

In this W analysis one is interested in removing most lower momentum particles which originate predominantly from background processes while keeping most of the W decay muons. With the above cuts, we aim to reduce part of the fake muons background assuring a good muon track reconstruction ($DG0, DDG0$ and χ^2 cuts) and selecting tracks with momentum smaller than the maximum possible physical energy. After applying these basic cuts, the background will be further reduced via a likelihood method, described in chapter ??, where background and signal features will be studied in detailed.

The correlations between the several cut variables are shown in Fig. 5.2 for data and for the W-si. The only exception is the correlation between the vertex extrapolated variables DCA_z and DCA_r and the FVTX related matching variables. This is not entirely unexpected as both should be sensitive to the amount of multiple scattering in the central magnet yoke and initial shielding.

Variable	Lower Bound	Upper Bound
MuID lastGap	*	Gap 4
χ^2	0	20
$DG0$	0	20
$DDG0$	0	9
μ candidate	*	1

Table 4.2: The Basic Cuts used in the Run 13 analysis. lastGap refers to the last gap in the MuID which saw a μ candidate event. The fourth gap is the furthest penetration possible, therefore suggesting a high energy muon. Other parameters are described in table 4.1

4.3 Feature Engineering

4.3.1 Discriminating Kinematic Variables

4.3.2 Simulations

Chapter 5

Spin Analysis

5.1 Classification of Signal or Background Events

After producing our data set, engineering features which help us convert our experimental data into observables, we are then tasked with the problem of separating out signal events from background events. Many processes are capable of producing muons, many of which are dominant in the W boson kinematic regime (Figure 5.1).

Inclusive μ Production, 500 GeV/c

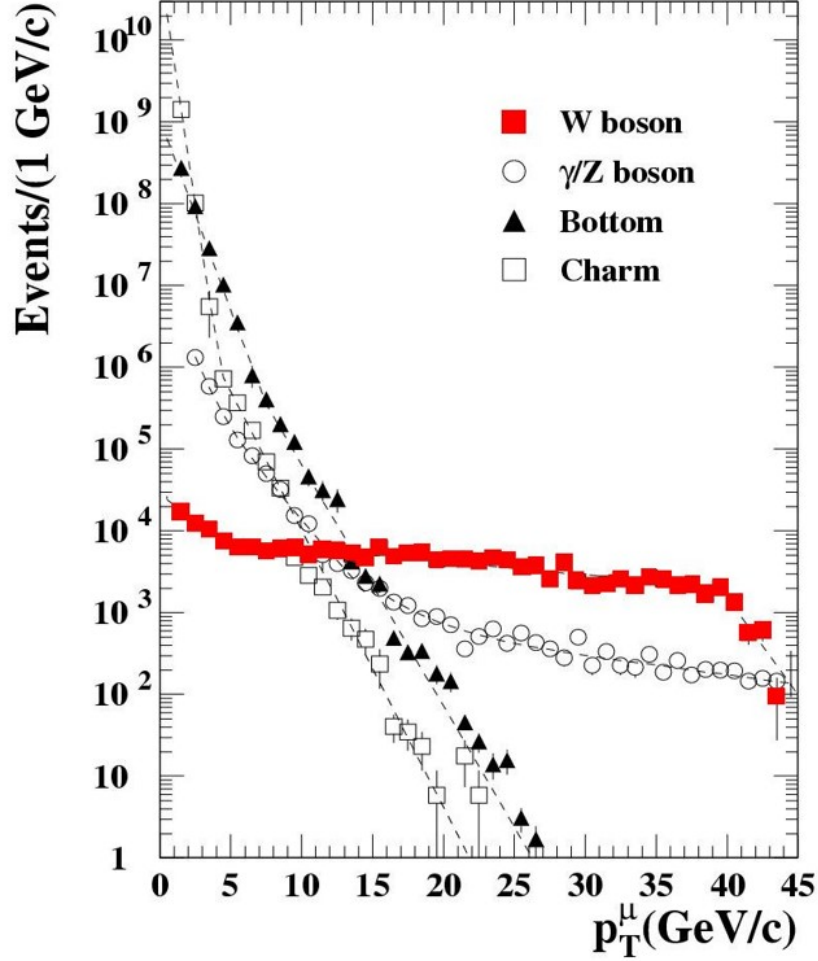


Figure 5.1: Observing the production of muon as a function of p_T , we can see that in the kinematic region of W production that the dominant sources of muons come from other processes. The new PHENIX muon trigger threshold is sensitive at 10 GeV/c and above.

We can divide up the total observed muon spectrum into contributions from three sources:

- Real Muon Background
 - Z, γ^*
 - $W \rightarrow \text{had}$

- $W \rightarrow \tau$
- onium
- open charm
- direct photon
- Fake Muons (Hadronic Background)
 - Hadrons which are reconstructed as high p_T muons due to detector resolution.
- Signal Muons
 - Real $W \rightarrow \mu$ events.

Previous analyses have attempted to separate the muon spectrum into p_T bins, to estimate the composition, however, because the $W \rightarrow \mu$ signal is so small in the forward kinematic regime, these methods are not sufficient, as there is no 'visible' cutoff in the spectrum. However, by using simulations. However, we may use other methods to split up our spectrum, with the ultimate goal of calculating A_L , and correcting for background dilution using the signal to background ratio. We must use another method to effectively describe the difference between an event which comes from a signal, vs background event.

5.1.1 Naive Bayes Classification

There are many techniques available for classifying a collection of variables (a feature set) into categories. Naive Bayes classification is an excellent candidate for classification, in cases where we have two classifications with distributions of featuresets which are uncorrelated. Naive Bayes even works when feature sets are slightly correlated. It is a robust, fast, scalable machine learning technique. Traditionally used for classification of text documents, Naive Bayes is also able to handle numeric features whose distributions are known [6].

In our analysis, we begin with a Naive Bayes classifier which is trained to classify two signal muons, vs background muons. We combine both Real Muon Background muons and Fake Muons (Hadronic Background Muons) in the label of "Background Muons" at this stage, though, later, we will separate out the muons further.

The descriniating variables described in 4 were chosen from the multitude of possible physical event parameters, because they were all maximally uncorrelated. Concretely, these correlations are presented in

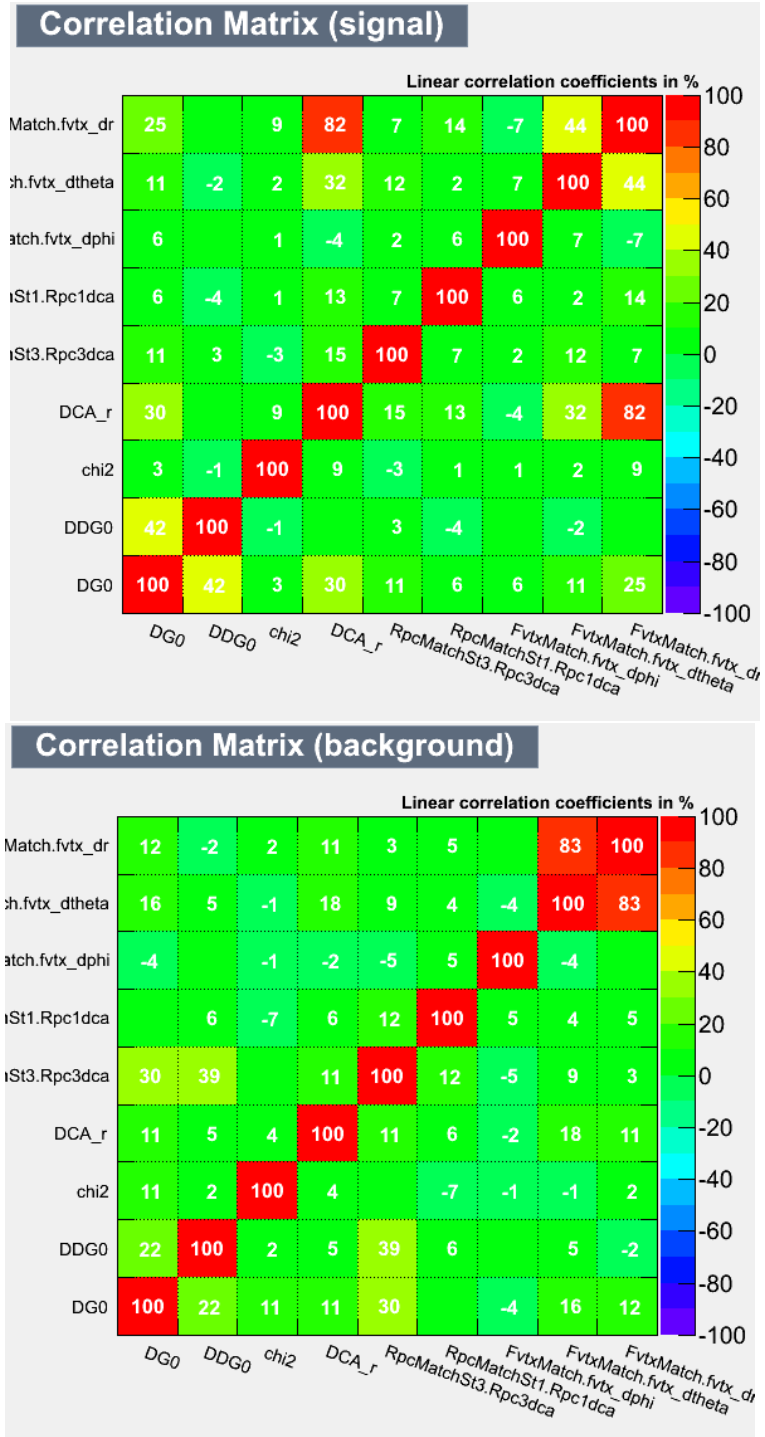


Figure 5.2: Low correlations between the signal variable distributions (from simulation), and the background variable distributions make this data set a good candidate for classification using Naive Bayes

Briefly, a Naive Bayes classifier may be constructed from the core of the familiar Bayes Theorem from probability and statistics.

In our case, we understand Naive Bayes as a conditional probability. Concretely, we consider a vector of features (i.e. our discriminating kinematic variables):

$$\mathbf{x} = (x_1, \dots, x_n) \quad (5.1)$$

and assume independence between each feature x_n . We then define the probability of a given classification, C_k given a set of features x_n :

$$p(C_k|x_1, \dots, x_n) \quad (5.2)$$

This conditional probability is defined in terms of Bayes Theorem:

$$p(C_k|\mathbf{x}) = \frac{p(C_k) p(\mathbf{x}|C_k)}{p(\mathbf{x})} \quad (5.3)$$

The terms here are defined as:

- $p(C_k) \rightarrow$ prior probability
- $p(\mathbf{x}|C_k) \rightarrow$ likelihood
- $p(\mathbf{x}) \rightarrow$ evidence

In principal, the final step in a classifier is to assign a class. This is done by computing the probability of a feature-set belonging to one class, or to another class, using Bayes Theroem. The class with the larger probability is than taken as the defacto classification of that particular feature set. However, we may instead observe these probabilities directly, and label data with this probability. This is what we ultimately call our " W_{ness} " parameter. This will be discussed in section ??.

5.1.2 Composition of Probability Distribution Functions

After we have engineered appropriate features to use in the analysis, we can proceed with composing probability density functions so we can proceed with the calculation of likelihoods, which will label our data set, allowing us to reduce our data set further from the basic cuts, without removing any signal events.

5.1.3 Labeling Data With Likelihood Ratio: W_{ness}

5.2 Extended Unbinned Maximum Likelihood Fits

5.2.1 Modeling The Hadronic Background

5.2.2 Modeling the Muon Background

5.2.3 Modeling the W-Signal

5.2.4 Overview

5.2.5 Fit Performance

5.2.6 S/BG and Muon Backgrounds

5.2.7 W_{ness} Dependence of S/BG

5.3 Calculation of A_L for $W \rightarrow \mu$

5.3.1 Overview

5.3.2 Asymmetry Calculation

5.3.3 Discussion of Work Done By Analysis Team

5.4 Data Validation

Mention Daniel's GPR, Ralf's PEPSI, Abraham's FVTX work, and Francesca's cross-checks.

- 5.4.1 Simulations and The Signal to Background Ratio
- 5.4.2 Gaussian Process Regression
- 5.4.3 Four Way Cross Validation
- 5.4.4 Asymmetry Consistency Check
- 5.4.5 Beam Polarization
- 5.4.6 Beam Luminosity
- 5.4.7 Code Cross Validation

Chapter 6

The Vernier Analysis

6.1 Overview

6.2 Analysis Note Here

6.3 W Cross Section

Chapter 7

Discussion and Conclusion

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